



**SNS COLLEGE OF TECHNOLOGY**

(An Autonomous Institution)

Coimbatore-35

# Elevator effects - Stick fixed Neutral point

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# What is the neutral point?

- **Neutral point.** A mathematical analysis of the longitudinal static stability of a complete **aircraft** (including horizontal stabilizer) yields the position of center of gravity at which stability is **neutral**. This position is called the **neutral point**.

## 5-5 Neutral Point (Stick-fixed)

From the studies just completed, the final stability equation can be written for the airplane in gliding flight with fixed controls with no propeller:

$$\frac{dC_m}{dC_L} = \frac{x_a}{c} + \left( \frac{dC_m}{dC_L} \right)_{\substack{\text{fus} \\ \text{Nac}}} - \frac{a_t}{a_w} \bar{V}_{\eta_t} \left( 1 - \frac{d\epsilon}{d\alpha} \right) \quad (5-32)$$

and the equilibrium equation:

$$C_{m_{eq}} = C_L \frac{x_a}{c} + C_{m_{ac}} + C_{m_{fus}} - \frac{a_t}{a_w} C_L \bar{V}_{\eta_t} \left( 1 - \frac{d\epsilon}{d\alpha} \right) - a_t(\alpha_0 - i_w + i_t) \bar{V}_{\eta_t} \quad (5-33)$$

The contributions of the various airplane components to its static longitudinal stability ( $dC_m/dC_L$ ) are shown in Figure 5-17.

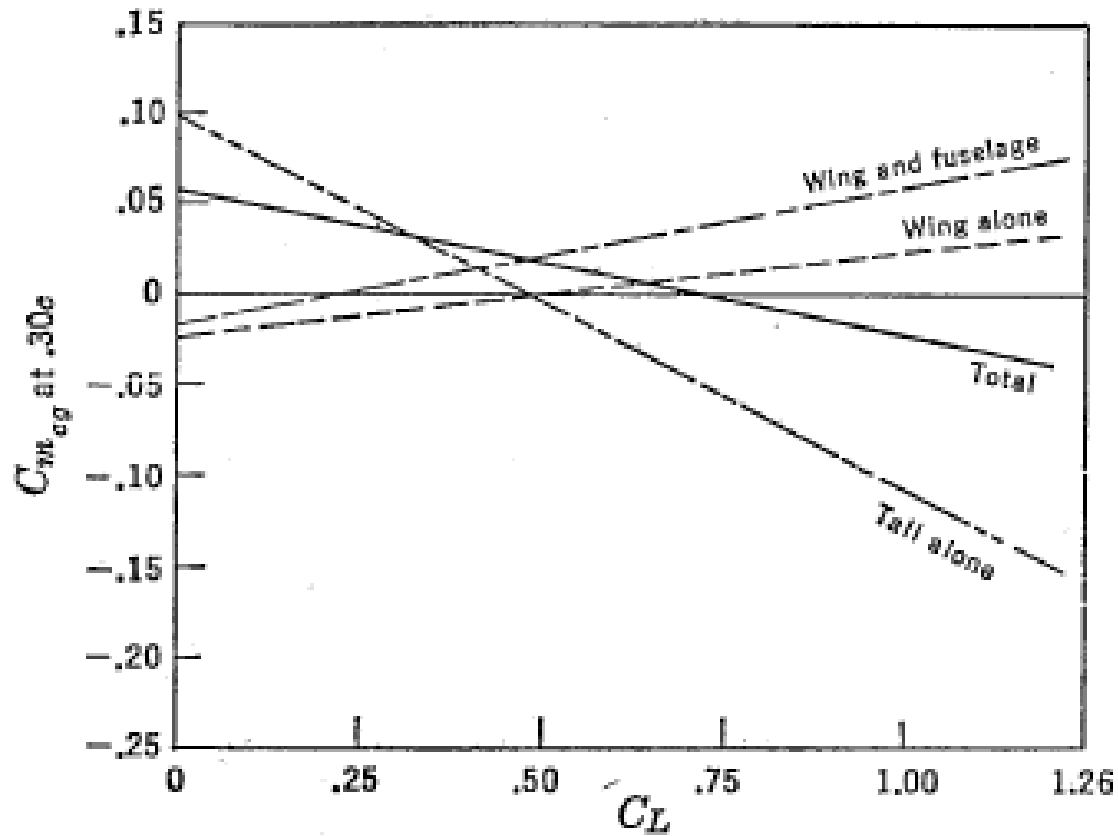


FIGURE 5-17. Typical longitudinal stability breakdown.

