



# **SNS COLLEGE OF TECHNOLOGY**

**Coimbatore-15**  
**An Autonomous Institution**



Accredited by NBA – AICTE and Accredited by NAAC – UGC with 'A+' Grade  
Approved by AICTE, New Delhi & Affiliated to Anna University, Chennai

## **DEPARTMENT OF ELECTRONICS & COMMUNICATION ENGINEERING**

### **19ECT212 – CONTROL SYSTEMS**

**II YEAR/ IV SEMESTER**

### **UNIT IV – STABILITY ANALYSIS**

### **TOPIC 4.3,4 ROOT LOCUS TECHNIQUES & CONSTRUCTION**

# OUTLINE



- REVIEW ABOUT PREVIOUS CLASS
- INTRODUCTION- ROOT LOCUS TECHNIQUES
- RULES FOR CONSTRUCTION OF ROOT LOCUS
- ACTIVITY
- RULES FOR CONSTRUCTION OF ROOT LOCUS
- SUMMARY



# INTRODUCTION

- The Root locus is the locus of the roots of the characteristic equation by varying system gain  $K$  from zero to infinity.
- We know that, the characteristic equation of the closed loop control system is

$$1+G(s)H(s)=0$$

- The points on the root locus branches satisfy the angle condition.
  - To know whether the point exist on root locus branch or not.
  - We can find the value of  $K$  for the points on the root locus branches by using magnitude condition.



# INTRODUCTION

- Characteristic equation of closed loop control system is

$$1+G(s)H(s)=0$$

$$\Rightarrow G(s)H(s)=-1+j0$$

- The **phase angle** of  $G(s)H(s)$  is

$$G(s)H(s)=\tan^{-1} (0/1) = (2n+1)\pi$$

- The **angle condition** is the point at which the angle of the open loop transfer function is an odd multiple of  $180^0$ .



# INTRODUCTION



- Magnitude of  $G(s)H(s)$  is –

$$|G(s)H(s)| = 1$$

- The magnitude condition is that the point (which satisfied the angle condition) at which the magnitude of the open loop transfer function is one.



# RULES FOR CONSTRUCTION OF ROOT LOCUS



- **Rule 1 – Locate the open loop poles and zeros in the ‘s’ plane**
- **Rule 2 – Find the number of root locus branches.**
  - The root locus branches start at the open loop poles and end at open loop zeros. So, the number of root locus branches  $N$  is equal to the number of finite open loop poles  $P$  or the number of finite open loop zeros  $Z$ , whichever is greater
  - Mathematically, we can write the number of root locus branches  $N$  as

$$N = P \text{ if } P \geq Z$$

$$N = Z \text{ if } P < Z$$



# Rules for Construction of Root Locus



- **Rule 3 – Identify and draw the real axis root locus branches.**
  - If the angle of the open loop transfer function at a point is an odd multiple of  $180^\circ$ , then that point is on the root locus.
  - If odd number of the open loop poles and zeros exist to the left side of a point on the real axis, then that point is on the root locus branch.
  - Therefore, the branch of points which satisfies this condition is the real axis of the root locus branch.



