



SNS COLLEGE OF TECHNOLOGY

Coimbatore-36.

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COURSE NAME : 19CSB301&Automata Theory and Compiler Design

III YEAR/ V SEMESTER

UNIT –III SYNTAX ANALYSIS AND SEMANTIC ANALYSIS

Topic: Bottom Up Parser_LR Parser

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Bottom up parsing (Right most Derivations)

- * Terminals \rightarrow Non-Terminals
leaf node \rightarrow Root Node (Start Symbol)

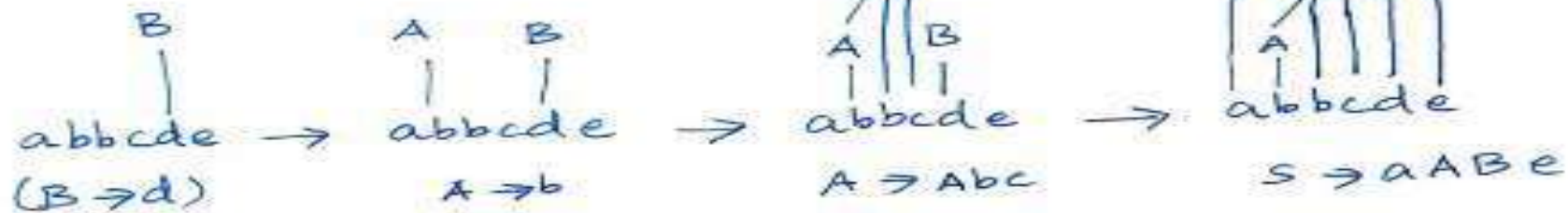
* Example 1:

