

(An Autonomous Institution) Coimbatore-641035.



UNIT 1– COMBINATORICS

5]. Solve
$$a_{n} - 7a_{n-1} + 10a_{n-2} = 0$$
, $n \ge 2$ with
 $a_{0} = 4$, $a_{1} = 17$
Give $a_{n} - 7a_{n-1} + 10a_{n-2} = 0$
characteoristic eqn: $m^{2} - 7m + 10 = 0$
 $(m-2)(m-5) = 0$
 $m = 2, 5$
HS $a_{n} = A(2)^{n} + B(5)^{n}$
Since RHS=0, $PS=0$.
The Soln. 95 $a_{n} = A(2)^{n} + B(5)^{n}$





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Coimbatore-641035.

UNIT 1– COMBINATORICS

$$GAVeD \ a_0 = 4$$

$$\Rightarrow a_0 = A(a_0)^0 + B(f_0)^0$$

$$A = A + B \Rightarrow (1)$$
and $a_1 = 17 \Rightarrow a_1 = A(a_0)^1 + B(f_0)^1$

$$17 = 2A + 5B \Rightarrow (2)$$
Solving (1) and (2), $A + B = 4$

$$aA + 5B = 17$$

$$(1) \times 2 + 2B = 3$$

$$(1) \Rightarrow A = 4 - 3$$

$$A = 1$$

$$\therefore a_n = 1(2)^n + 3(5)^n$$
Solve the recover on a relation

$$G(K) = -35(K-1) - 35(K-2) - 3((K-3)) \quad worth for
$$G(K) = -35(K-1) - 35(K-2) - 3((K-3)) \quad worth for
$$G(K) = -35(K-1) - 35(K-2) - 3((K-3)) \quad worth for
$$G(K) = -35(K-1) + 35(K-2) + 3((K-3)) = 0$$

$$G(K) = 3(K-1) + 35(K-2) + 3((K-3)) = 0$$

$$G(K) = -3(K-1) + 35(K-2) + 3((K-3)) = 0$$

$$G(K) = -3(K-1) + 35(K-2) + 3(K-3) = 0$$

$$M^2 = 1 + 2 + 10$$

$$M^2 = 0$$

$$M^2 = -1 - 2 + 1$$

$$A = -1, -1, -1$$

$$H_5 = (A + Bn + cn^R)(-1)^n \quad m = -1, \quad m^2 + ann + 1 = 0$$

$$G(K) = -2 (k_1, S(n)) = (A + Br + c)(-1)^1 = -2$$

$$A + Br + c = 2 - -1$$

$$A + 2B + 4c = -1 - -2 (3)$$$$$$$$







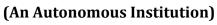
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Bolveng (1), (2) and (3),
Sub. A = 0 Ph (2) & (3),
B+c = 2 - + (4)
2B+4c = -1 - + (5)
(4) × 2 + 2B + 3c = 4
2c = -5
c = -5/2
(4)
$$\Rightarrow B = 2 - c = 2 - (-5/2)$$

 $B = 2 + \frac{5}{2}$
 $B = 2 + \frac{5}{2}$
 $B = \frac{9}{2}$
 $\therefore a_n = \left[\frac{9}{2}n - \frac{5}{2}n^2\right] (-1)^n$
3]. Solve the neconcence nelation $a_{n+2} = 4a_{0+1} - 4a_{0+1}$
 $n \ge 0, a_0 = 1, a_1 = 3$
Give the neconcence nelation $a_{n+2} = 4a_{0+1} - 4a_{0+1}$
 $n \ge 0, a_0 = 1, a_1 = 3$
Give $a_{n+2} - 4a_{n+1} + 4a_{n-2} = 0$
 $a_{n+2} - 2a_{n-1} + 4a_{n-2} = 0$
 $(m-2)^2 = 0$
 $m = 2, 2$
 $2dn = (A + Bn) 2^n$
Give $a_{0} = 1 \Rightarrow A = 1$
 $a_1 = 3 \Rightarrow (A + 2B) = 3$
 $2A + 2B = 3 \Rightarrow 2B = 3 - 2 = 1$
 $B = \frac{1}{2}$
 $\therefore a_n = (1 + \frac{1}{2}n) 2^n$







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H solve the neutrine is nelation for the
global of sequence 0,1,1,2,3,5,8,13,...
solp.:
If banaced sequence 0,1,1,2,3,5,8,13,...
satisfies the neutrine nelation
$$f_{n} = f_{n-1} + f_{n-2}$$

