

## **SNS COLLEGE OF TECHNOLOGY** (An Autonomous Institution)

# **CO-ORDINATE SYSTEMS**











## **Coordinate systems:**

- Coordinates systems are often used to specify the position of a point, but they may also be used to specify the position of more complex figures such as lines, planes, circles or spheres.
- The choice of the coordinate system is based on the problem one is studying.
- Certain problems are solved easily by using rectangular coordinate systems whereas certain others are not.
- Some coordinate systems make more sense, make it easier to describe a system.
- Coordinates give you a systematic way of naming the points in a space.

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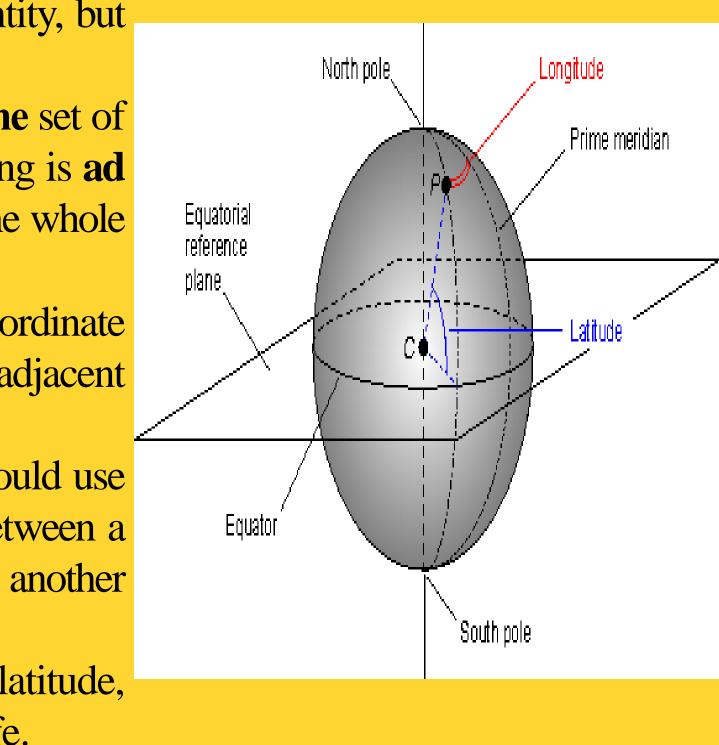




- Consider the set of locations in your room. Each point has a unique identity, but they **don't** come with names.
- We can use descriptions, like "the point at the corner of the desk", or "the set of points exactly three inches from the top of the **lamp**", but that sort of thing is **ad hoc**. If we can name them systematically, we can start reasoning about the whole space.
- A simple way to systematically name every point, called a Cartesian coordinate system, is to give its perpendicular distance from the floor and two adjacent walls—each point gets a unique name in this system.
- If the room is circular, you'd have to make an imaginary wall, or you could use the height from the floor, the distance from the center, and the angle between a line from the center through the point and a line from the center through another fixed point, like the door. This is an example of cylindrical coordinates.
- On the globe, we systematically name locations by giving their latitude, longitude, and altitude. you're using a spherical coordinate plane in real life.

