

SNS COLLEGE OF TECHNOLOGY



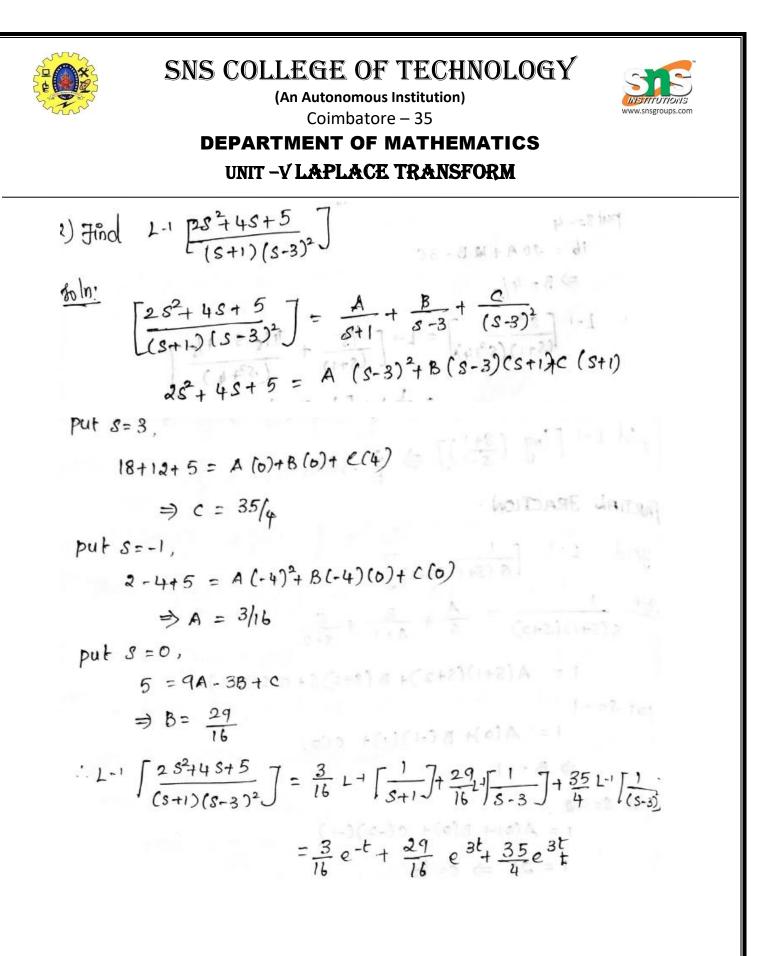
(An Autonomous Institution)

Coimbatore – 35

DEPARTMENT OF MATHEMATICS UNIT -V LAPLACE TRANSFORM

PARTIAL FRACTION : Jind 2- [s(s+1)(s+2)] $\frac{30|n:}{S(S+1)(S+2)} = \frac{A}{S} + \frac{B}{S+1} + \frac{C}{S+2}$ 1 = A(S+1)(S+2) + B(S+2)S + C S(S+1)put s=-1 I = A(0) + B(-1)(1) + c(0) $\Rightarrow B = -1$ put S = -2, 1 = A(0) + B(0) + C(-2)(-1) $1 = 2C \implies c = 1/2$ puts=0 = 01 = A(1)(2) + B(0) + C(0)=) 1= 2A =) A= 1/2 $\frac{1}{s(s+1)(s+2)} = \left[\frac{\frac{1}{2}}{\frac{1}{8}} - \frac{1}{s+1} + \frac{\frac{1}{2}}{\frac{1}{8+2}}\right]$ $L^{-1}\left[\frac{1}{S(S+1)(S+2)}\right] = L^{-1}\left[\frac{y_2}{S}\right] - L^{-1}\left[\frac{1}{S+1}\right] + L^{-1}\left[\frac{y_2}{S+2}\right]$ $=\frac{1}{2} L^{-1} \left[\frac{1}{5}\right] - L^{-1} \left[\frac{1}{5+1}\right] + \frac{1}{2} L^{-1} \left[\frac{1}{8+2}\right]$ $= \frac{1}{2} - e^{-t} + \frac{1}{2} e^{-2t}$ = $\frac{1}{2} [1 - 2e^{-t} + e^{-2t}]$ DHAN 20 C

19MAB102/ Integral Calculus & Laplace Transform S.Sindhuja/AP/Maths/SNSCT PAGE -1 of 3





SNS COLLEGE OF TECHNOLOGY



(An Autonomous Institution)

Coimbatore – 35

DEPARTMENT OF MATHEMATICS UNIT -Y LAPLACE TRANSFORM

3) $J_{100} L^{-1} \left[\frac{S^2}{(S+1)(S^2+4)} \right]$
$\frac{(36\ln 1)(s^{2}+4)}{(s+1)(s^{2}+4)} = \frac{A}{s+1} + \frac{Bs+C}{s^{2}+4}$
$3^2 = A(S_{+}^2 + 4) + BS + C(3 + 1)$
=) 1= A(5)+B(-1)(0)+c(0)
$\Rightarrow A = \frac{1}{5}$ put s = 0
put $s = 0$ $\Rightarrow 0 = 4A+C \Rightarrow C = -41s$ put $s = -4$
16 = 20 A + 12 B - 3C $\Rightarrow B = 4/5$
$ \sum_{i=1}^{n} \frac{s^2}{(s+1)(s^2+4)} = 1^{-1} \left[\frac{4s}{(s+1)} + \frac{4s-4}{(s^2+4)} \right] $
$= \frac{1}{5} L^{-1} \left[\frac{1}{5+1} \right]^{+} \frac{4}{5} \left[\frac{5}{5^{2}+4} \right]^{-} \frac{4}{5} L^{-1} \left[\frac{1}{5^{2}+4} \right]^{-}$ $= \frac{1}{5} e^{-t} + \frac{4}{5} \cos 2t - \frac{4}{5} e^{-\frac{5}{5}} \frac{1}{5^{2}+4} \int_{-\frac{5}{5}} \frac{1}{5^{2}+4} \int_$
- 18 - 18