

Normal reaction $N_R = W \cos \alpha$

Frictional force $F = \mu N_R$
 $= \mu W \cos \alpha$

When $\mu W \cos \alpha > W \sin \alpha$ → Block is at rest
 $\mu W \cos \alpha < W \sin \alpha$, the impending downwards motion takes place.

When the angle of plane with horizontal α , is increased, $W \sin \alpha$ will be more than $\mu W \cos \alpha$ and sliding takes place.

⇒ "The angle of the inclined plane, at which the body tends to slide down, known as angle of repose. denoted by α_m ."

$$\mu W \cos \alpha_m \leq W \sin \alpha_m$$

$$\mu W \cos \alpha_m = W \sin \alpha_m$$

$$\mu = \frac{W \sin \alpha_m}{W \cos \alpha_m}$$

$$= \tan \alpha_m \rightarrow \textcircled{1}$$

$$\mu = \tan \phi \rightarrow \textcircled{2}$$

ϕ ⇒ angle of static friction.





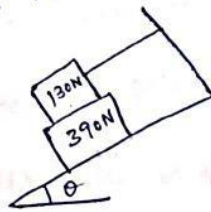
$\tan \alpha_m = \tan \phi$

$\alpha_m = \phi$

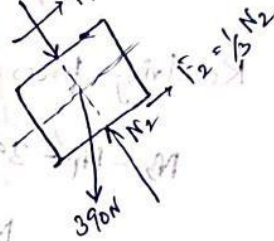
Angle of repose = angle of static friction.

Body on rough inclined plane

Q What should be the value of the angle θ so that motion of 390N block impends down the plane? The coefficient of friction $\mu = 1/3$.



FBD of upper block



FBD of lower block

FBD of upper block

T → tension of cable.

Resolving forces along plane

$T - 130 \sin \theta - F_1 = 0$

$T - 130 \sin \theta - \mu N_1 = 0$

$T - 130 \sin \theta + \frac{1}{3} N_1 \rightarrow \text{①}$

Resolving the force normal to plane

$N_1 = 120 \cos \theta \rightarrow \text{②}$

put ② in ①

$T = 130 \sin \theta + \frac{1}{3} (120 \cos \theta)$

$T = 130 \sin \theta + 43.33 \cos \theta \rightarrow \text{③}$