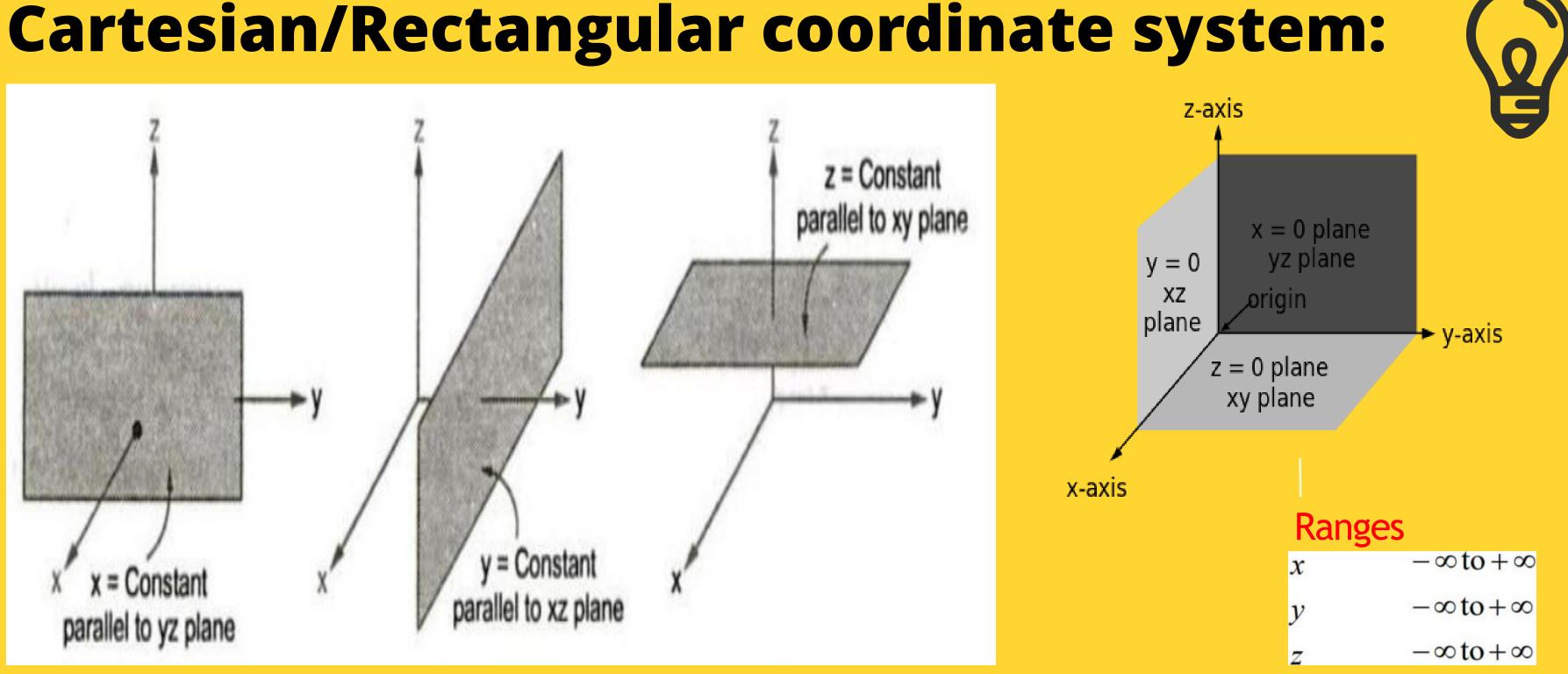
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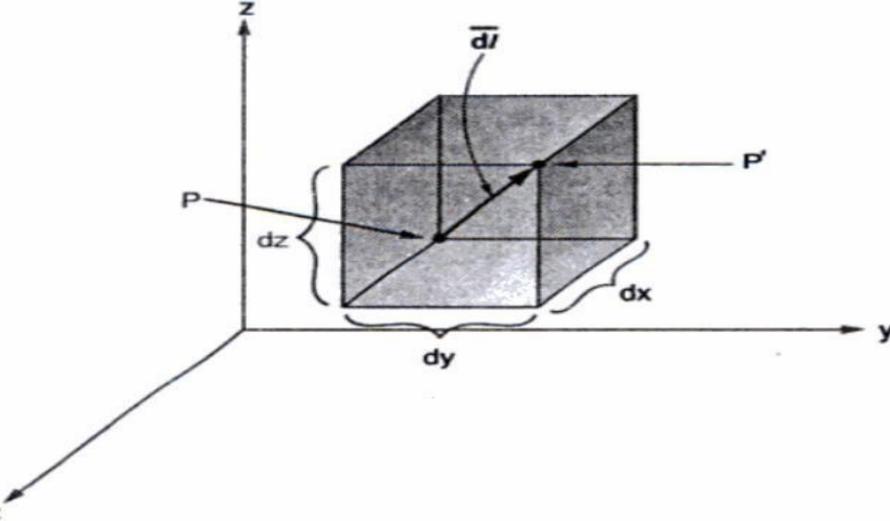
### **Cartesian/Rectangular coordinate system:**

- dx = Differential length in x direction
- Differential length in y direction dy
- dz = Differential length in z direction

$$\overline{dl} = dx \,\overline{a}_x + dy \,\overline{a}_y + dz \,\overline{a}_z$$