$S \rightarrow aABe$

$A \rightarrow Abc | b$

$B \rightarrow d$

Input : abcde



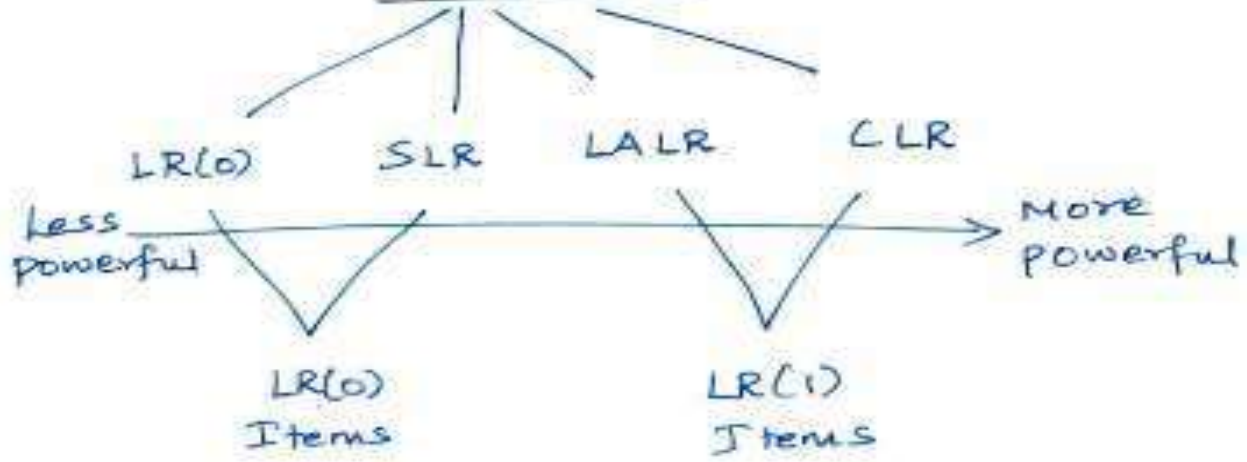


* Types of Bottom up parsing

Non-Recursive Shift Reduce parser

Operator precedence parser

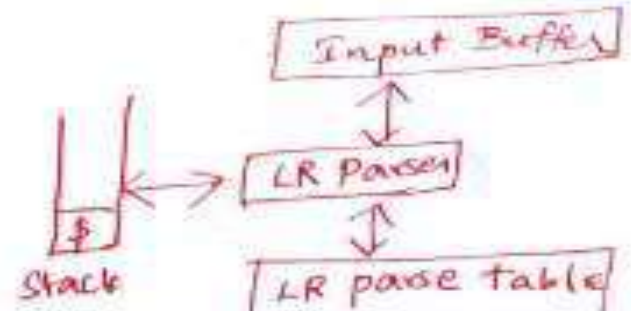
LR Parser



- SLR - Simple LR
- LALR - Lookahead LR
- CLR - Canonical LR

LR(k)

- Left to Right processing i/e
- Right most Derivations
- k (lookahead)





SHIFT REDUCE PARSING

Shift-reduce parsing is a type of bottom-up parsing that attempts to construct a parse tree for an input string beginning at the leaves (the bottom) and working up towards the root (the top).

Example:

Consider the grammar:

- $S \rightarrow aABe$
- $A \rightarrow Abc \mid b$
- $B \rightarrow d$

The sentence to be recognized is `abbcede`.

REDUCTION (LEFTMOST)

- `abbcede` ($A \rightarrow b$)
- `aAbcde` ($A \rightarrow Abc$)
- `aAde` ($B \rightarrow d$)
- `aABe` ($S \rightarrow aABe$)
- `S`

RIGHTMOST DERIVATION

- $S \rightarrow aABe$
- $\rightarrow aAde$
- $\rightarrow aAbcde$
- $\rightarrow abbcede$

The reductions trace out the right-most derivation in reverse.



Handles



Handles:

A handle of a string is a substring that matches the right side of a production, and whose reduction to the non-terminal on the left side of the production represents one step along the reverse of a rightmost derivation.

Example:

Consider the grammar:

$E \rightarrow E+E$

$E \rightarrow E * E$

$E \rightarrow (E)$

$E \rightarrow id$

$E \rightarrow \underline{E+E}$

$\rightarrow E+\underline{E * E}$

$\rightarrow E+E*\underline{id_3}$

$\rightarrow E+\underline{id_2} * id_3$

$\rightarrow \underline{id_1} + id_2 * id_3$

In the above derivation the underlined substrings are called **handles**.

Handle pruning:

A rightmost derivation in reverse can be obtained by “**handle pruning**”.

(i.e.) if w is a sentence or string of the grammar at hand, then $w = \gamma_n$, where γ_n is the n^{th} right-sentinel form of some rightmost derivation.



Stack Implementation of Shift Reduce Parsing



Stack	Input	Action
\$	$id_1 + id_2 * id_3 \$$	shift
\$ id_1	$+ id_2 * id_3 \$$	reduce by $E \rightarrow id$
\$ E	$+ id_2 * id_3 \$$	shift
\$ $E +$	$id_2 * id_3 \$$	shift
\$ $E + id_2$	$* id_3 \$$	reduce by $E \rightarrow id$
\$ $E + E$	$* id_3 \$$	shift
\$ $E + E *$	$id_3 \$$	shift
\$ $E + E * id_3$	$\$$	reduce by $E \rightarrow id$
\$ $E + E * E$	$\$$	reduce by $E \rightarrow E * E$
\$ $E + E$	$\$$	reduce by $E \rightarrow E + E$
\$ E	$\$$	accept

