



**SNS COLLEGE OF TECHNOLOGY**  
**An Autonomous Institution**  
**Coimbatore-35**



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Approved by AICTE, New Delhi & Affiliated to Anna University, Chennai

**DEPARTMENT OF ELECTRONICS & COMMUNICATION ENGINEERING**

**19ECB301-ANALOG AND DIGITAL COMMUNICATION**

III YEAR/ V SEMESTER

**UNIT 1 – ANALOG COMMUNICATION**

**TOPIC – AMPLITUDE MODULATION**



# AMPLITUDE MODULATION

19EC301 - Analog and Digital Communication.

Unit - 1 - Analog Communication

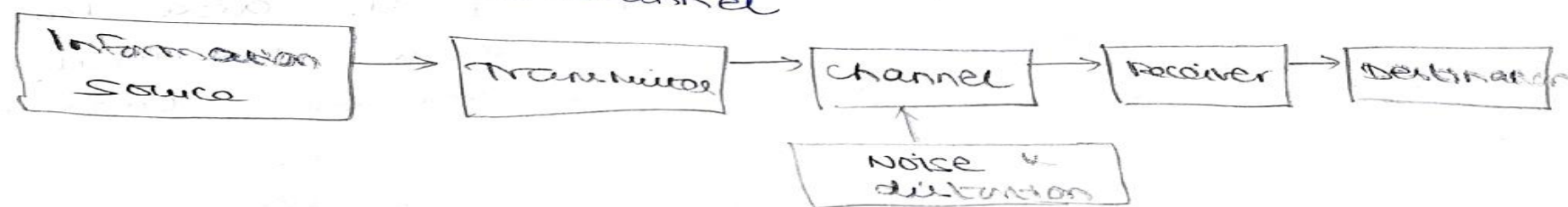
\* Introduction to Communication systems:

Communication is the process of establishing a connection b/w two points for information exchange.

Telecommunication: Long distance communication

Communication Components:

- Transmitter
- Receiver
- Channel



Without Modulation:

There are some disadvantages:

- Large antenna heights
- Short range of communication
- Signals get mixed up
- Multiplexing is not possible.

\* Modulation:

Modulation is defined as the process by which some parameter of the carrier signal (high frequency signal) is varied in accordance with the instantaneous values of the modulation signal.



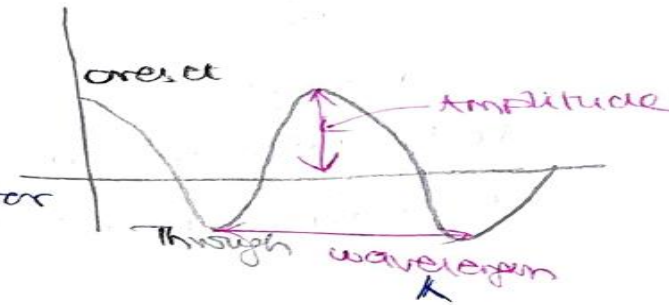
# AM MATHEMATICAL REPRESENTATION



**Frequency:**  
Number of cycles of a waveform per second.  
Unit is hertz.

**wavelength:**  
Distance b/w two points of similar cycles of a periodic wave.  
$$\lambda = \frac{c}{f} = \frac{3 \times 10^8 \text{ m/s}}{f}$$

**Bandwidth:**  
Freq range through which info is being transmitted.



**\* AM (Amplitude Modulation):**

It is defined as the process by which amp of the carrier signal is varied in accordance with the instantaneous value of the modulating signal, but freq and phase remains constant.