$$\left|\overline{dI}\right| = \sqrt{(dx)^2 + (dy)^2 + (dz)^2}$$

$$d\mathbf{v} = d\mathbf{x} d\mathbf{y} d\mathbf{z}$$
  
 $d\mathbf{\bar{S}} = dS \mathbf{\bar{a}}_n$ 



dS = Differential surface area of the element where

 $\bar{a}_n =$ Unit vector normal to

the surface dS

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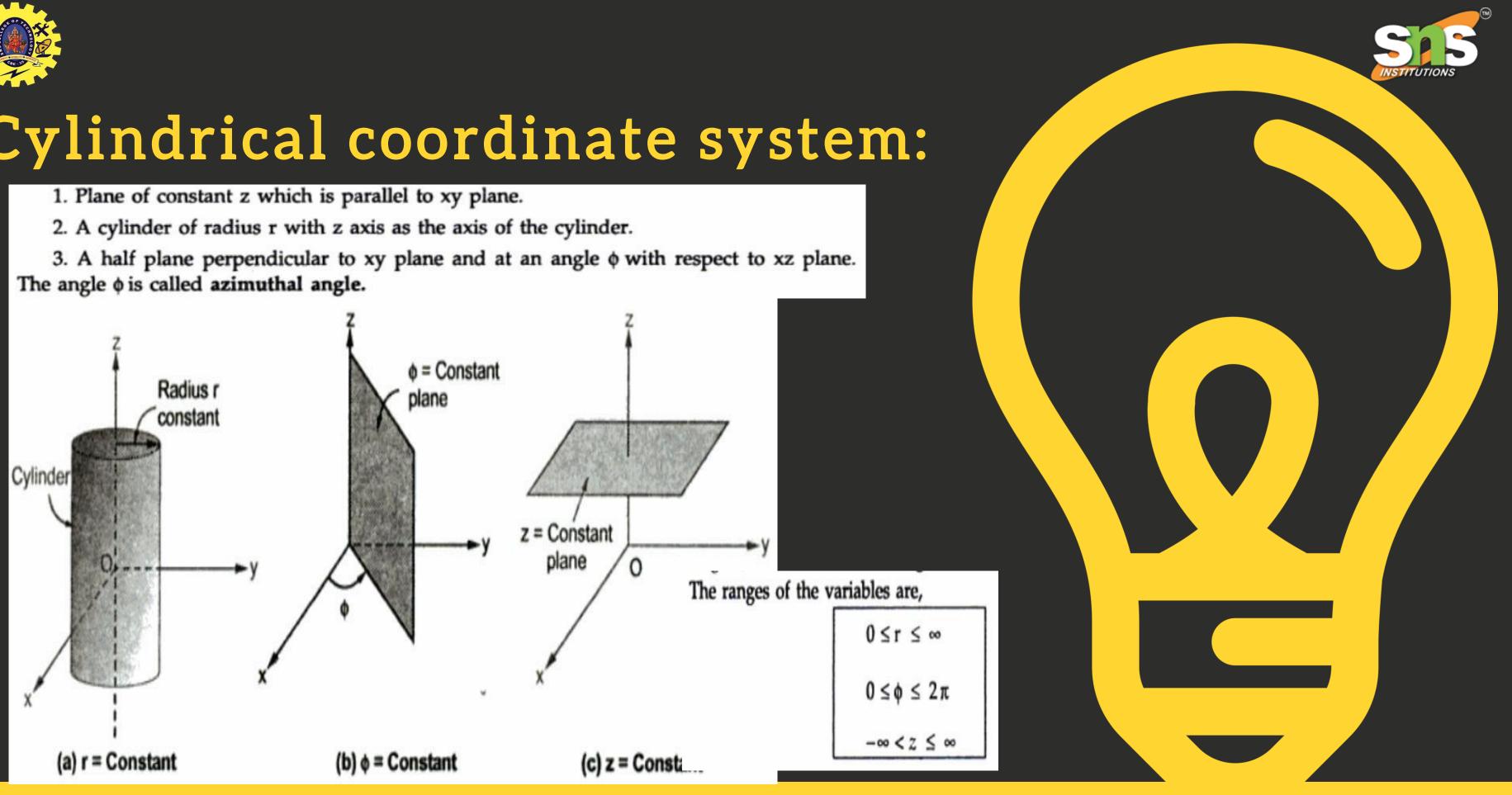