# ACTIVITY

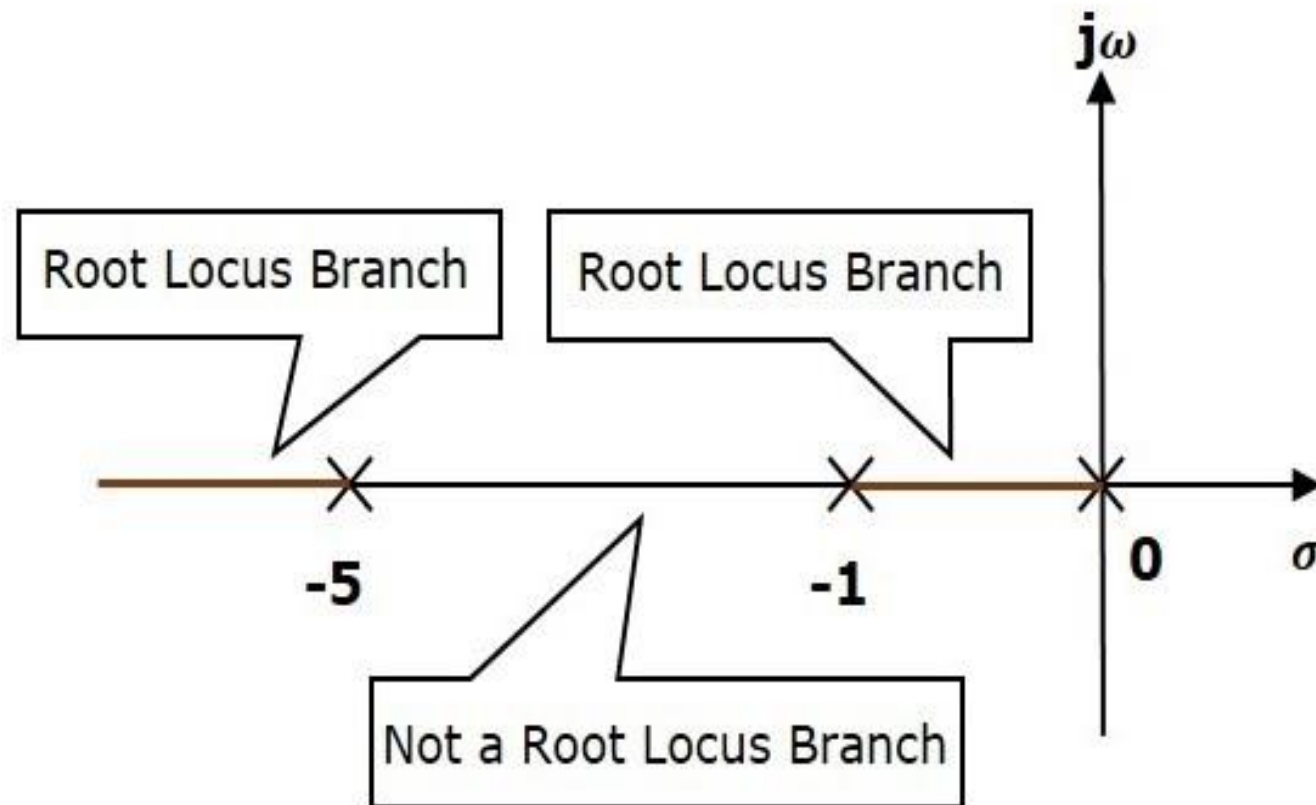


## GROUP DISCUSSION





# RULES FOR CONSTRUCTION OF ROOT LOCUS





# RULES FOR CONSTRUCTION OF ROOT LOCUS



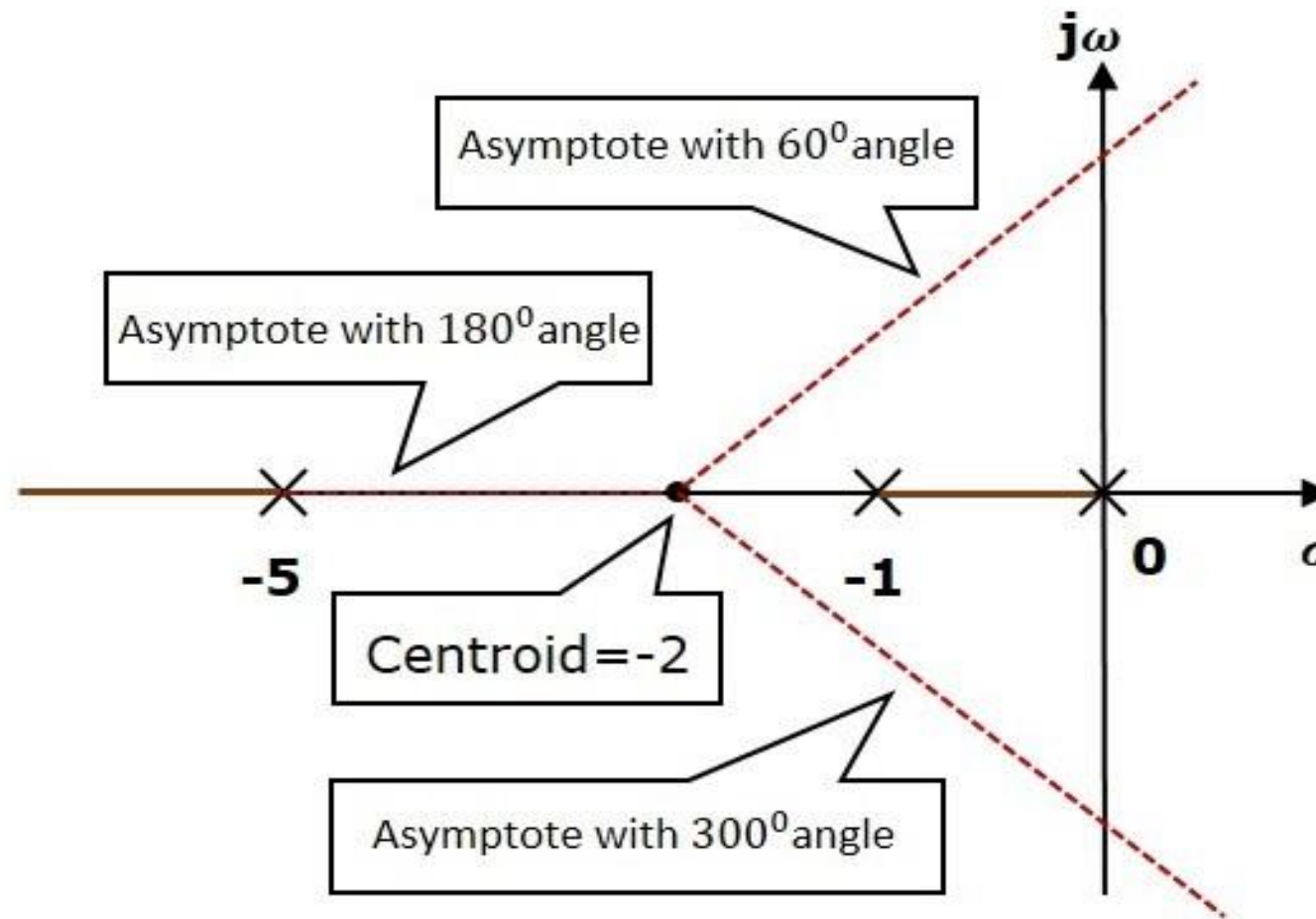
- **Rule 4 – Find the centroid and the angle of asymptotes**
  - If  $P=Z$ , then all the root locus branches start at finite open loop poles and end at finite open loop zeros.
  - If  $P>Z$ , then  $Z$  number of root locus branches start at finite open loop poles and end at finite open loop zeros and  $P-Z$  number of root locus branches start at finite open loop poles and end at infinite open loop zeros.
  - If  $P<Z$ , then  $P$  number of root locus branches start at finite open loop poles and end at finite open loop zeros and  $Z-P$  number of root locus branches start at infinite open loop poles and end at finite open loop zeros.

**Centroid = Sum of poles – Sum of zeros / (n-m)**

**The angle of asymptotes =  $180(2q\pm 1) / (n-m)$**



# Rules for Construction of Root Locus





# Rules for Construction of Root Locus



- **Rule 5 – Find Break-away and Break-in points.**
  - If there exists a real axis root locus branch between two open loop poles, then there will be a break-away point in between these two open loop poles.
  - If there exists a real axis root locus branch between two open loop zeros, then there will be a break-in point in between these two open loop zeros
- Write  $K$  in terms of  $ss$  from the characteristic equation  $1+G(s)H(s)=0$ .
- Differentiate  $K$  with respect to  $s$  and make it equal to zero. Substitute these values of  $ss$  in the above equation.
- The values of  $ss$  for which the  $K$  value is positive are the **break points**.