**Mathematical representation of an AM wave:**

Let the Modulating signal be,

$$V_m(t) = V_m \cos \omega_m t \quad \text{--- (1)}$$

Carrier signal

$$V_c(t) = V_c \cos \omega_c t \quad \text{--- (2)}$$

After Modn, peak amplitude of modulated wave is expressed as,

$$V_{AM}(t) = V_c + V_m(t) \quad \text{--- (3)}$$

Subst (1) in (3)

$$V_{AM} = V_c + V_m \cos \omega_m t$$

$$\Rightarrow V_c \left( 1 + \frac{V_m}{V_c} \cos \omega_m t \right)$$

$$V_{AM} = V_c \left( 1 + m_a \cos \omega_m t \right) \quad \text{--- (4)}$$



# AM FREQUENCY SPECTRUM

where  $m_a = \text{Modulation Index} = \frac{V_m}{V_c}$  (2)

Hence AM wave is given by

$$V_{AM}(t) = V_{AM} \cos \omega_c t \quad (5)$$

Subst (4) in (5)

$$V_{AM}(t) = V_c (1 + m_a \cos \omega_m t) \cos \omega_c t \quad (6)$$

AM Freq Spectrum and Bandwidth:

Although the modulation <sup>carrier</sup> & signal contains two frequencies  $f_c$  &  $f_m$ . The modulation process generates two new frequencies that are the sum & differences of  $f_c$  and  $f_m$ .

The spectrum is found by expand (6)

$$V_{AM}(t) = V_c (1 + m_a \cos \omega_m t) \cos \omega_c t$$

$$\Rightarrow V_c \cos \omega_c t + m_a V_c \cos \omega_m t \cos \omega_c t$$

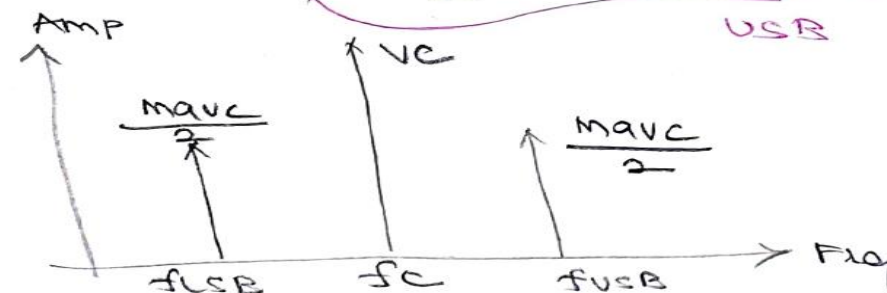
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$$\cos \omega_m t \cos \omega_c t = \frac{\cos (\omega_c - \omega_m) t + \cos (\omega_c + \omega_m) t}{2}$$

$$V_{AM}(t) = V_c \cos \omega_c t + \frac{m_a V_c}{2} [\cos (\omega_c - \omega_m) t + \cos (\omega_c + \omega_m) t]$$

$$V_{AM}(t) = \underbrace{V_c \cos \omega_c t}_{\text{Carrier}} + \frac{m_a V_c}{2} \underbrace{\cos (\omega_c - \omega_m) t}_{\text{LSB}} +$$

$$\frac{m_a V_c}{2} \underbrace{\cos (\omega_c + \omega_m) t}_{\text{USB}}$$



$$f_{LSB} = (f_c - f_m)$$

$$f_{USB} = (f_c + f_m)$$



# AM BANDWIDTH

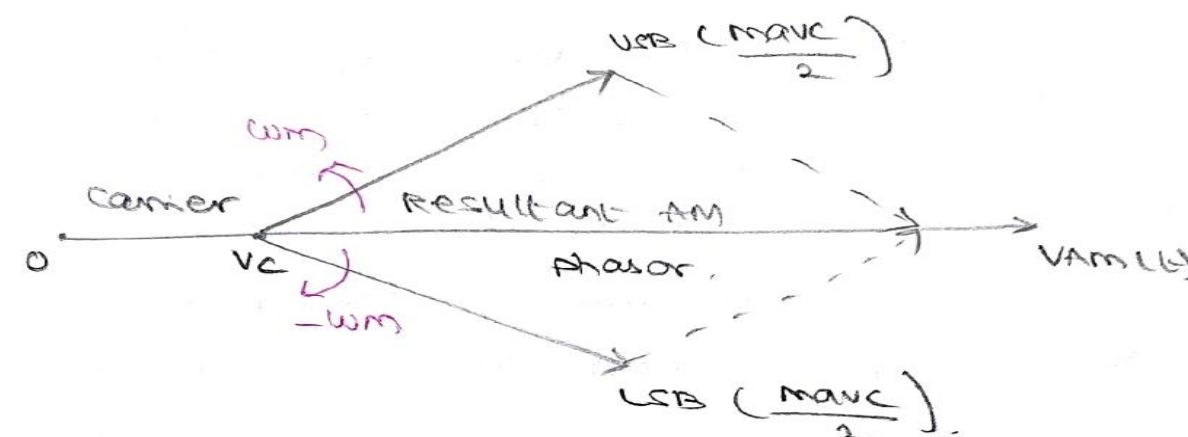
Bandwidth of AM:

$$B = f_{UCB} - f_{LCB}$$

$$\Rightarrow f_c + f_m - (f_c - f_m) = 2f_m$$

$$B = 2f_m \text{ Hz}$$

Phasor representation of AM wave with carrier:



Phasor of the USB rotates in anticlockwise direction at an angular frequency of  $\omega_m$  and phasor for the LSB rotates in clockwise direction at the angular frequency  $-\omega_m$ .

Modulation Index & % Modulation:

$$m_a = \frac{V_m}{V_c} \quad \% m_a = \frac{V_m}{V_c} \times 100$$

Calculation of  $m_a$  from AM waveform:

$$V_m = \frac{V_{max} - V_{min}}{2} \quad , \quad V_c = \frac{V_{max} + V_{min}}{2}$$

$$m_a = \frac{\left( \frac{V_{max} - V_{min}}{2} \right)}{\left( \frac{V_{max} + V_{min}}{2} \right)} \Rightarrow \frac{V_{max} - V_{min}}{V_{max} + V_{min}}$$



# AMPLITUDE MODULATION

(3)

Degree of Modulation:

- \* Under Modulation,  $m_a < 1$ , when  $V_m < V_c$
- \* Over Modulation  $m_a > 1$ , when  $V_m > V_c$
- \* Critical Modulation  $m_a = 1$ , when  $V_m = V_c$ .

AM Power Relation;

$$P_t = \text{Carrier Power} + \text{Power in LSB} + \text{Power in USB}$$

$$\Rightarrow P_{\text{carr}} + P_{\text{LSB}} + P_{\text{USB}}$$

$$\Rightarrow \frac{V^2_{\text{carr}}}{R} + \frac{V^2_{\text{LSB}}}{R} + \frac{V^2_{\text{USB}}}{R}$$

$$P = I^2 R$$

$$P = \frac{V^2}{R}$$

(i) Carrier Power;

$$P_c = \frac{V^2_{\text{carr}}}{R}$$

$$\Rightarrow \frac{(0.707 V_c)^2}{R}$$

$$\Rightarrow \frac{\left(\frac{V_c}{\sqrt{2}}\right)^2}{R} \Rightarrow \frac{V_c^2}{2R}$$

$$V_{\text{carr}} = 0.707 V_c$$

$$P_c = \frac{V_c^2}{2R}$$

(ii) Power in Side Bands;

$$P_{\text{LSB}} = P_{\text{USB}} = \frac{(0.707 V_{\text{SB}})^2}{R}$$

where  $V_{\text{SB}}$  is the peak volt of USB and LSB.