## Cylindrical coordinate system:



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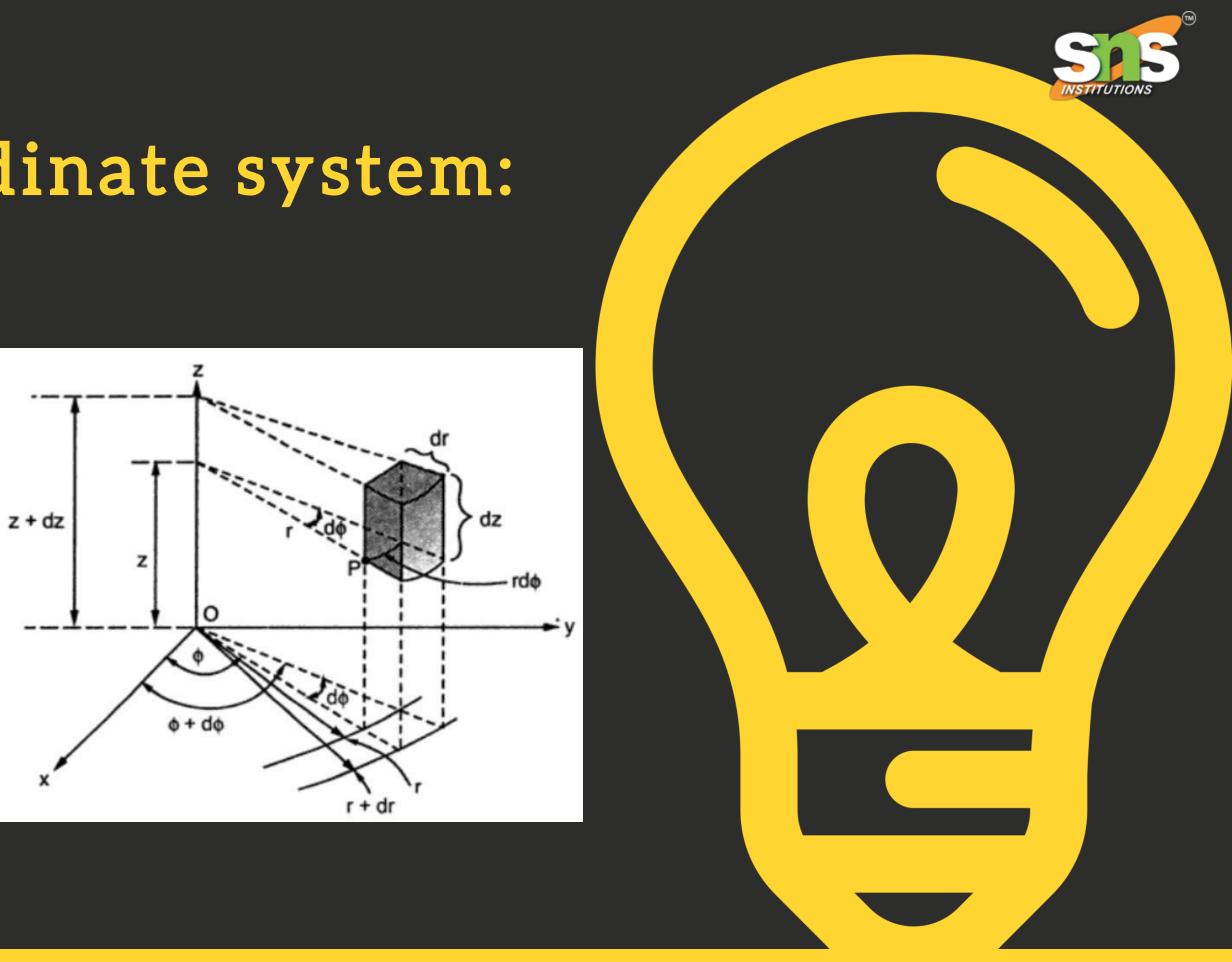
### Cylindrical coordinate system:

Differential length in r direction dr = r dø dz = Differential length in z direction

$$\overline{\mathbf{d}l} = \mathrm{dr} \ \overline{\mathbf{a}}_r + \mathrm{r} \ \mathrm{d}\phi \ \overline{\mathbf{a}}_\phi + \mathrm{dz} \ \overline{\mathbf{a}}_z$$

$$|\overline{\mathbf{d}l}| = \sqrt{(\mathbf{d}r)^2 + (r\,\mathbf{d}\phi)^2 + (\mathbf{d}z)^2}$$

