



The Theory of Inference:

Argument : An argument is a sequence of statements. All statements except the tinal one are called plenfises (a assumption of hypothesis). The fixed statement is called conclusion. ie, Lot P, Pa, ..., Pn be a sequence of Statements that stield concluded a. It 93 denoted by  $(P_1 \land P_2 \land \dots \land P_h) \rightarrow Q$  is a tautology. Valid Argument: An argument is called valid if the conclusion is true when all premeses one true. Invalsd Argument: An argument is called privated of it is not valed augument. Rules of Inference: Rule P: A puemise may be introduced at any point in the devilvation Rule T: A formula S may be Introduced at any point in a decivation of S & tautologically implied by any one of more of the proceding formala's Rule Cp: If Swe can desurve & broom R and a set of premases, then we cap devare R-> & broom the set of premases alone. EL Show that RVS forlows Types of peool: i). Direct Proof (V) 20210000 11). Inderect Ploaf (a1) Ploof by contradiction 111). conditional ploof iv) In consestent proof





Direct Proof: when a conclusion is deserved from a set of premises by using accepted rules of reasoning then such a process of descevation is called direct ploof. If 1 got a good swill the The room which give men pace Implication Rules: () my more would a give me > > 1 didn's 301 & 9000 30002  $P, P \rightarrow a \Rightarrow a$ J. Modus Phones: P+Q, TA => TP 2] modus Tollens : 3]. Disfunctive Syllogism: TP, PVQ ⇒ Q 4]. Hypothetfcal Syllegism: P>Q, Q→R ⇒ P→Q (a) chain Rule 5. Samplification Rule:  $P, \alpha \Rightarrow PAQ$ PAQ > P,Q BazPVa 6]. Addetion Rule:  $P_{\Lambda 7Q} \Rightarrow 7(P \rightarrow Q)$ J. Equivalence Rule: I Show that R is valled from the premises  $P \rightarrow Q$ ,  $Q \rightarrow R$  and P. Rule Premises Step \$12 P→Q 62\$. Q->R  $P \rightarrow Q, Q \rightarrow R \Rightarrow P \rightarrow R$ {1,2} }. PYK 4. JP, P→Q →Q] 14,53 5. R 2]. Show that RVS follows logically from the premises CVD,  $(CVD) \rightarrow 74$ , TH -> (ATTB), and (ANTB) -> RVS : Loongs

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Piemises Rule Step P 1. CVD P TH (CVD) 2. T TH 71,833. P (ANTB) 74 > T 4. ANTB P <u>5</u>3, 43 6. RVS AA7B→ T 6. RVS 25,63 7 valed 98 a RA (PVQ) 3]. Show that PVQs conclusion from the premases JM. P-> M and Rule premases P Step TM 1. P P-> M 2. T TP 3. 31,23 pra 4. Q 5 Q > R 6. R 7 £5,63 T RA(PVQ) \$4,73 D AVC), D that AJ. Show B. B