$$V_{\text{SB}} = \frac{m_a V_c}{2}$$

$$P_{\text{LSB}} = P_{\text{USB}} = \frac{\left(0.707 \frac{m_a V_c}{2}\right)^2}{R}$$

$$\Rightarrow \frac{\left(\frac{1}{\sqrt{2}} \cdot \frac{m_a V_c}{2}\right)^2}{R} \Rightarrow \frac{m_a^2 V_c^2}{8R} = \frac{m_a^2}{4} P_c$$

$$P_{\text{LSB}} = P_{\text{USB}} = \frac{m_a^2}{4} P_c$$



# AM-TRANSMISSION EFFICIENCY



$$P_T = P_C + P_{LSB} + P_{USB}$$
$$\Rightarrow \frac{V_c^2}{2R} + \frac{m^2 V_c^2}{8R} + \frac{m^2 V_c^2}{8R}$$
$$\Rightarrow \frac{V_c^2}{2R} \left( 1 + \frac{m^2}{4} + \frac{m^2}{4} \right)$$
$$P_T = \frac{V_c^2}{2R} \left( 1 + \frac{m^2}{2} \right) \Rightarrow P \left( 1 + \frac{m^2}{2} \right)$$

Transmission Efficiency;

$$\eta = \frac{\text{Power in SB}}{P_T}$$

$$\Rightarrow \left( \frac{m^2 V_c^2}{8R} + \frac{m^2 V_c^2}{8R} \right)$$

$$\frac{V_c^2}{2R} \left\{ \frac{m^2}{4} + \frac{m^2}{4} \right\}$$

$$\Rightarrow \frac{\cancel{V_c^2}}{\cancel{2R}} \left( \frac{m^2}{4} + \frac{m^2}{4} \right) \Rightarrow \frac{\left( \frac{m^2}{2} \right)}{\left( \frac{2 + m^2}{2} \right)}$$

$$\eta \Rightarrow \frac{m^2}{2 + m^2} \Rightarrow \% \eta = \frac{m^2}{2 + m^2} \times 100$$

If  $m = 1$ , then 100%. Modulation takes 33.33%,

$$\% \eta = \frac{1}{2+1} \times 100 = \frac{1}{3} \times 100 = 33.33\%$$

Hence only 33.33% of energy is used & remaining power is wasted by the carrier signal along with sidebands.



# ADVANTAGES AND DISADVANTAGES OF AM

## Advantages ;

- \* Simple Modulator & demodulators
- \* Low cost
- \* AM can travel a long dist
- \* It covers larger than FM.

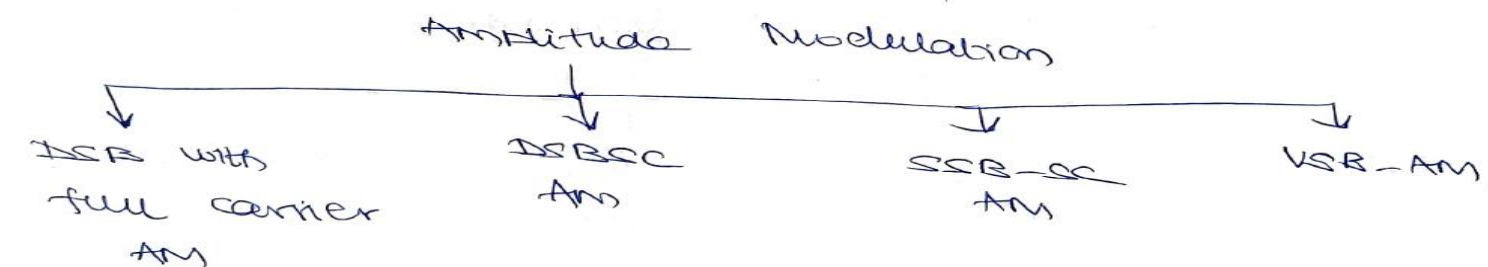
## DIS ADV ;

- \* power waste take place
- \* poor performance if noise more

## Application ;

- Radio broadcasting
- Picture transmission in TV system.

## \* Classification of AM :



## Double Side Band Suppressed carrier :

- \* In this the transmitted wave consists of only upper and lower sideband.
- \* Total power is saved, here through the suppression of the carrier wave.

$$\text{Tx in BW} \rightarrow 2f_m$$

## Expression for DSB-SC

Modulation signal

$$v_m(t) = v_m \cos \omega_m t \quad \text{--- (1)}$$





**THANK YOU**