

SNS COLLEGE OF TECHNOLOGY (AN AUTONOMOUS INSTITUTION) COIMBATORE - 35 DEPARTMENT OF MATHEMATICS



Strong induction [Second prantiple of northematical In the form, we use the same bashe Step as before, but we use a different 9 nductore Step.

- i). Assume that P(j) is tout too j=12, ..., to
- ii) we have to prove that P(K+1) is true

well osdling proporty:

Every honempty set of non-negative integers: has a least element.

Pigeonhole psunciple

If (n+1) pigeon occupies in holes then atleast one hole has more than the phyeon Proof:

Assume that there are (1+1) pageons and n holes. To prove atleast one hole has more than one pigeon. we prove this by method of contradiction.

Suppose not, atleast one hole has not more than one pageon.

Form 1898 each and every hope has exactly one progeon. Strace those one in holes, which implies we have totally n phycons which is a contradiction to own

Hence atleast one hope has more than one pageon. assumption.

bioneralizzed progeonbole principle

If 'm' pigeon occupies in holes then atleast one hole has more than $\lceil \frac{m-1}{n} \rceil$ to progeons.

Hove [71] denotes the greatest entegen 1098 than 091 equal to 2, which is a Heal number.

(HM) (HM) =

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1. Show that among 100 people, atleast 12,06 them were both 9n the same month.

$$m = number 9$$
 propers = No. of people = 100

 $n = No$. of Holes = No. of month = 12

By acnoralized PHP,

$$\left[\frac{m-1}{n}\right] + 1$$

$$= \left[\frac{100-1}{12}\right] + 1 = 9$$
 were born 9n the same month.

a). Show that of an dectionarios on a laborary contain a total of 40,325 pages, then one of the electronceaes must have atleast 1614 pages.

No. of pageons: m = No. of pages = 40,325 No. of holos: n = No. of decisionariles = 25 By Generalized PHP.

y Generalized PHP3
$$\left[\frac{m-1}{n}\right]+1=\left[\frac{40,325-1}{25}\right]+1$$

$$=1614 \text{ Pages 9n the dictionastles}$$

I show that In a group of 6 people, at least 3 must be mutual follends (On) atleast 3 must be strangers.

I Show that Pf 7 word are used to paint 50 becycles, at least 8 becycles well be the same $m = N\Delta$ of blocks = 50 $p = N\Delta$ of colores = 7 colows.

= 8 braycles will be the Same colous.

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