Rule
Step Piemases p
1. $D \rightarrow (AVC)$ p
2. D
$f_{1,a_{3}}$ a. AVC $BT [P \rightarrow a \not \rightarrow TPVa]$
{3} 4. TA→C
P D D P P P
5. $A \rightarrow B$ $[4,53] 6.$ $7A \rightarrow B$ $T [P \rightarrow 0, A \rightarrow K \rightarrow T M$ $T [P \rightarrow 0 \Rightarrow 7B \rightarrow 7P]$ $T [P \rightarrow 0 \Rightarrow 7B \rightarrow 7P]$
$[6]$ 7. $TB \rightarrow A$ $P$ $P \rightarrow P$
$\begin{array}{cccc} \hline & & & \\ \hline \\ \hline$
Bezg 1877 ere P
Eq3 10. DVF T PVP T
11.
and IP from 218-5 2 79
Indexect Proof: TO, P-D, PVP => R
the paper plents the
and age the conclusion there of the
we get $\neg c \land (H_1 \land H_2 \land \dots \land H_m) \Rightarrow F, P \Rightarrow B \Rightarrow P$
where F is the contradiction.
J. Prove by Proderect method $70, P \rightarrow 0, PVR \Rightarrow R$
Process COO
Step TR. Negation of condusion
a. PVR P
50.) F
( , , , , , , , , , , , , , , , , , , ,
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a Show +	bat TPATQ⇒	- T(PAG) by
9 pdflec	t ploof.	
Step	Premices	Rule
1.	PAQ	Negation of conclusion
えら &.	Р	T PAQ => P
З.	TPATR	Р
ş33 4.	TP	T TPAR STP
fa,43 ち.	PVJb	T P,Q =>PAQ
253 6.	F	T
		s, $\delta \rightarrow TQ$ , $P \rightarrow Q \Rightarrow TP$
3. Show the	where $R \rightarrow 7a$ , $Rv = 1$	,, <b>O</b> , <b>O</b> ,
by mar		Rule
Step	Plemases	Negation of conclusion
1.	Р	
æ.	P>Q	P T P, P→A ⇒ Q
21,233.	æ	
4.	R->7Q	P T $P \rightarrow Q$ , $TQ \Rightarrow TP$
3,A3 5.	TR	
6.	RVS	P
\$5,6] T.	S	T TR, RVS => 5
8.	S->7R	P
§7,839	70	$T$ $P, P \rightarrow 0 \rightarrow 0$
\$2 92 10.	QATQ	$T$ $P, Q \Rightarrow PAQ$
11.	-	T PATP (=> F
	-70	P-78 (=) 78
Has	J Ste and	(2-5), (2-27) A (5-30),
N.	2). ((176) A 1 (176) A 1	P-78 (=)" 7P R-15), 12-77) ATS-10), P-78) =) 7P
	£ £ . 11	





100000	0		
Condet iona	Rioof:	i a a f	the
J. Show that	R→S can be	deciver (	).~~~ ₹
	$\rightarrow (Q \rightarrow S), 7$		
Set	plemages	PT ASSUM	ed premice) ep ison(24 linna)
	R.(ASSeuro	(A) Rule	€P (JEBEUT USDa)
Q.	TRVP	Р	
रा, २७ ३.	P	T	TP, PVQ=>Q
4.	P-> (Q->S)	P	
え,43 あ.	6-25	Т	$P, P \rightarrow Q \Rightarrow Q$
6. SE (7	Q	P	
{5,63 γ.	S	T	$P, P \rightarrow Q \Rightarrow Q$
21,73 8.	R->S	CP	
21. Decive th	se following	restpg C	Þ:
	$\Rightarrow P \rightarrow (P \land R)$	U U	
ii P P→	(R→(RAS)) =	×Q~S	
III) Pra	$\Rightarrow P \rightarrow (PAQ)$		· · · · · · · · · · · · · · · · · · ·
III). TPVQ,	TQVR, $R \rightarrow S \Rightarrow$	Pys	÷.
) P→q ⇒	$P \rightarrow (P \land R)$		1,60
Step	Reem9508	Rule	
	P	PLASSUN	nod premise)
2,7		Р	
ર્શ, શ્રે રુ.		T P	$P \rightarrow Q \Rightarrow Q$
利,33 年· ~ ~ ~	PAQ		A => PAR
5.	D-> (PAQ)	СР	





ii). P.  $P \rightarrow (Q \rightarrow (R \land S)) \Rightarrow Q \rightarrow S$ Rule premises Prassumed premise) Step R 1. P P 2. P-> (Q -> (RAS)) 3. P, P+Q >Q Q-> (RAS) 22,33A .  $P, P \rightarrow Q \rightarrow Q$ 51,435. RAS PAR => Q S T 553 6. Q->S CP 到,6月. P>Q > P> (PAQ) TPVQ, TQVR, R>S > P>S iii). Rule Premes 08 PLASsumed PlemPle) Step P 1. P TPVQ 2. 7PVQ \$ P>Q P->Q 529 3. P, P> a>Q T Q 21,33 8. P TOVR 5. 354 Q -> R 6. P, P>A>Q 7 R 74,63 7. 8. R-JS. T §7,899. 0Sa A,93. 10. P->S