$$\left( \frac{dC_m}{dC_L} \right)_{\text{Wing}} = x_{cg} - x_{ac}$$

$$N_0 = x_{cg}(dC_m/dC_L=0) = x_{ac} - \left( \frac{dC_m}{dC_L} \right)_{\substack{\text{Fus} \\ \text{Nac}}} + \frac{a_t}{a_w} \bar{V}_{\eta t} \left( 1 - \frac{de}{d\alpha} \right)$$



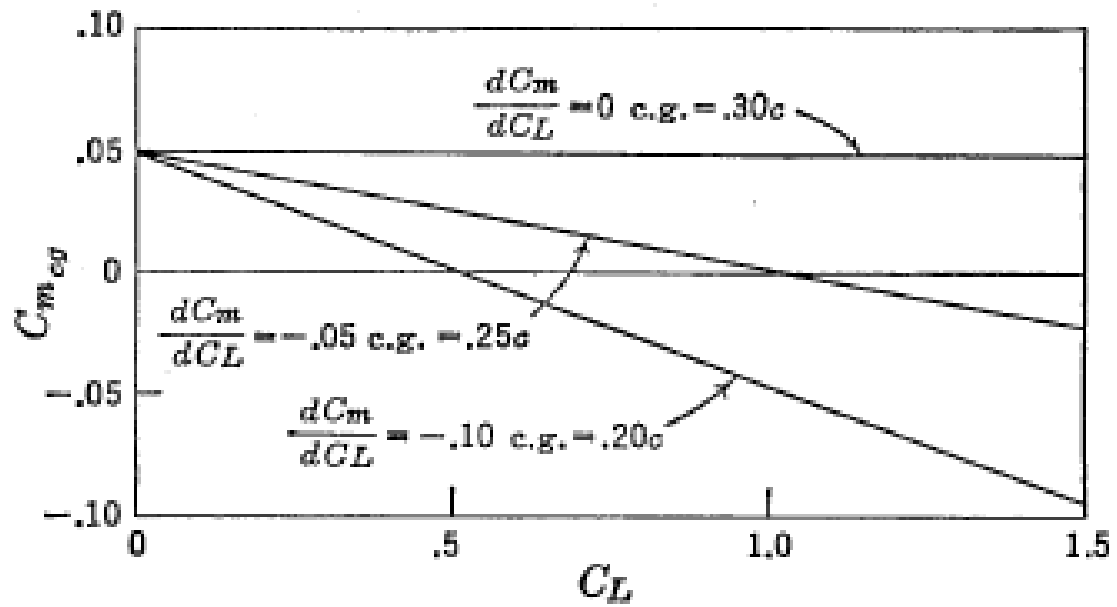


FIGURE 5-18. Typical effect of c.g. shift on pitching moments.

$$\frac{dC_m}{dC_L} = x_{cg} - N_0$$

# Static margin

- In aircraft analysis, **static margin** is defined as the distance between the center of gravity and the neutral point of the aircraft, expressed as a percentage of the mean aerodynamic chord of the wing.



# ELEVATOR EFFECT

$$\frac{dC_m}{d\delta_e} = - \left( \frac{dC_L}{d\alpha} \right)_t \bar{V}_{\eta_t} \frac{d\alpha_t}{d\delta_e}$$