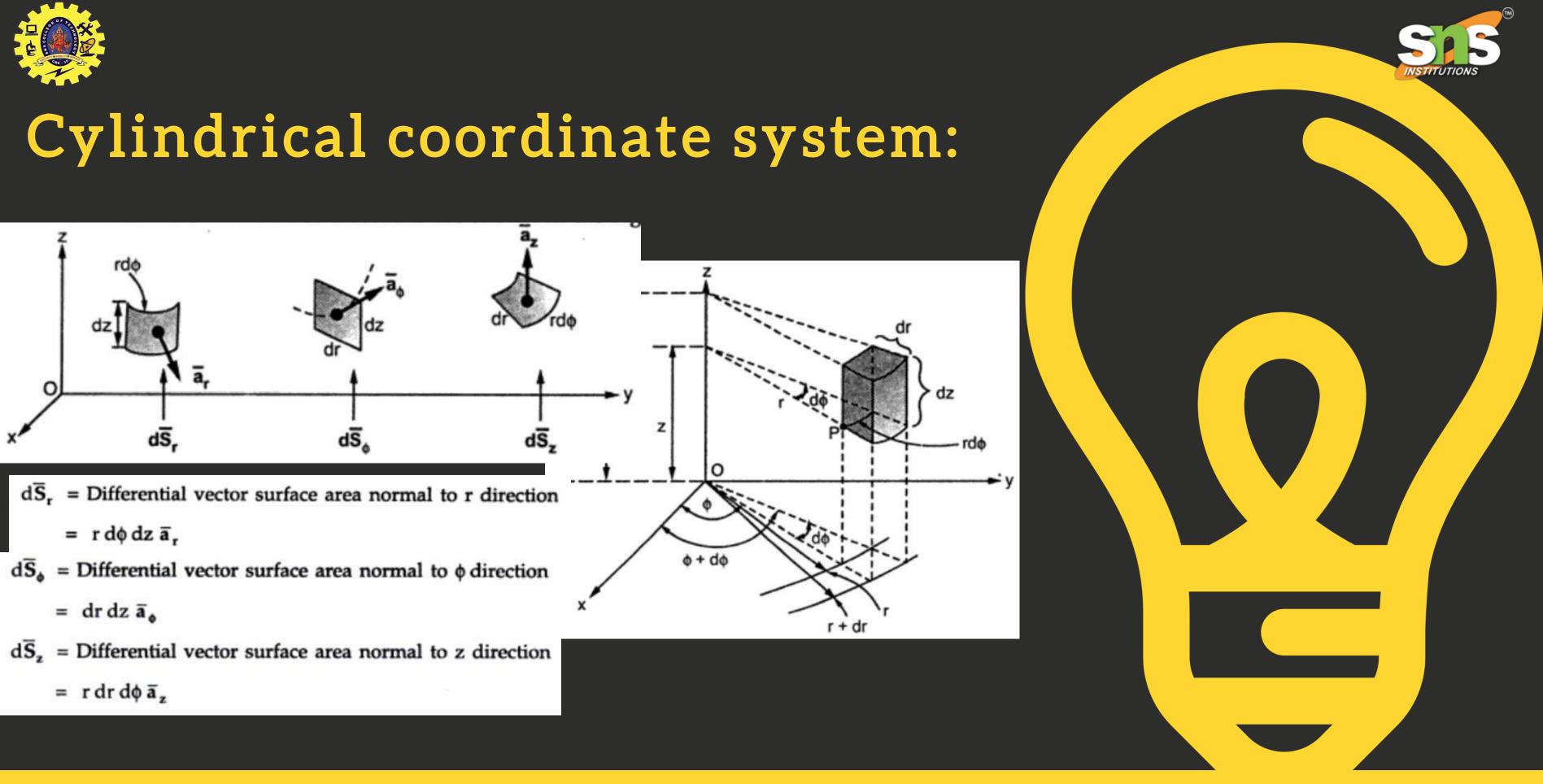
$$dv = r dr d\phi dz$$



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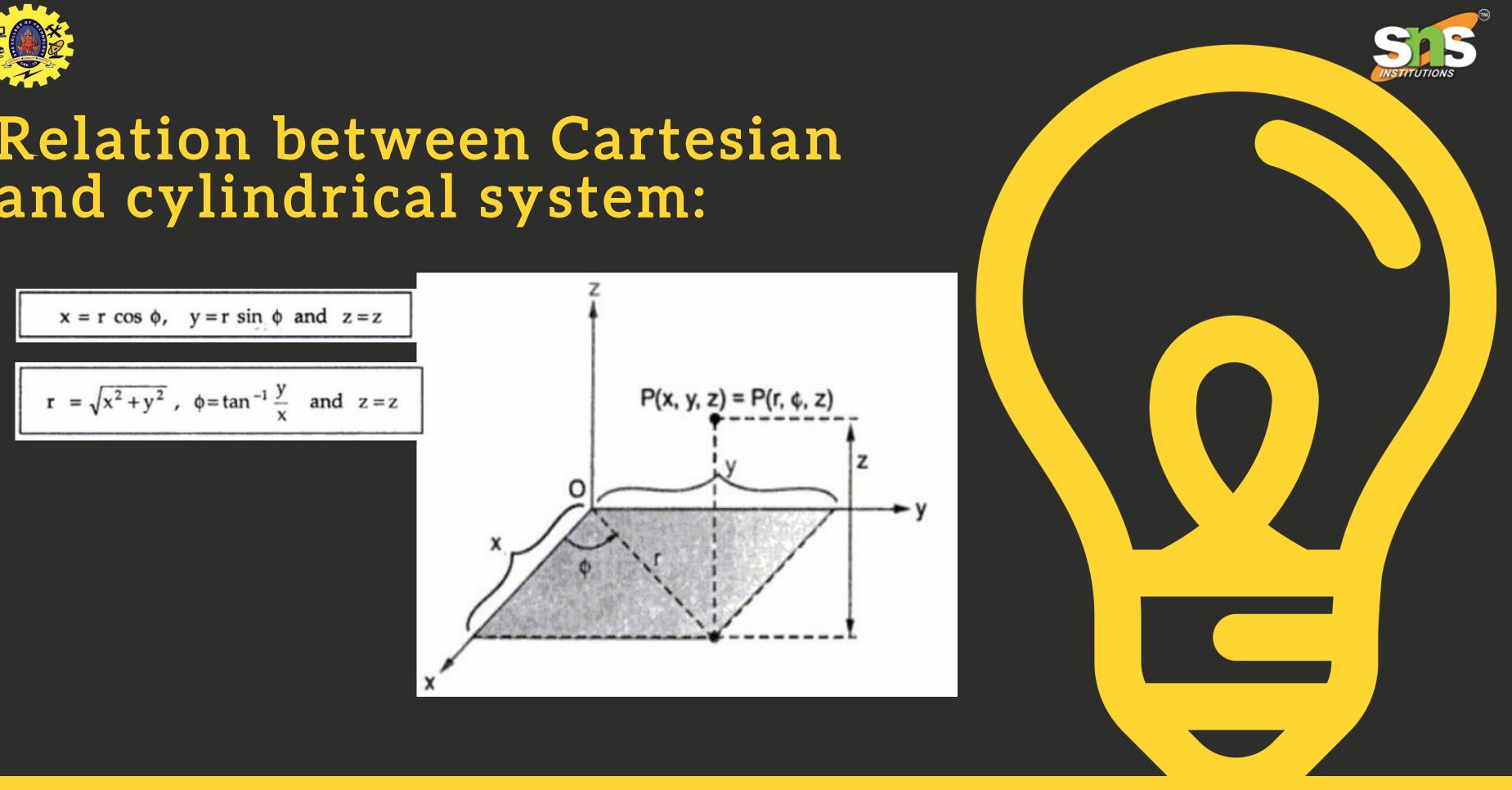