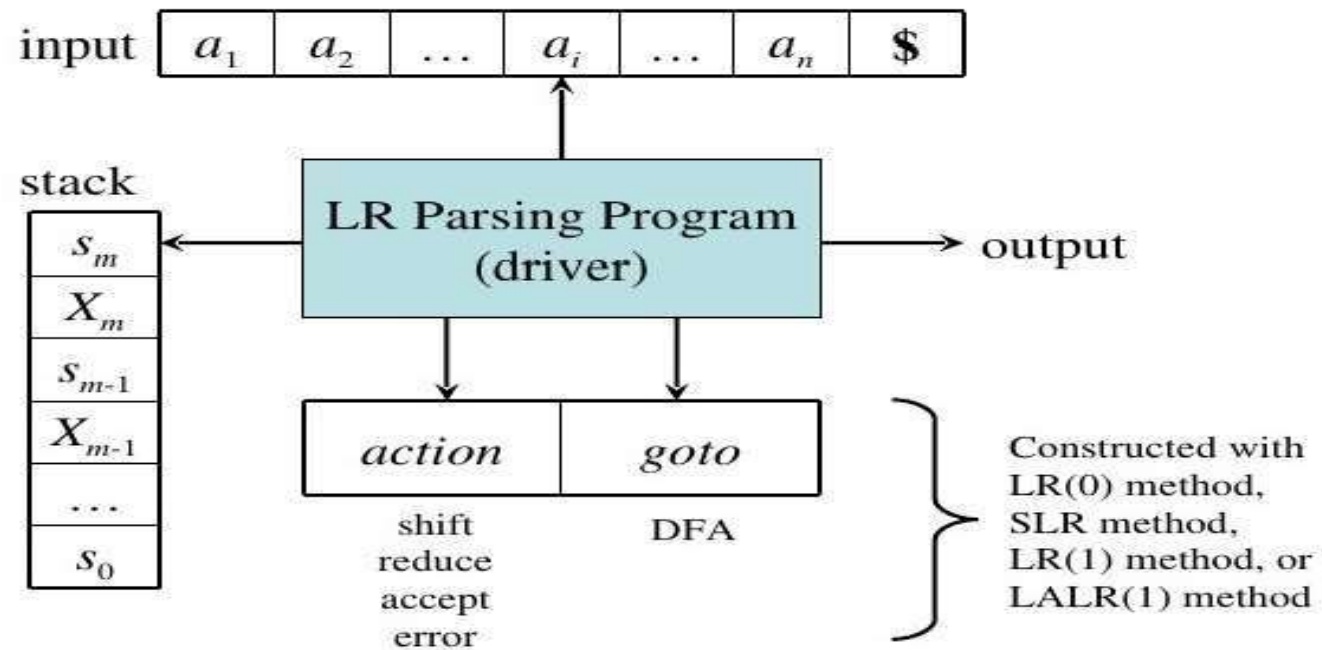
Actions in shift-reduce parser:

- **shift** – The next input symbol is shifted onto the top of the stack.
- **reduce** – The parser replaces the handle within a stack with a non-terminal.
- **accept** – The parser announces successful completion of parsing.
- **error** – The parser discovers that a syntax error has occurred and calls an error recovery routine.



LR Parsing Method

Model of an LR Parser





LR Parsing Algorithm

Input: An input string w and an LR parsing table with functions *action* and *goto* for grammar G .

Output: If w is in $L(G)$, a bottom-up-parse for w ; otherwise, an error indication.

Method: Initially, the parser has s_0 on its stack, where s_0 is the initial state, and $w\$$ in the input buffer. The parser then executes the following program :

```
set ip to point to the first input symbol of  $w\$$ ;  
repeat forever begin  
  let  $s$  be the state on top of the stack and  
   $a$  the symbol pointed to by ip;  
  if  $action[s, a] = \text{shift } s'$  then begin  
    push  $a$  then  $s'$  on top of the stack;  
    advance ip to the next input symbol  
  end  
  else if  $action[s, a] = \text{reduce } A \rightarrow \beta$  then begin  
    pop  $2 * |\beta|$  symbols off the stack;  
    let  $s'$  be the state now on top of the stack;  
    push  $A$  then  $goto[s', A]$  on top of the stack;  
    output the production  $A \rightarrow \beta$   
  end  
  else if  $action[s, a] = \text{accept}$  then  
    return  
  else  $error()$   
end
```




