

It is a past of a sentence that certains



A declarative sentinue contains surject and prieolicate. that does what the Subject does on a processes

Predecate

A part of a declarative sentence describing the properties of an object (on) relation among object is called a prodicate.

I. Tigos is an wild animal. It is denoted by P(s).

al sam is poor and Ram is intelligent

It is denoted by P(S) 1 I(8)

Quantages:

Quantifier is the one which is used to quantify the nature of vaccables.

Types of quantifier: J. Orfiversal quantifies (tx) or (x)

The quantifier "for all x is called ungversal quantifies.

Eg: I for all x, or Is an Integer In symbolic forms +xx, I(x)

2). Every apple is sed.

For all x, 96 x 18 an apple then x 18 sed. $(4x) \left[A(x) \rightarrow R(x) \right]$





J. Exestentfal quantifier: (Jx) The quantiffer "for some x" is called the exactential quantifier. Eg: some men acce Intelligent There exist an or such that x is a man and a is intelligent. (FX) (M(X) / I(X))

Bound and frice variables: The variable is said to be bound 98 It is concerned with either wilversal (+20) 001 existential (Jx) quantition.

Otherwase It is called bree variable. Supe of the grant of the Supe of the quantifier is the torimula torrowing the quantifier (x) P(x, y) > x & bound variable y is brice vocable prx, y) 98 the Scope of the quantifoot.

Theory of Inference for Predecate earculus

J. Urriversal Specification [US Rule]

 $(\forall x) P(x) \Rightarrow P(y)$

al. Universal General Tratton [UG Rule]

 $P(y) \Rightarrow (\forall x) P(x)$

Existential specification [ES Rule]

 $(Jx) P(x) \Rightarrow P(y)$

H. Existential General Proation [EGI Rule]

 $P(y) \Rightarrow (\exists x) P(x)$

gu x, & x x an apple Scanned with CamScanner





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1. Show that (Jx) M(x) follows loggically
            (x) [H(x) \rightarrow M(x)], (\exists x) H(x)
                   Step premises Rule
                 1. (20 [H(2)→m(20)] P
\begin{cases} \frac{1}{3} & \frac{2}{3} & \frac{1}{3} & \frac{
                                                                                                                                     US
                                                                                                      E61
                6. (FOU M(O1)
         2. All humans are mortal. Sachen 33 a human
            Therefore he is mostal.
                                    H(21): 2 96 a human
                                    M(x): x is Mortal
            H(6) : Sachen B a human
                   The premeses wie.
                               (+x) [H(x) -> M(x)], H(5)
                     conduston: M(5)
                        Step premises Rule
                          1. (+x)[H(x) -> M(x)] P
                                      H(5) -> M(5)
                                                                M(S)
        92,3)4.
         3. Show that the premises, "one student in this
                  class knows how to write programs 9n JAVA "a
              "Everyone who knows how to weste program an
                  JAVA can get a bigh-paying 306" amply the
                  conclusion "some one on this class can get a
                                                                                                        High - paying deb .
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Let A(x): x 1/3 90 +159s closs
         J(21): X Knows how to weste program 9n JAVA
         H(x): ze can get a high payling Job.
    The premises are,
      (fx) (A(x) ハJ(xx)), (ヤx) (弱)→ H(x))
    Copolu Scon: Fx (A(21) A H(21))
                              Rule
    Step premisos
       (P) (K) (K) (K) (K) (K) (K) (K) (K)
       Ala) V 2(A)
                              T AIY) AT(Y) => A(Y)
927 3. A(y)
              J(4)
    S. (₹a) (J(x)→H(a))
 ₹53 6. J(y) → H(y) US
              HIY)
{3,T3 8.
            ( BIH VCEIT
         (Ja) (Although)
                              EG
 4]. Veryly the valldaty of the following argument.
  "Every Aving thing is a plant or an animal"
 "John's gold flat is also and & is not a plant"
 "All ansmals have hearts". Therefore, " John's
  gold best has a heart".
     L(x1): x & a larging thing L(j): js allre
                                PG): jis not a
   P(x): x % a plant
A(21): 2 % an animal

