

(An Autonomous Institution) Coimbatore - 641 035 DEPARTMENT OF MATHEMATICS POISSON DISTRIBUTION



Por 8500 alstabution:

A mandom variable x & said to follow Pol & on by non hegative values of its probability mass function is given by,

$$P[X=x] = \frac{e^{\lambda} a^{x}}{x!}, \quad \text{se} = 0 \pm 0 \text{ and inhere is } a$$

$$P(x=x) = \frac{e^{\lambda} a^{x}}{x!}, \quad \text{se} = 0 \pm 0 \text{ and inhere is } a$$

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Peoporty:

\* Binomial detailbution B a lamiting case of pollson distribution.

\* n→∞, P+0

MGIF, mean and voulance of Potosson eschibilition:

MGIF:  $M_{x}(t) = \sum_{x=0}^{\infty} e^{\pm x} p(x)$  $= \underbrace{\varepsilon}_{\alpha=0}^{\infty} e^{\pm \alpha} \underbrace{e^{-\lambda} \lambda^{\alpha}}_{\alpha!}$  $= e^{-\lambda} \frac{20}{2} e^{\pm x \cdot \lambda^{x}}$ = e d s (det) d  $= \bar{e}^{\lambda} \left[ \frac{(\lambda e^{\pm})^{\circ}}{0!} + \frac{(\lambda e^{\pm})^{\prime}}{1!} + \frac{(\lambda e^{\pm})^{\circ}}{2!} + \dots \right]$  $= e^{\lambda} \left[ 1 + \frac{\lambda e^{t}}{1!} + \frac{(\lambda e^{t})^{2}}{2!} + \dots \right]$  $= e^{-\lambda} \left[ e^{e^{t} \lambda} \right] \left[ e^{x} = 1 + \frac{x^{2}}{1!} + \frac{x^{2}}{2!} + \cdots \right]$   $= e^{-\lambda + \lambda} e^{t}$   $= e^{-\lambda + \lambda} e^{t}$ 



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$$m_{x}(t) = e^{(e^{t}-1)A}$$

mean!

$$E(x) = \left[\frac{d}{dt} m_{x}(t)\right]$$

$$= \left[\frac{d}{dt} e^{(e^{t}-1)} \lambda\right]$$

$$= \left[e^{(e^{t}-1)} \lambda\right]$$

$$= \lambda e^{(e^{t}-1)}$$

Variance:

$$Vosition definition of the content of the content$$

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mx (f) = 0y(6+-1)

 $mean = \lambda$ valance = 7



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I IF a polision variate P(x=q) = 9P(x=4) + 90P(x=6). Find mean and voulance. Soln.

$$\frac{x!}{6-y} = (x=x) = \frac{x!}{6-y}$$

(18ven, 
$$P(x=2) = P(x=4) + P(x=6)$$
  

$$\frac{e^{-\lambda} \lambda^2}{2!} = Q \frac{e^{-\lambda} \lambda^4}{4!} + QO \frac{e^{\lambda} \lambda^6}{6!}$$

$$\frac{\partial^{2}}{\partial x} = \frac{9\lambda^{4}}{24} + \frac{90\lambda^{6}}{720}$$

$$\frac{\partial^{2}}{\partial x} = \frac{9\lambda^{2}}{24} + \frac{90\lambda^{4}}{720}$$

$$\frac{1}{2} = \frac{9\lambda^{2}}{24} + \frac{90\lambda^{4}}{720}$$

$$\frac{1}{2} = \frac{3\lambda^{2}}{8} + \frac{\lambda^{4}}{8}$$

$$\lambda^{4} + 3\lambda^{2} = 4$$

$$\lambda^{4} + 3\lambda^{2} - 4 = 0$$

$$\lambda^{4} + 3\lambda^{2} = 4$$

$$3^{3}+3^{2}+43+4=0$$
 and

$$\lambda^{3} + \lambda^{2} + 4\lambda + 4 = 0$$
 and  $\lambda^{3} + \lambda^{2} + 4\lambda + 4 = 0$  and  $\lambda = -1$   $\lambda = -1$ 

mean = vollarie = 2

where u and or are mean and variance of Potskop distribution.