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### **Relation between Cartesian** and cylindrical system:



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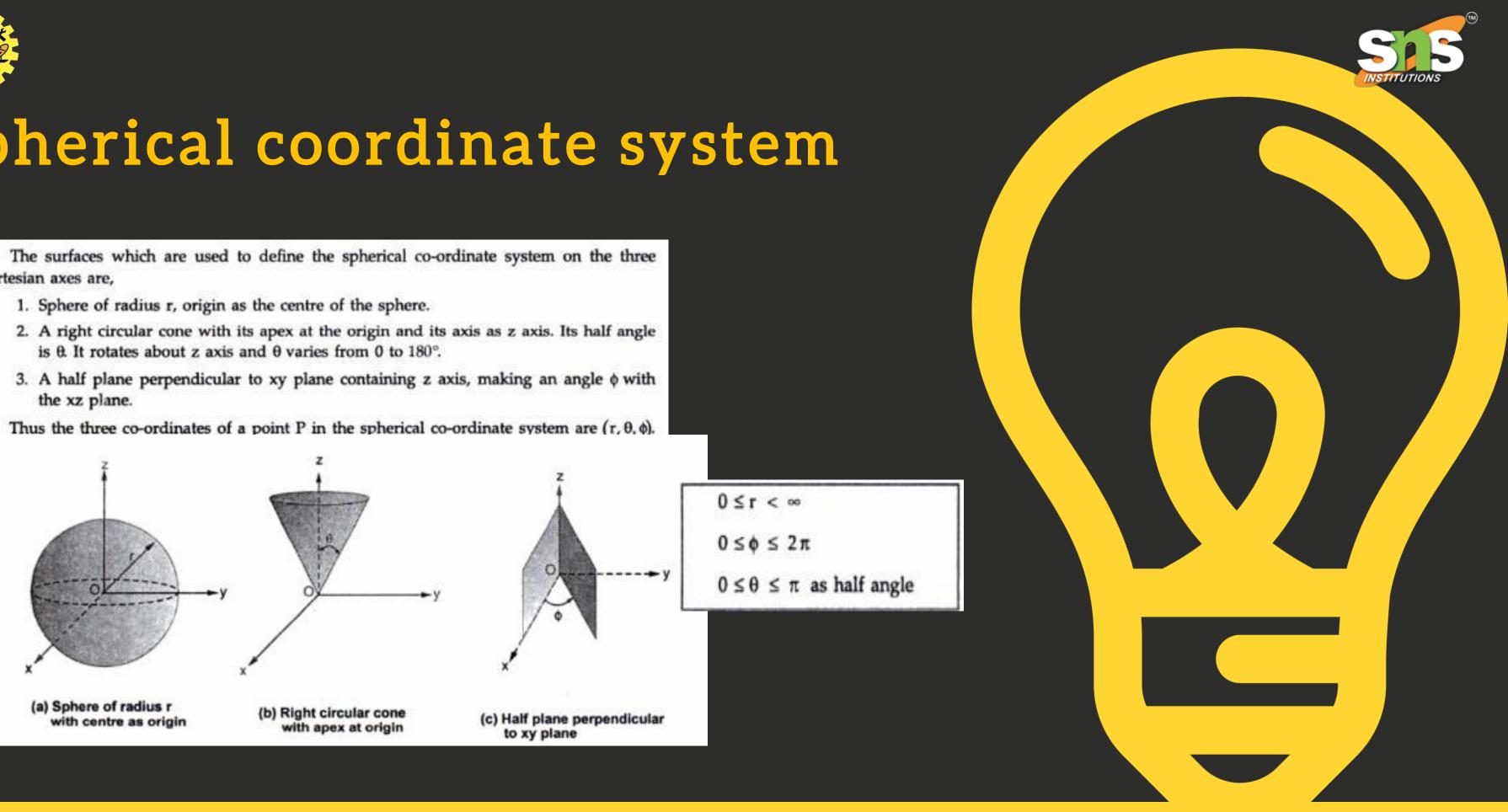




## Spherical coordinate system

cartesian axes are,

- is  $\theta$ . It rotates about z axis and  $\theta$  varies from 0 to 180°.



