

## SNS COLLEGE OF TECHNOLOGY



## (An Autonomous Institution) DEPARTMENT OF AERONAUTICAL ENGINEERING

Subject Code & Name: 19AST203 Aircraft Structural Mechanics

## TOPIC: Bredt – Batho formula

## **Bredt-Batho formulae**

The 1st Bredt-Batho formula indicates the relationship between the torsional moment MT acting on a thin-walled hollow tube, its enclosed area Am and the resultant shear flow T / shear stress  $\tau$ . It is calculated as follows:  $\tau$ =Tt=MT2·Am·t.

The variable t represents the thin-walled component's wall thickness. The enclosed area Am lies within the centre line of the tube and is also called the hollow area. The shear stress  $\tau$  resulting from the <u>Torsion</u> is constant over the entire wall thickness t, which means that the shear flow T also remains constant in the circumferential direction.

The 2nd Bredt-Batho formula indicates the component's twisting  $\vartheta$ , which depends on the material's shear modulus G. A component's torsional <u>Resistance</u> I<sub>T</sub> can also be determined.

The Bredt-Bredt-Batho formulae apply only to torsion acting on closed hollow tubes with an axis of <u>Rotation</u> that lies on the shear centre.

A beam with a closed section experiencing only a pure torque T and without any axial constraints, does not develop direct stresses, ie s z = 0.

So equations (4.2) and (4.3) become:

$$\frac{\partial q}{\partial s} = \frac{\partial q}{\partial z} = 0$$

The only way to satisfy these equations would be if the shear flow 'q' was constant.

NOTE: Although 'q' is constant, the shear stress 't ' may not be if the wall thickness 't' varied with 's'.



Figure 45: Closed beam with applied torque.

To determine the relationship between applied torque and shear flow,

apply equilibrium to the end of the beam.

In essence the applied Torque T must equal to the torque generated by the shear flow.

Look at the end of beam, and a small section ds.



Figure 46: Equating applied torque with moment generated by shear flow.

The torque produced by the shear flow on element ds is pqsd s. Integrating about the whole section gives:

 $T = \oint pqds$ 

We have previously defined that:

$$\oint pds = 2A$$

Therefore:

$$q = \frac{T}{2A}$$
(5.1)

Often referred to as the 'Bredt-Batho Formula'. Substituting this equation into (4.21) gives the rate of twist due to the Torque 'T':

Let us suppose the origins where the shear flow has unknown values 9 s. or sin all avias of Then for closed section along as being a section  $q_{s} = \frac{-S_{x}}{I_{yy}} \int x + ds - \frac{\overline{S}_{y}}{\overline{I}_{xx}} \int y + ds + q_{s,0}$ 9 = 96+950 9310 = -M Ms unbalanced Moment 96 basic Shear flow equation for open tube 95,0 > Unknown shearflow equation at origin of 's co-ordinates. The value of shearflow at origin of 's' is found by making a cut at that point and equating applied the initial moments, taken abo some convinience point. ) plot Shearflow for given closed Section 82 1000N - E3A 40 HOM

$$\begin{aligned} F \times x = P + 0 = -12 (13.32)^{2} \\ F \times x = 2267.74 cm^{4} \\ T = 2267.74 cm^{4} \\ T = 2267.74 cm^{4} \\ T = 29 = 6400 - 12 (13.33)^{2} \\ T = 29 = 6400 - 12 (13.33)^{2} \\ T = 29 = 4267.73 cm^{4} \\ T = 29 = 4267.73 cm^{4} \\ T = 29 = 6400 - 12 (13.33) (13.33) \\ T = 29 = 4267.74 \\ T = 29 = 12 (13.33) (13.33) \\ T = 29 = -53 2.26 cm^{4} \\ T = 29 =$$

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$$\begin{aligned} P_{s} &= P_{b} + P_{s,0} \\ P_{s,0} &= -\frac{H}{2h} \\ P &= \frac{1}{2} \pi r^{2} + \frac{1}{3} bh \\ P &= \left[ \frac{1}{2} \times \pi \times 18^{2} + \frac{1}{3} \times (\mu \circ \times 10) + (\mu \circ \times 20) \right] \\ A &= 1353 \cdot H^{2} cm^{2} \\ Moment about b 'b ' (unbedenced homent) \\ A &= (10000 \times 10 - 2) \left( \frac{\pi r^{2}}{2} \right) \times 27.26 \right) \\ H &= (-10000 \times 10 - 2) \left( \frac{\pi r^{2}}{2} \right) \times 27.26 \right) \\ H &= 0.0000 - 2\pi \cdot 26 \times \pi \times 15^{2} + 9 \cdot 08 \times 800 \\ = -2\pi 36 - 2\pi \cdot 26 \times \pi \times 15^{2} + 9 \cdot 08 \times 800 \\ H &= -22000H \cdot 95 N lon \\ Q_{5,0} &= 8 \cdot 129 N lom \\ Q_{5,0} &= 9 ad \\ Shear flow of closed Section \\ Q_{5} &= 9b + 9s \cdot 0 \\ Q_{ab} &= -2\pi \cdot 26 + 8 \cdot 13 \\ Q_{ab} &= -19 \cdot 13 \end{aligned}$$

9.bc = 0 + 8.13 9bc = 8.13 N lcm 9cd = 9.08+8.13 9cd = 17.21 NICM 1 FORT C-22004.95 2 × 1353.45 9510 = \$10 = 8.13 N Com 95.0 ma cit. d 40/8.13 7. 1 3 C=1× TT × 30. FC - 3 3-14 Torsional effect of Multicell tube: mal 428. 40000find Assumption: -1. Angle of twist is equalifor all cells?  $\Theta_1 = \Theta_2 = \Theta_3 = \Theta$ hop = arp 2. Material is homogeneous. barolo 20 walt ( A \$. It obeys hooks law. 4. Beam is subjected to torque ale S1. 8 4 20, 10 for single cell 21. 91-T= 2A9