H(21): 2 % a heart H(j): j has a heart howell
  GIVN: (+x) [L(x) + P(91) V A(x)]
         LG) ATPG), (4x) [A(x) >H(x)]
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conclusion: H(j)	
Step Priemises	Rule
1. (Yx) [L(x) > P(x) VA	(z) P
$\{i\} \stackrel{?}{\sim} L(j) \rightarrow p(j) \vee A(j)$	US
3. L(j) n 7P(j)	P
(3)4· L(j)	T PAR > P
(2,4) 5 P(j) V A(j)	T P, P>Q >Q
664 6. TP(j) -> A(j)	T FAX 7PVQ
7. (+x1)[A(x1) -> H(x)]	P. Dong and Company
(1) > H(j)	5G 5 FR 12 F
9. TP(j) > H(j)	T PNO => P, Q
533 10. 7 P(j)	T P, P-> 0
п. нд)	enageri et a
A-7 (- B-7)	THE ALLEY SECTION
	. , mussc", "8ame
5]. "All lock morege 35	loud music, loud music
and must	
exist"	ac must c
R(x) : x 13 cl cl L(x) : x 9s a low	ad music
G ₁ yn.	(150) R(x)
GIVM: (XX) [R(X) -> L(X)] >	The same of the sa
1 A DOLL SCOP : (FX) L(X)	good too the
1. (\(\frac{1}{2}\)) (\(\R(\x))^{-}	> L(x)) P
{1) 2. R(4) → L	(y) Production
3. (Fx) R(x)	ES
(33) 4. R(4) {2,43} 5. L(4)	7
6. (Fx) L(x)	EG





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6] Establish the validaty of argument.
    1). All integers are eathernal not
    ii) some antogers are power of three.
   111) Therefore some sational numbers are
       Power of 3.
    I(x): of 98 an 90toges
    R(x): 2 % an eathoral number
    P(x): or 98 power of 3.
    Byun (+x) (I(x) -> R(x)), (7x) (I(x) AP(x))
   conclusion: (Fx) [R(x) 1 P(x)]
                                  Pule
     Stop
               Premasos
                              P
          (\forall x) \left[ I(x) \rightarrow R(x) \right]
     - 1,-
  713 2.
              T(y) \rightarrow R(y)
         (FX) [I(X) A P(X)]
  8394.
                                  ES
              I(9) 1 P(9)
                                  + PAQ > PER
                I(A)
                R(9)
                P(y)
943 7
76,77 8.
            R(4) 1 P(4)
                                EG
         (Fx) [R/x) AP/x)]
J. Show that (x) [P(x) VQ(x)]
  by anderect people
   Premares: (x) [P(x) VQ(x)]
   Conclusion: (2) P(x) V(7x) Q(x)
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Stop	PROMPERS (A) [P(X) V Q(X)]	Rule P
1. 13 2. 3.	Pry) v (Jx) & (m)	Nogation of wordursion
§33 4.	$(\exists x)$ $\exists x)$ $\exists x)$ $\exists x)$	T T(PAG) T PAG > P
449 5- 453 6.	(7x) P(x)	E3 T PARD
7. 273 8.	(x) TR(x) TR(y)	US T P,6 => PnQ T 7Pn7Q <>> 7(PV)
36,83 9. 393 10.	TP(4) / TQ(4)) T(P(4) / Q(4))	P.Q => PAQ
(9,103 11. (113 12.	F	m manleration
8J. US9.	ng cp sule, oftals the one of the	(X) EKINO
Ctop	Premises ($\forall x$) [$P(x) \rightarrow Q(x)$] ($\forall x$) [$P(x) \rightarrow Q(x)$]	P P US
5233 4	R(y) > 7Q(y) R(y) TQ(y)	plassumed) TP,P+A+A
{3,43 5. {13 6. 55,63 T	P(y) -> Q(y)	US T P+B, 7B → 7P