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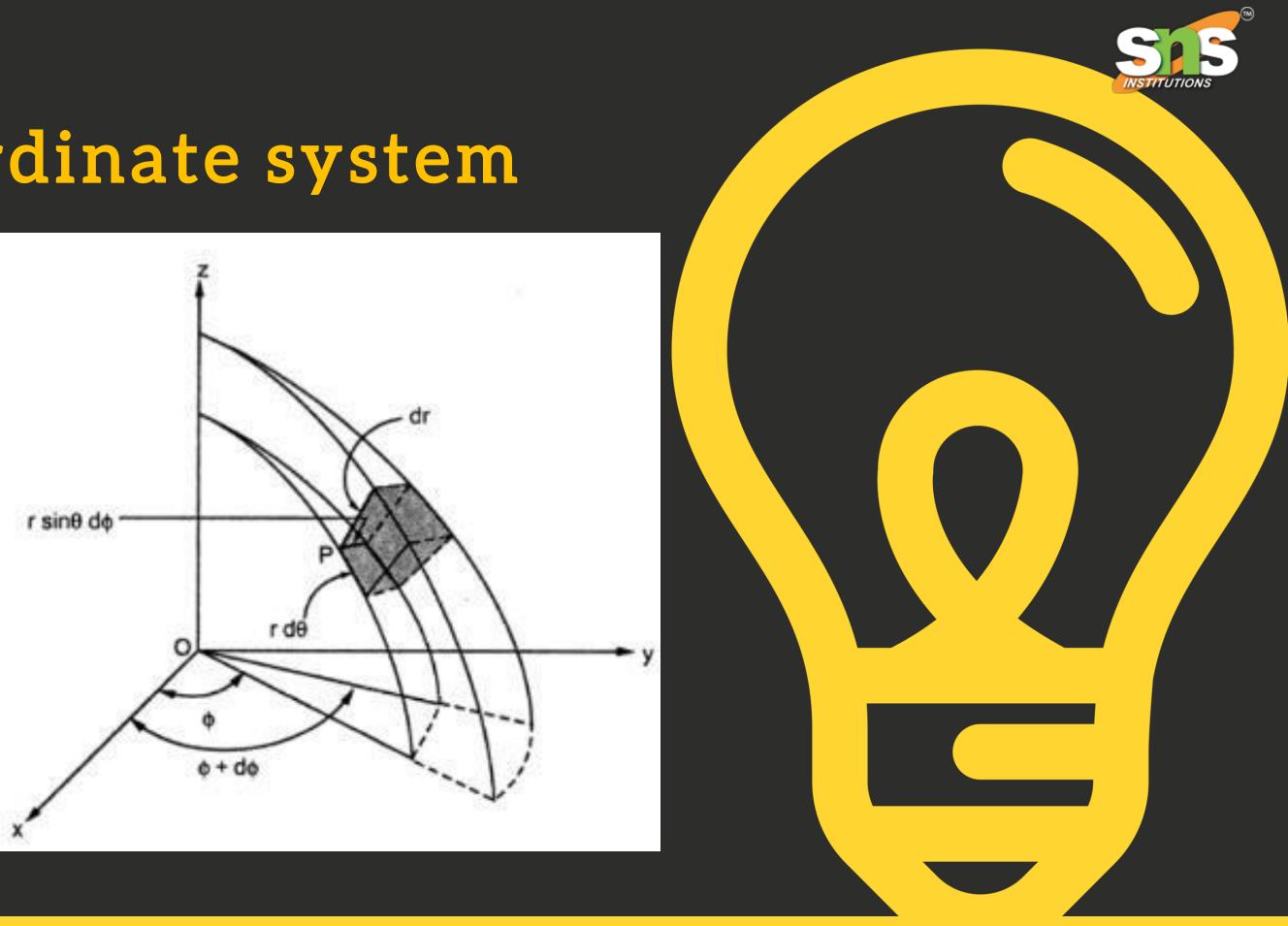
### Spherical coordinate system

Differential length in r direction dr =  $r d\theta$  = Differential length in  $\theta$  direction  $r \sin \theta d\phi = Differential length in \phi direction$ 