LR(0) parser

Q. $S \rightarrow AA$
 $A \rightarrow aA | b$

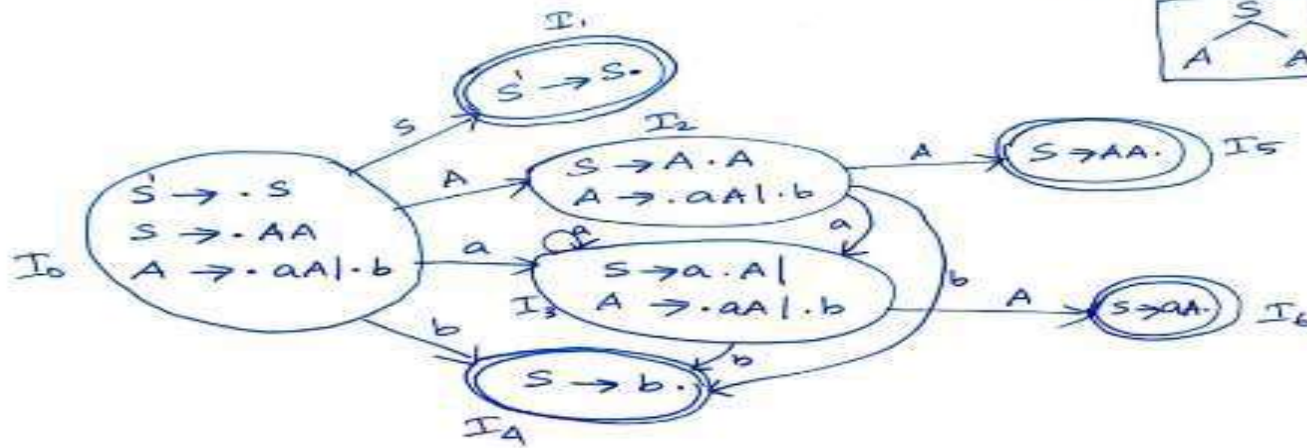
Step 1: Augmented Grammar

$S' \rightarrow S$
 $S \rightarrow AA$
 $A \rightarrow aA | b$

Step 2: Canonical LR(0) items

LR(0) items \rightarrow productions \rightarrow

$S \rightarrow \underline{\cdot}AA$ (yet to read)
 $S \rightarrow A \cdot A$ (want to read A)
 $S \rightarrow AA \cdot$ (completing read).



No. The production

1 $S \rightarrow AA$
2 $A \rightarrow aA$
3 $A \rightarrow b$



step 3: parse Table

	Goto (Non-Termi)		Action (Terminals)		
	A	S	a	b	\$
I ₀	2	1	S ₃	S ₄	
I ₁					Accept
I ₂	5		S ₃	S ₄	
I ₃	6		S ₃	S ₄	
I ₄			r ₃	r ₃	r ₃
I ₅			r ₁	r ₁	r ₁
I ₆			r ₂	r ₂	r ₂

state \xrightarrow{T} Shift
state $\xrightarrow{N-T}$ Goto
Final state \rightarrow Red



STACK	INPUT	ACTION
\$0	<u>a</u> abb\$	
\$0a <u>3</u>	<u>a</u> bb\$	Shift a3
\$0a3a <u>3</u>	<u>b</u> b\$	Shift a3
\$0a3a3 <u>b</u> 4	<u>b</u> \$	Shift b4
\$0a3 a3A6	<u>b</u> \$	Reduce (R ₃) 3 rd production (3A → b)
\$0 a3A6	<u>b</u> \$	Reduce (R ₂) 2. A → aA
\$0 <u>A</u> 2	<u>b</u> \$	Reduce (R ₂)
\$0A2 b4	<u>\$</u>	Shift b4
\$0A2 A5	<u>\$</u>	Reduce (R ₃) (3. A → b)
\$0 <u>S</u> 1	<u>\$</u>	Reduce (R ₁) (1. S → AA)
		Accept .