with $f_{0} = 0$, $f_{1} = 1$
 $a_{0} = f_{n} - f_{n-2} = 0$
Characteristic eqn: $m_{n}^{2} = m-1 = 0$
 $m = \frac{1 \pm \sqrt{5}}{2}$
Solve RH5=0 \Rightarrow P3=0
 \therefore The 30/2 Bs $f_{n} = A\left(\frac{1+\sqrt{5}}{2}\right)^{n} + B\left(\frac{1-\sqrt{5}}{2}\right)^{n}$
(A ven $f_{0}=0 \Rightarrow f_{0} = A\left(\frac{1+\sqrt{5}}{2}\right)^{n} + B\left(\frac{1-\sqrt{5}}{2}\right)^{n}$
 $add f_{1}=1 \Rightarrow f_{1} = A\left(\frac{1+\sqrt{5}}{2}\right)^{1} + B\left(\frac{1-\sqrt{5}}{2}\right)^{1} \Rightarrow$
 $A\left(\frac{1+\sqrt{5}}{2}\right) + B\left(\frac{1-\sqrt{5}}{2}\right)^{1} \Rightarrow$
 $A\left(\frac{1+\sqrt{5}}{\sqrt{5}}\right) + B\left(\frac{1+\sqrt{5}}{2}\right) + B\left(\frac{1+\sqrt{5}}{2}\right)^{1} \Rightarrow$
 $A\left(\frac{1+\sqrt{5}}{2}\right) + B\left(\frac{1+\sqrt{5}}{2}\right) + B\left(\frac{1+\sqrt{5}}{2}\right)^{1} \Rightarrow$
 $A\left(\frac{1+\sqrt{5}}{\sqrt{5}}\right) + B\left(\frac{1+\sqrt{5}}{2}\right) + B\left(\frac{1+\sqrt{5}}{2}\right) + B\left(\frac{1+\sqrt{5}$





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characterization eqn:

$$m^{3}-6m^{2}+11m-6=0$$

 $m=1, 2, 3$
25 for a RHS = $0 \Rightarrow PS = 0$
 $\therefore a_{n} = A(1)^{n} + B(2)^{n} + (3^{n} - 1), \quad m=1, \quad m^{3}-5m+6=0$
 $(m-2)(m-3)=0$
 $ext{ for } A = B + C = 2, \Rightarrow (1)$
 $a_{1} = 5$
 $B + 2B + 3C = 5 \Rightarrow (2)$
and $a_{2} = 15$
 $A + B + C = 15 \Rightarrow (3)$
Solving (1), (2) and (3),
(1) $\Rightarrow C = 2 - A - B \Rightarrow (4)$
Sub (4) in (2),
 $B + 2B + 3(2 - 0 - B) = 5$
 $P + 2B + 3(2 - 0 - B) = 5$
 $P + 2B + 3(2 - 0 - B) = 5$
 $P + 2B + 3(2 - 0 - B) = 15$
 $A + B + 9(2 - A - B) = 15$
 $A + 4B + 9(2 - A - B) = 15$
 $B + 4B + 12 - 9B - 9B = 15$
 $-2A - B = 5 - 6 = -1$
 $2A + B = 1 \Rightarrow (6)$
Sub (A) in (3),
 $A + 4B + 9(2 - A - B) = 15$
 $B + 4B + 12 - 9B - 9B = 15$
 $-2B - 5B = -3$
 $BA + 5B = 3 \Rightarrow (6)$
(b) $\Rightarrow BA + 5B = 5$
(b) $\Rightarrow BA + 5B = 5$
(c) $\Rightarrow A = 5A - 5B = 5$
(b) $\Rightarrow BA + 5B = 5$
 $(b) \Rightarrow BA + 5B = 5$
 $(c) BA + 5B = 5$





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UNIT 1– COMBINATORICS

Sub A =1 Pr (5),
A + B = 1
$$\Rightarrow$$
 B = -1
(1) \Rightarrow B + B + C = A
 $1 - 1 + c = A$
 $c = A$
 \therefore Solution is $a_n = 1(1)^n - 1(2)^n + 2(3)^n$
 $a_n = 1^n - 2^n + 2(3)^n$
(5) Solve the sie uncertaine states
 $a_n = 2a_{n-1} - 2a_{n-2} \Rightarrow n \ge R$ and $a_0 = 1$, $a_1 = 3$
Given
 $a_n - 2a_{n-1} + 8a_{n-2} = 0$
chouse the effective eqn.
 $m^2 - 2m + R = 0$
 $m = \frac{2 \pm \sqrt{H - H(1)(2)}}{2(n)} = \frac{2 \pm \sqrt{H - 9}}{2}$
 $= \frac{2 \pm 2i}{2}$
 $= 2 \pm \frac{1}{2}$
 $m = 1 \pm i$ $(\alpha \pm 1B)$
 \therefore Solution is $a_n = 3^n$ (A cos is $e + B$ Sin $n e$)
where $\pi = \sqrt{\alpha^2 + \beta^2}$ and $\theta = \tan^{-1}(P/\alpha)$
 $\pi = \sqrt{2}$
 $= \sqrt{2}$
 $A_n = (\sqrt{3})^n [A (\cos \frac{n\pi}{H} + B) \sin \frac{n\pi}{H}] \rightarrow (A)$
Given $a_0 = 1 \Rightarrow a_0 = A = 1$
and $a_1 = 2 \Rightarrow a_1 = (\sqrt{2}) [A \cos \frac{\pi}{H} + B \sin \frac{\pi}{H}] = 3$
 $A \sqrt{2} \times \frac{1}{\sqrt{2}} + \theta \sqrt{2} \times \frac{1}{\sqrt{2}} = 2$



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$$H + B = \mathcal{X}$$

$$B = \mathcal{X} - 1$$

$$B = 1$$

$$\therefore \text{ Solution 9S } a_n = (\sqrt{\mathcal{X}})^n \left(\log \frac{n\pi}{4} + 9 \sqrt{9n} \frac{n\pi}{4} \right)$$

$$Huo J. Solve the lecuvoience relation
$$\varphi(n) - 10\varphi(n-1) + 9 \varphi(n-2) = 0 \text{ with } \Im(0) = \Im, S(1) = 11$$$$