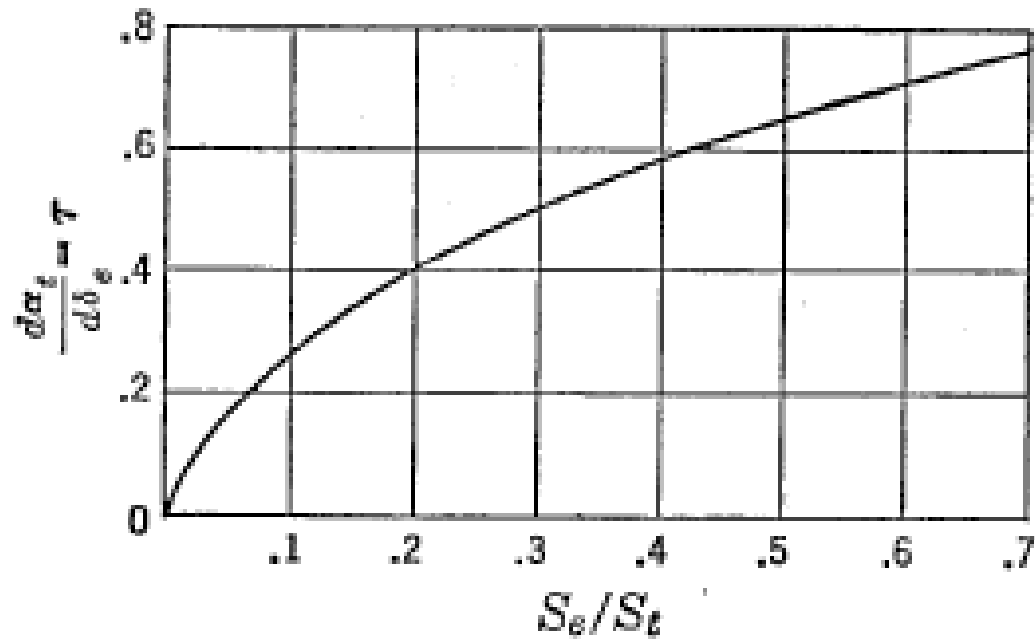


FIGURE 5-33. Elevator effectiveness.

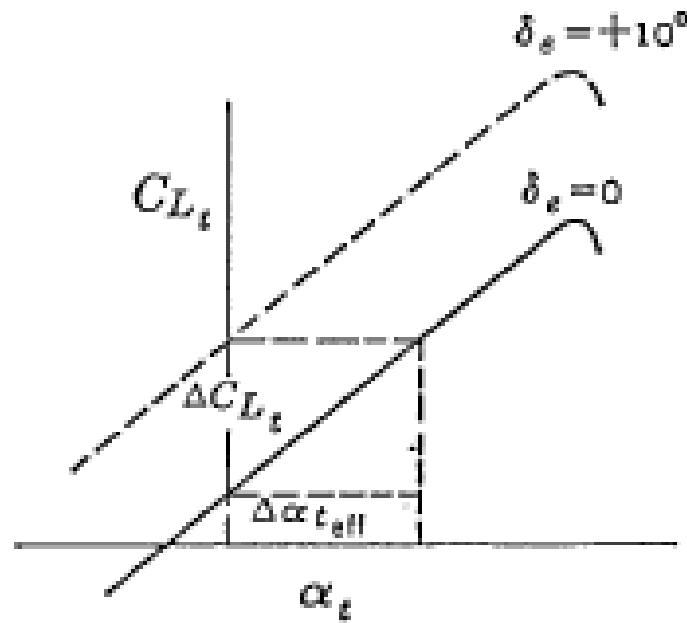


FIGURE 5-34. Effect of elevator deflection on horizontal tail lift.

# Elevator Angle versus Equilibrium Lift Coefficient

$$\alpha_t = (\alpha_w - \epsilon - i_w + i_t + \tau\delta_e)$$

The propeller-off equilibrium equation can be rewritten

$$C_{m_{cg}} = C_{m_{ac}} + C_L \frac{x_a}{c} + C_{m_{fus}} + C_{m_{nac}} - a_t(\alpha_w - \epsilon - i_w + i_t + \tau\delta_e) \bar{V} \eta_t$$



with  $\delta_{e0}$  the elevator angle at zero lift:

$$\delta_e = \delta_{e0} + \frac{d\delta_e}{dC_L} C_L$$

$$\frac{d\delta_e}{dC_L} = - \frac{dC_m/dC_L}{C_{m\delta}}$$

This c.g. will then be the neutral point sought, and the slope  $dC_m/dC_L$  will also be zero.

