

SNS COLLEGE OF TECHNOLOGY

Coimbatore-35 An Autonomous Institution

Accredited by NBA – AICTE and Accredited by NAAC – UGC with 'A++' Grade Approved by AICTE, New Delhi & Affiliated to Anna University, Chennai

DEPARTMENT OF ELECTRONICS & COMMUNICATION ENGINEERING

19ECt302 – TRANSMISSION LINES AND antennas

III YEAR/ V SEMESTER

UNIT 2 – GUIDED WAVES

TOPIC 5 – TM WAVES IN RECTANGULAR WAVEGUIDES







CAN YOU RELATE THE FIGURES?





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TM WAVES IN RECTANGULAR WAVEGUIDES/19ECT302-TRANSMISSION LINES AND ANTENNAS/R.PRABHA/ECE/SNSCT





WAVEGUIDES

- A waveguide is a special form of transmission line consisting of a hollow, metal tube.
- The tube wall provides distributed inductance, while the empty space between the tube walls provide distributed capacitance.
- Waveguides are practical only for signals of extremely high frequency, where the wavelength approaches the cross-sectional dimensions of the waveguide.
- Below such frequencies, waveguides are useless as electrical transmission lines.





TYPES

Rectangular waveguides

Most preferred type

• Frequency difference between consecutive modes - smaller

Circular Waveguides

- Less Preferable
- Polarization not maintained – circular symmetry





RECTANGULAR WAVEGUIDE

- Consider a rectangular waveguide of width "a" and • breath "b".
- An EM wave is assumed to propagate in z direction • as shown in fig.



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Boundary condition

Ex=Ez=0 at y=0 and y=b

Ey=Ez=0 at x=0 and x=a



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• Basic equations from Maxwells curl equations

Maxwell's Equation

 $\nabla^2 \mathbf{E} + \omega^2 \mu \varepsilon \mathbf{E} = \mathbf{0}$

 $\nabla^2 \mathbf{H} + \omega^2 \mu \varepsilon \mathbf{H} = \mathbf{0}$

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From $\nabla \times \mathbf{E} = -\mu \frac{\partial \mathbf{H}}{\partial t}$, we have $\frac{\partial E_y}{\partial E_y} = -\mu \frac{\partial F_y}{\partial E_y}$ ∂E_z *∂z* dy ∂H ∂E_x ∂E_z ∂x $\frac{\partial E_y}{\partial x} - \frac{\partial E_x}{\partial y} = -\mu \frac{\partial H_z}{\partial t} \Longrightarrow \frac{\partial E_y}{\partial x} - \frac{\partial E_x}{\partial y} = -j\omega\mu H_z$

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From $\nabla \times \mathbf{H} = j\omega \varepsilon \mathbf{E}$, we get

$$j\omega\varepsilon\mathbf{E} = \begin{vmatrix} \hat{\mathbf{x}} & \hat{\mathbf{y}} & \hat{\mathbf{z}} \\ \frac{\partial}{\partial x} & \frac{\partial}{\partial y} & \frac{\partial}{\partial z} \\ \frac{\partial}{\partial x} & \frac{\partial}{\partial y} & \frac{\partial}{\partial z} \end{vmatrix}$$

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$$\frac{\partial H_z}{\partial y} - \frac{\partial H_y}{\partial z} = j\omega\varepsilon E_x \Rightarrow \frac{\partial H_z}{\partial y} + j\beta_z I$$
$$\frac{\partial H_x}{\partial z} - \frac{\partial H_z}{\partial x} = j\omega\varepsilon E_y \Rightarrow -j\beta_z H_x - \frac{\partial H_z}{\partial x}$$
$$\frac{\partial H_y}{\partial z} - \frac{\partial H_z}{\partial x} = 0$$

$$\frac{\partial H_y}{\partial x} - \frac{\partial H_x}{\partial y} = 0$$

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ACTIVITY

Which number replaces the question mark?



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TM WAVES (Hz=0) Hx & Ey =0 Ez, Ex & Hy will have value. Hy = (c3 sinhx + c4 coshx) e \$ B.C Can not be applied directly to Evaluate C3 & C4. -> Because tangential component of sty = o at the surface of the Perfect conductors.

CS teamed with Combined

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 $E_{z} = \frac{1}{\partial w_{\mathcal{E}}} \frac{\partial Hy}{\partial x}$ = jwe an [c3 sin hx + c4 coshy] = ve Ez = h [C3 cas hz - c4 sin hz] e]z Jwe

ying B-C I

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Therefore E_z becomes $E_{zz} = -\frac{c_{ah}}{\frac{1}{3}\omega_{E}}$ Applying B-C II Ez = o at z = a Ez = - acy sin ha e 32 JWE To make Ez = 0 at zza, h=mT

CS -







Subs

$$E_{z} = -\frac{m\pi}{a} \frac{c_{4}}{\partial w_{E}} \frac{sm}{a} \frac{m\pi}{a}$$

$$Hy = -\frac{\partial w_{E}}{h^{2}} \frac{\partial E_{z}}{\partial x}$$

$$Hy = c_{4} \cos\left(\frac{m\pi}{a}\right) x e$$

$$III^{ly} other fields are obtained.$$

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-7z



subs F= JB fer wave propagation

$$E_{z} = -m\pi \frac{c_{4}}{a} \frac{Sn}{fwe} \frac{m\pi}{a} \frac{m\pi}{fwe} \frac{J}{a}$$

$$Hy = c_{4} \cos\left(\frac{m\pi}{a}\right) z e$$

$$E_{\chi} = \frac{\beta}{\omega \epsilon} c_4 \cos\left(\frac{m\pi}{a}\right) \chi$$

CS Spenned with California

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-JBZ The Z

-JBZ e

lds of planes.



THANK YOU

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