Potason distribution.

Soln.

Cavon, 
$$M_{\chi}(t) = e^{+(e^{t}-1)}$$
 $e^{\lambda(e^{t}-1)} = e^{+(e^{t}-1)}$ 
 $\Rightarrow \lambda = 4$ 



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Mean = 
$$\lambda = 4 \Rightarrow \text{mean} = \mu$$
  
 $\lambda = \mu$ 

Now, 
$$P(x = \lambda + \delta) = P(x = \lambda + \delta) = P(x = b)$$
  
P(x = x) =  $\frac{e^{-\lambda}}{x!}$ ,  $x = 0 \pm 0$ ,  $\infty$   

$$P(x = b) = \frac{e^{-\lambda} + b}{b!}$$

$$= \frac{(0.018)4096}{720}$$

$$P(x = b) = 0.102$$

3) The number of monthly breakdown of a Computer & a landom vaulable baring Polisson destribution with mean equal to 1.8. Find the Puebability that this computer will function for a motith with only one breakdown. Soln.

PD: 
$$P[x=x] = \frac{e^{\lambda} \lambda^{x}}{x!}$$
  
Cryon, mean  $\lambda = 1.8$   
 $P[x=x] = \frac{e^{-1.8}(-8)^{x}}{x!}$ 



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$$P[x=i] = \frac{e^{-1.8} (1.8)^{1}}{1}$$

$$= 0.165 \times 1.8$$

$$P[x=i] = 0.297$$

4] If 3% of electric bulbs manufacture by a company are defective. Find the probability that 90 the Sample of loo bulbs exactly 5 bulbs are defective..

Soln.

PD: 
$$P(x=x) = \frac{e^{-\lambda} \lambda^{\alpha}}{x!}$$

Caren, 
$$h=100$$
,  $p=3\% = 0.03$   
 $h=np$   
=100 (0.03)

$$\begin{array}{r}
 \lambda = 3 \\
 \text{Now,} \quad P(x = 5) = \frac{e^{3} (3)^{5}}{5!} \\
 = \underbrace{(0.05)(243)}_{120} \\
 = \underbrace{12.150}_{120}
 \end{array}$$

b] A manufacturior of PPns knows that & 1, of the product are defective. If he bells pris in boxes of 100 and guarantees that not more than 4 ping will be defective. What is the perpartinty that box fall, meet guarantee quality? W911

= 0.101



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Soln.

Given 
$$n=100$$
,  $P=2.7.=0.02$   
 $A=DP$   
 $=100 \times 0.02$   
 $A=2$ 

Now, 
$$P(x \le 4) = 1 - P(x > 4)$$
  
 $P(x > 4) = 1 - P(x \le 4)$   
 $= 1 - \left[ P(x = 0) + P(x = 1) + P(x = 2) + P(x = 3) + P(x = 4) \right]$   
 $= 1 - e^{-2} \left[ \frac{20}{0!} + \frac{21}{1!} + \frac{2}{2!} + \frac{2}{3!} + \frac{2}{4!} \right]$   
 $= 1 - e^{-2} \left[ 1 + 2 + \frac{4}{2} + \frac{8}{6} + \frac{16}{24} \right]$   
 $= 1 - 0.135 \left[ \frac{3 + 6 + 6 + 4 + 2}{3} \right]$   
 $= 1 - 0.135 \left[ \frac{21}{3} \right]$   
 $= 1 - 0.135 \left[ \frac{7}{3} \right]$   
 $= 1 - 0.135 \left[ \frac{7}{3} \right]$ 

HW J. A can have from 2 cars cobach it haves out day by day. The number of demands for a con 910 each day & dischabilted with mean Calculate the preposition of days sowisch i). perther car is used 1) Some demand

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= 0.055