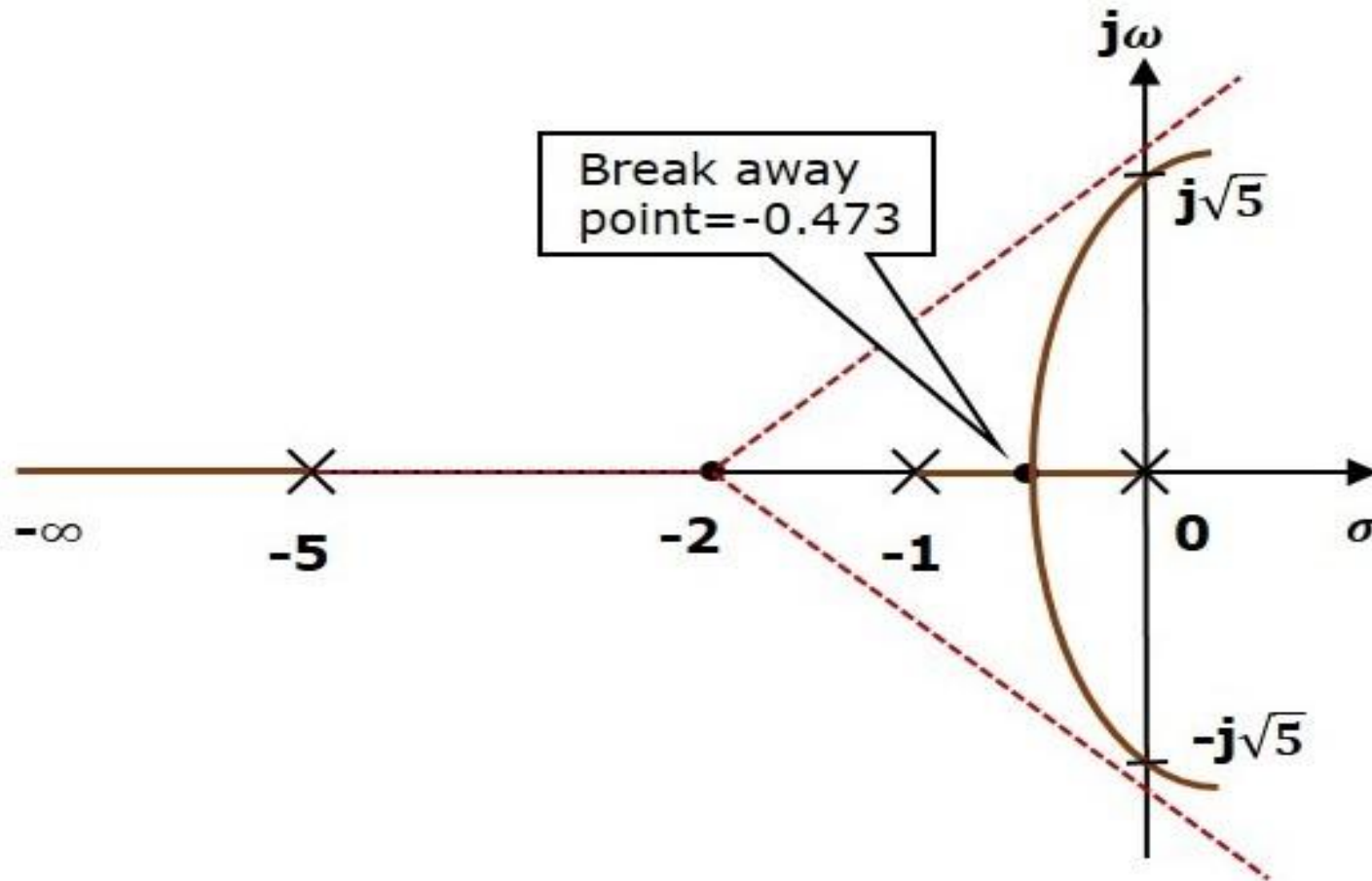
# Rules for Construction of Root Locus



- **Rule 6 – Find the angle of departure and the angle of arrival.**
  - The Angle of departure and the angle of arrival can be calculated at complex conjugate open loop poles and complex conjugate open loop zeros respectively
- **Rule 7 – Intersection point on imaginary axis**
  - Substitute  $s=j\omega$  in the characteristic equation and equate real part and imaginary part to zero separately



# Rules for Construction of Root Locus





# SUMMARY

<https://www.youtube.com/watch?v=sBO7R5GQpfl>

<https://www.youtube.com/watch?v=iR1A4vnops0>