 $dl = dr \, \bar{a}_r + r d\theta \, \bar{a}_\theta + r \sin \theta d\phi \, \bar{a}_\phi$ 

 $\left| \overline{dI} \right| = \sqrt{(dr)^2 + (r d\theta)^2 + (r \sin \theta d\phi)^2}$ 

 $dv = r^2 \sin \theta dr d\theta d\phi$ 



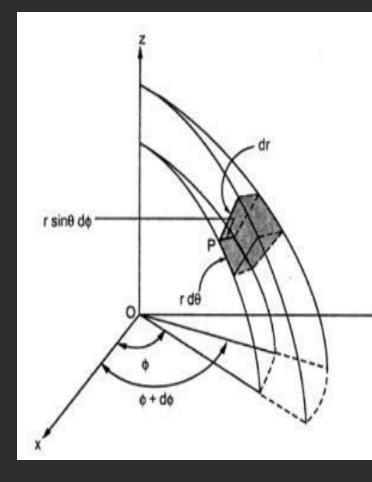
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## Spherical coordinate system

- $dS_r$  = Differential vector surface area normal to r direction
  - $= r^2 \sin \theta d\theta d\phi$
- $d\overline{S}_{\theta}$  = Differential vector surface area normal to  $\theta$  direction
  - $= r \sin \theta dr d\phi$
- $dS_{\phi}$  = Differential vector surface area normal to  $\phi$  direction
  - $= r dr d\theta$



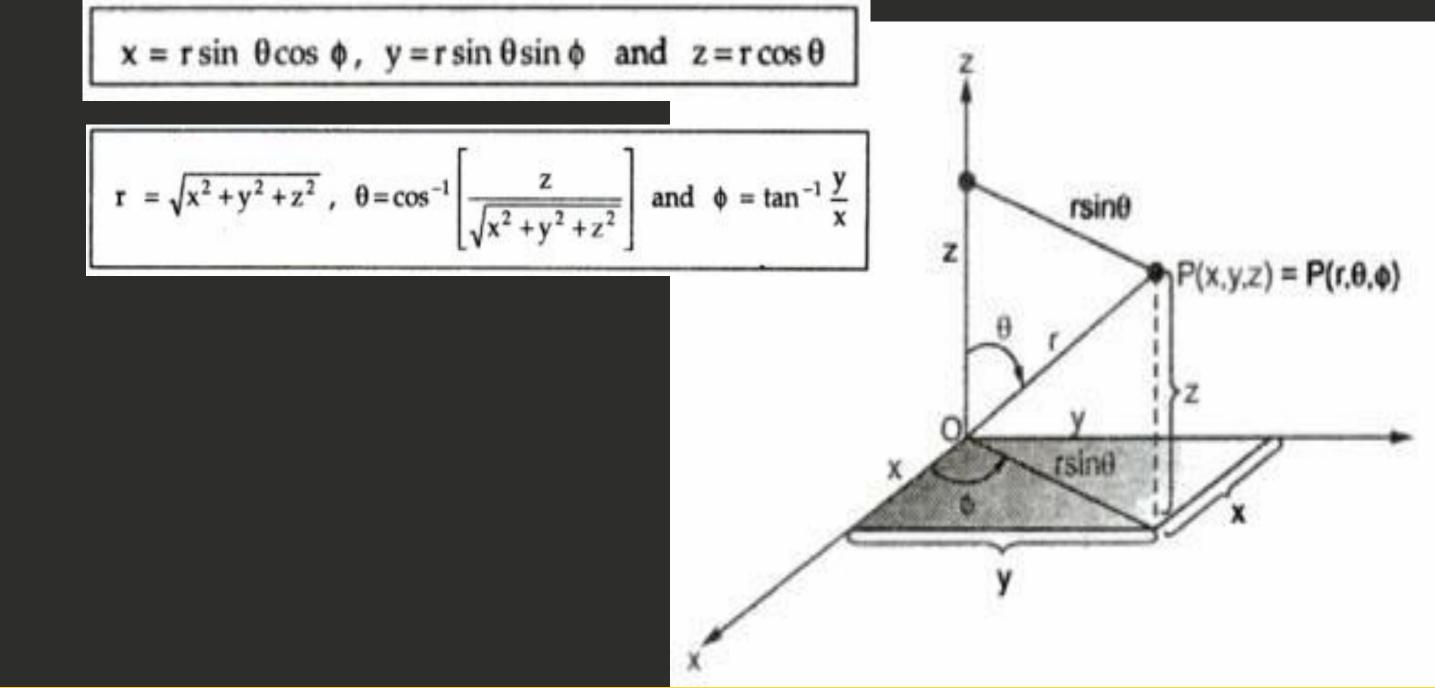
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### **Relation between Cartesian and spherical** system



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# THANK YOU