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A &c to be 9hcons	istent of HINF	$H_{1}, H_{2}, \dots, H_{n}$ $H_{2} \wedge \dots \wedge H_{m} \Rightarrow F$ $\Lambda \gamma A,  \text{where}  A$	
J. Plove that		\$ P→Q, Q-7R	
Step	PLEMILOS	Rule	
1.	$P \rightarrow Q$	P	Ere
ي. تر ترج ا	$\begin{array}{c} \mathcal{Q} \rightarrow \mathcal{R} \\ \mathcal{P} \rightarrow \mathcal{R} \end{array}$	T P2Q, G	$\rightarrow R \Rightarrow P \Rightarrow$
4. {4} 5.	S-77R R-77S	P T P+a<	=> 78->7P
23,536.	P->7S	T P>Q, E	$q \rightarrow R \Rightarrow r \Rightarrow r \Rightarrow r$
7. 263 8.	R→S TPV7S	P ⊤ P→Q ≮	> TPVQ
283 9.	T (PAS)	T TPVTA	\$ TIPAE
10. {9,10y 11.	PAS (PAS) AT (PAS)	P T P,Q⇒	PAQ
12.	F	T	. T. (d. f.
2]. Show that	the premaces	$p \rightarrow q, P \rightarrow \gamma$	, 9->7×,
p aue	P	P	
a.	P->9	Р	
٤٦, ٢٦ ٤.	9		$a \Rightarrow a$
{3, A] 5.	9.778 78	P T P, P->1	a⇒a
6. ₹63 Т.	P->~ tr>TP	P T P→Q×	⇒ 7Q →7P

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35,73 B. T  $P, P \Rightarrow Q$ TP JI, BJ 9. PATP T P, R ⇒ PAR PATP & F T F 10. 3] prove that the premares a-> (b-> c), d > (bATC), and are for constituent. P 1. and T PAQ => PAQ a ziz 2. 3. a + (b + c) P T  $P, P \rightarrow Q \Rightarrow P \rightarrow Q$ ぎみ33 4. b→C T 213 5. d 6. d > (bATC) P T  $P, P \rightarrow Q \rightarrow Q$ 25,63 T. BATC T 7(P+Q) \$ PA7Q えて了 8. 7(b→c) 54,83 9. (b→c)AT(b→c) T P, Q → PAQ T AJ. Show that the followsing premices are anconsistent. F 1. It Jack masses many Jasses through fillness, then be fars high School. 2 If Jack fars high schools then he is uneducated. 3. If Jack reads a lot of books, then he IVI. TECHEGORE not uneducated. 4. Jack MARSOS many classes through 9112025 and reads a lot of books. P: Jack MPLSES many classes through gillness Q: Jack Jarls brigh School. R: Jack leads a lot of books S: Jack 98 uneducated.





The premises are

$P \rightarrow R, 6$	R>R, S=TR, PI	15.	
Act	Premases	Rule	
) &.	P>Q	Р	and the first
ર્શ, શ્રુ રૂ.	$R \rightarrow R$ $P \rightarrow R$		
4.	$S \rightarrow \tau R$	T	$P \rightarrow R, R \rightarrow R = P \rightarrow R$
243 5. 33,53 6.	R →7S	T	P>R <> 78-17P
263 T.	$P \rightarrow 7S$ $7P \vee 7S$	T	, c
夏73 8.	7 (PAS)	T	$P \rightarrow a \Leftrightarrow 7Pvq$ $7(P \land a) \Leftrightarrow 7Pv7q$
9. 28,93 10.	PAS (PAS) A T (PAS)	P	
$n_{\rm c}$	F		P, Q ⇒ PAQ PATP⇔F.
			FAIR VE.

- 5. 1). If there is a ball game, then to a verifying was difficult.
  - ii). If thely augred on time then
  - 11i). They awaved on time iv). Therefore there was no ball game. Show that the above statements are Valsd Statement.
  - Let p: There was a ball game
    - Q: Travelling was difficult
    - R: They arrived on time.
    - The premises are p-a, R -> TQ, R,
      - The conclussion is TP.





Step		Premases	Rule
١.	25		P
2.		$R \rightarrow 7Q$	P
FI, & J &.		78	$ au  P, P \rightarrow Q \Rightarrow Q$
4.		P>Q	P
夏3,4y を、		7P	$T$ , $P \rightarrow 0, 7 R \Rightarrow 7 P$