



Problem



- 1) A torsion bar suspension is to be designed to support a maximum static load of 3433.5 N at the end of a lever arm 250 mm long. The deflection of the lever above the horizontal is to be 30° with a total angle of deflection of 90° . Assuming a safe allowable stress of 784800 kPa. Calculate (a) diameter of torsion bar (b) The effective length (c) The load rate

Given data:

$$\text{static load} = 3433.5 \text{ N}$$

$$\text{Dynamic load} = 2 \times \text{static load.}$$

$$= 2 \times 3433.5$$

$$= 6867 \text{ N}$$

$$l = 250 \text{ mm}$$

$$\theta = 90^\circ$$

$$\alpha = 30^\circ$$

$$f_s = 784800 \text{ kPa}$$

$$E_s = 784.8 \text{ MPa}$$
$$= 784.8 \text{ N/mm}^2$$



① → ②



$$C \text{ (or) } G = 73575 \times 10^6 \text{ Pa (considering)} \\ = 73575 \text{ N/mm}^2$$

To find:

- (i) d
- (ii) L
- (iii) α

Solution

$$d = \sqrt[3]{\frac{16 T_{\max}}{\pi f_{s\max}}}$$

$$T = W \times y$$

$$y = l \cos \alpha$$

$$= 250 \cos 30$$

$$\boxed{y = 216.5 \text{ mm}}$$

$$T = 6867 \times 216.5$$

$$\boxed{T = 1.487 \times 10^6 \text{ N}\cdot\text{mm}}$$

$$d = \sqrt[3]{\frac{16 T_{\max}}{\pi f_{s\max}}}$$



$$d = \sqrt[3]{\frac{16 \times 1.487 \times 10^6}{\pi \times 784.8}}$$

$$\boxed{d = 21.2 \text{ mm}}$$

$$(ii) \quad L = \frac{G \theta_{\max} d}{2 f_s \max}$$

$$= \frac{73575 \times 90 \times 21.2}{2 \times 784.8}$$

$$= \frac{73575 \times \frac{\pi}{2} \times 21.2}{2 \times 784.8}$$

$$\cancel{L = 1561 \text{ mm}} \quad \boxed{L = 1561 \text{ mm}}$$

$$\theta_{\max} = 90^\circ$$

$$\theta_{\max} = \frac{\pi}{180} \times 90$$

$$= \frac{\pi}{2} \text{ radians}$$

$$(iii) \quad r = \frac{\pi d^4 G + 32 L W x}{32 L (l^2 - x^2)}$$

$$x = l \sin \alpha$$

$$= 250 \times \sin 30$$

$$\boxed{x = 125 \text{ mm}}$$



① → ②



$$\tau = \frac{(\pi d^3 (21.2)^4 \times 73575) + (32 \times 1561 \times 6867 \times 125)}{32 \times 1561 (250^2 - 125^2)}$$

$$\tau = 38.25 \text{ N/mm}$$

(or)

$$\tau = 38250 \text{ N/m}^2$$

Result:

$$d = 21.2 \text{ mm (or) } d = 0.021 \text{ m}$$

$$L = 1561 \text{ mm (or) } L = 1.56 \text{ m}$$

$$\tau = 38.25 \text{ N/mm (or) } \tau = 38250 \text{ N/m}^2$$