



#### (An Autonomous Institution) Coimbatore – 35

### DEPARTMENT OF MATHEMATICS UNIT – I TESTING OF HYPOTHESIS

DEST OF SIGNIFICENCE OF SMALL BAMPLES!

VARIANCE RATIO TEST (07) F- Test FOR EQUALITY OF VARIANCE

Null Thypothesis: Ho: T,2= T22

Test stastics:  $F = \frac{8^2}{5^2}$  where  $5^2 > 5^2$ .

ushere  $S_1^2 = \frac{n_1 S_1^2}{n_1 - 1}$  of  $S_1^2 = \frac{\sum (\alpha_1 - \overline{\lambda}_1)^2}{n_1 - 1}$  &

 $\frac{S_2^2 = n_2 S_2^2}{n_2 - 1}$  of  $S_2^2 = \frac{\sum (n_2 - \bar{n}_2)^2}{n_{2-1}}$ 

Deglee & Freedom: (V1, V2)

where 1 = (n,-1), vo = (n,-1)

Note 1:- F Greater than zone always.

Note 2: - Suppose S2 greater than S,2, then F = S22

with digree of greadom, VI=n2-1, v2=n1-1

Applicettons ? 'I test' & used to test of the two samples have come from the same population.





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) two landom sample of 11 and of lems show that the sample standard deviations of their weights as 0.8 & 0.5 nespectively. Assuming that the weight distributions are normal, test the hypothesis that the true variances are equal, against the alternative hypothesis that they are son: Given . . n = 11 , 31 = 0.8 n2=9, 82 =0.5  $S_1^2 = \frac{n_1 s_1^2}{n_1 - 1} = \frac{11(0.8)^2}{11 - 1} = 0.404$  $\frac{g_2^2 = \frac{n \times g_2^2}{n_{2-1}}}{n_{2-1}} = \frac{9(0.5)^2}{9-1} = 0.2812$ step 1 -> Formulate Ho & HI. Ho: 2, = 23 the second second second H1: 5,2 + 5,2 stip 2 -> Los at x = 5 y. slip 3 > Test Statistic, F= \frac{S12}{S22} = \frac{0.704}{0.2812} = 2.5 stip 4 - Degrees & freedom (1914) (n.-1, n2-1) = 2 Ceincalvalue, Ftab: Fx = 3.35 Step 5 → conclusion: F=2.5 < 3.35= Fx

:. Ho is accepted at x:5%.





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) Two eardom samples yave the zollowing levelle:

Sample Size samplemean sum g equals a deviation from the means.

1 12 14 108

2 10 15 90

Test whether the samples came from the same population.

Population.

$$N_1 = 12$$
,  $X_1 = 14$ ,  $(x_1 - \overline{x}_1)^2 = 108$ 
 $x_2 = 10$ ,  $x_2 = 15$ ,  $(x_2 - \overline{x}_2)^2 = 90$ 
 $x_3^2 = \frac{\mathcal{E}(n_1 - \overline{n}_3)^2}{n_1 - 1} = \frac{108}{12 - 1} = 9.818$ 
 $x_3^2 < x_2^2$ 

Step 1: Formulate Ho and Hi:

Ho:  $x_1^2 = x_2^2$ 

stip o: Los at a = 5%.

Step 3: Test statéstics, 
$$R = \frac{S_2^2}{S_{12}} = \frac{10}{9.818}$$

F = 1.018





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critical value, Fx = 2.90

Step & : Conclusion:

.. Ho is accepted at 5% Los.

(ii) t - Test:

step 1: Hormulate Ho & Hi:

Ho: H1 = H2 olip 2: Los at 5/ = x

Step 3: Test Statistic, 
$$l = \overline{x_1} - \overline{x_2}$$

$$S \sqrt{\frac{1}{n_1} + \frac{1}{n_2}}$$
Here  $n_1 = 12$ ,  $n_2 = 10$ ;  $\overline{x_1} = 14$ ,  $\overline{x_2} = 15$ 

$$Now s^2 = \underbrace{\sum (x_1 - \overline{x_1})^2 + \sum (x_2 - \overline{x_2})^2}_{n_1 + n_2 - 2}$$

$$= \underbrace{108 + 90}_{12 + 10 - 2} = 9.9$$

$$S = 3.14$$





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$$S_1^2 = \frac{\sum (\pi_1 - \overline{\pi}_1)^2}{n_1 - 1} = \frac{\mu_1 \cdot 5}{7} = 5.9286$$

$$S_2^2 = \frac{\sum (\pi_2 - \overline{\pi}_2)^2}{n_2 - 1} = \frac{101.7143}{6} = 16.9524$$

$$S_1^2 < S_2^2$$

$$Step 1 : \text{ formulate Ho & Hi :}$$

$$H_6: \nabla_1^2 = \nabla_2^2$$

$$H_1: \nabla_1^2 \neq \sigma_2^2$$

$$Step 2 : \text{ Los at } \sigma = 1 \text{ y.}$$

$$Step 3 : \text{ Test statistic, } F = \frac{S_2^2}{S_1^2}$$

$$= \frac{16.9524}{5.9286} := 2.86$$

$$\text{Otep 4 : } \text{ respects } q \text{ Freedom, : } (v_1, v_2)$$

$$= (n_2 \cdot 1, n_1 \cdot 1)$$

$$= (6, 4)$$

$$\text{Step 5 : Conclusion, } F = 2.86 < 7.19 = Fx$$

$$\text{Ho & accepted at Ho at } 1 \text{ y. 20} \text{ s.}$$