



(An Autonomous Institution)

Coimbatore-641035
DEPARTMENT OF MATHEMATICS

UNIT 2- COMBINATORICS

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GRENEMATERS FUNCTIONS:
     The generating function for the sequence
es' wath torms as, an or lead numbers
Is the enterste sum.
   G1(x) = a0 + a, x + a2 x2 + ... + an xn+.
         = 3 an 20
Step 1: Rewellte the Me avoience con., with RHS=0
working Rule:
Step &: Multiply the eqn. obtained in step 1 by xn
    & summang from (0 to 00) 091 (1 to 00)
        09 (& 2000)
Step 3: Put G(x) = \sum_{n=0}^{\infty} a_n x^n and write G(x) = 0.00
        a function of a
 Step 4: De compose GICXI Porto poortfal braction.
 Step 5: Express an as the co-efficient of x"
        95 (51(20)
  (1-x)^{-1} = 1 + x + x^2 + x^3 + \dots
  (1+x)^{-1} = 1-x+x^2-x^3+...
  (1-x)^{-2} = 1+2x+3x^{2}+4x^{3}+\cdots
  (1+x)^{-2} = 1-2x+3x^2-4x^3+...
I. use the method of generating junction to
801 ve the sie awarence egn. an = 3 an -, +1, n >1
given an=1
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Giv.
$$q_{n} = 3q_{n-1} + 1$$

Let $G_{1}(x) = \sum_{h=0}^{\infty} a_{h} x^{h}$
 $\Rightarrow a_{n} - 3a_{n-1} - 1 = 0$

multiply by x^{h} is taking summation

 $x^{h} = x^{h} a_{n} - 3 x^{h} x^{h} a_{n-1} - \frac{3}{n-1} x^{h} = 0$
 $x^{h} = x^{h} a_{n} - 3 x^{h} x^{h} x^{h} x^{h} x^{h} = 0$
 $x^{h} = x^{h} a_{n} - 3 x^{h} x^{h} x^{h} x^{h} = 0$
 $x^{h} = x^{h} a_{n} - 3 x^{h} x^{h} x^{h} x^{h} = 0$
 $x^{h} = x^{h} x^{h} x^{h} + x^{h} x^{h} + x^{h$





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$$G(x) = -\frac{1}{2} [1+x+x^{2}+...] + \frac{3}{2} [1+3x+(3x)^{2}+...]$$

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$$\frac{2}{h=0} a_{n} x^{h} = -\frac{1}{2} \sum_{h=0}^{\infty} x^{h} + \frac{3}{2} \sum_{h=0}^{\infty} (3x)^{h}$$

$$= -\frac{1}{2} \sum_{h=0}^{\infty} (1)^{h} x^{h} + \frac{3}{2} \sum_{h=0}^{\infty} (3)^{h} x^{h}$$

$$\frac{1}{2} \log_{10} q_{\text{peneroffing}} \text{ functions, } 30 \text{ low that } 40 = 2^{h} \text{ gyn.}$$

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$$G(x) \left[\frac{1-3x+x^{2}}{x^{2}} \right] + \frac{3}{x} - \frac{x}{x^{2}} = \frac{1}{1-3x}$$

$$G(x) \left[\frac{(x-1)^{3}}{x^{2}} \right] = \frac{1}{1-3x} + \frac{3-3x}{x^{2}}$$

$$= \frac{x^{2} + (1-3x)(3-3x)}{x^{2}(1-3x)}$$

$$= \frac{x^{2} + 3x - 4x + 6x^{2}}{x^{2}(1-3x)}$$

$$G(x) = \frac{7x^{2} - 7x + 3}{x^{2}(1-3x)} \quad (2(-1)^{2})$$

$$G(x) = \frac{7x^{2} - 7x + 3}{x^{2}(1-3x)(x-1)^{2}}$$

$$\frac{7x^{2} - 7x + 3}{(1-3x)(x-1)^{2}} = \frac{A}{1-3x} + \frac{B}{x-1} + \frac{C}{(x-1)^{2}} \rightarrow (1)$$

$$= \frac{A(x-1)^{3} + B(1-3x)(x-1) + C(1-3x)}{(1-3x)(x-1)^{2}}$$

$$7x^{2} - 7x + 3 = A(x-1)^{3} + B(1-3x)(x-1) + C(1-3x)$$

$$x = 1, \quad 3 = C(1-3)$$

$$-C = 3 \Rightarrow C = -3$$

$$x = 0, \quad 3 = A - B + C \Rightarrow A - B = 4$$

$$x = \frac{7}{4} - \frac{7}{4} + 3 = \frac{A}{4} + 0 + 0$$

$$\frac{A}{4} = \frac{7-14+8}{4} = \frac{15-14}{4}$$

$$A = 1$$





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