

## SNS COLLEGE OF TECHNOLOGY (AN AUTONOMOUS INSTITUTION) COIMBATORE - 35 DEPARTMENT OF MATHEMATICS



Tautology: A statement formula which is true always surcespectave of the touth values of the anderedual variables is called a tautology. F9 : PNTP & a tautology.

A statement formula which is always false contra dection : is called a contradiction (on aboundety. E9:

PATP is a contriadiction.

## Cont goncy:

A statement formula which is neither tautology nor contractiction is called contigency.

E9: P +> a is contrigency.

q is a tautology. J. Show that [IP A (PAQ)] -

p	9	TP	PAQ	7PA(PAQ)	[7PA(PAQ)] → q
Т	T	F	Т	P 1417	S at .
Т	F	F	F	F BK	T
F	T	Т	FT	F	Т
F	F	T	F	F	T

Since all the entries In the resulting column is trues the given expression is a tautalogy.

RI. Show that (PAQ) A T (PVQ) B a contradiction.

Т	Т	Т	T	(t <b>F</b> air)	- CALP	
T	F	F	Т	F	F	
F	Т	F	Т	F	F	
F	F	F	F	Т	F uHgng colu contrad	

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ELLING

3. Identify the given exepted from

7	[PV(	a) V	(TPV	7Q)	TIPVI				
Р	a	TP	70	PVQ	7 (PVA)	TPVTA	V(TPVTQ)		
T	T	F	F	T	F	F	F		
Т	F	F	T	Т	F	T	T		
F	Т	T	F	T	F	T			
F	F	T	Т	F	Т	T			

Since the entires in the resulting column are T as well as F, the given expression is a contrigency.

Examine whether [(PVQ) ===] +> [Ar - ~(PVQ)]

Eque valence:

Two statement formulas p and g are equivalent if  $p \leftrightarrow g$  is a tautology. It is denoted by  $p \Leftrightarrow g$ . Show that the proposetions are logically equivalence

tor the tollowfing. (i)  $P \rightarrow Q \Leftrightarrow TPVQ$ (ii)  $P \rightarrow (QVR) \Leftrightarrow (P \rightarrow Q) \vee (P \rightarrow R)$ 

p	a	⇒ 7PV P→a	JP	TPVa	P→Q ⇔ 7PVQ
Т	T	т	F	Т	TT
T	F	F	F	F	Т
F	T	Т	T	T	T
F	F	T	T	TIN	In that T (PAG)

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(ii P	Q	P→ R	QVR	$\Rightarrow (P \rightarrow P \rightarrow (Q \lor R)$	P→Q	P→R	$(P \rightarrow Q)$ $(P \rightarrow R)$	$P \rightarrow (QVR)$ $\Leftrightarrow \Leftrightarrow$ $(P \rightarrow Q)V(P \rightarrow R)$	
T	T	T	Т	Т	Т	Т	Т	T	
/	Т	F	T	T	Τ.	F	Т	T	
· T	F	T	Т	T	F	T	Т	T	
F	Т	T	T	Τ	Т	Т	Т	T	
, T	F	F	F	F	F	F	F	T	
F	F	Τ	T	Т	T	T	Т	T	
F	Т	F	T	Т	T	T	Т	T .	
F	F		F	T	Т	Т	T	and Transford	3

Int ( uving ) HOLE bautology.

Hence  $P \rightarrow (R \vee R) \Leftrightarrow (P \rightarrow R) \vee (P \rightarrow R).$ S (BIAL) TT COM SITTEMA

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