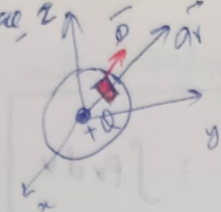


Flux density at any point on the surface,  $\vec{D}$

is  $\vec{D} = \frac{Q}{4\pi r^2} \hat{a}_r \text{ C/m}^2$



vector form

$$\vec{D} = \frac{d\psi}{dS} \hat{a}_n \text{ C/m}^2$$

$$S = 4\pi r^2$$

Relation between  $\vec{D}$  and  $\vec{E}$

$$\vec{E} = \frac{Q}{4\pi\epsilon_0 r^2} \hat{a}_r$$

$$\vec{E} = \vec{D}/\epsilon$$

$$\boxed{\vec{D} = \epsilon \vec{E}}$$

$d\psi \Rightarrow$  Total flux lines crossing normal thro. the diff surface area  $dS$

Electric flux density is also called as electric displacement.

### Gauss's law

Objective:- To learn one of the fundamental law of electromagnetics

To find fields due to symmetrical charge distributions

Gauss's law constitutes one of the fundamental laws of electromagnetism.

Gauss law states that the total electric flux  $\psi$  through any closed surface is equal to the total charge enclosed by that surface.

$$\psi = Q_{enc}$$

$$\psi = \oint_S d\psi$$

$$\psi = \oint_S \vec{D} \cdot d\vec{s} = \text{total charge enclosed}$$

$$Q = \int_V \rho_v dv$$

or

$$Q = \oint_S \vec{D} \cdot d\vec{s} = \int_V \rho_v dv$$

Integral form

Applying divergence theorem

$$\oint_S \vec{D} \cdot d\vec{s} = \int_V \nabla \cdot \vec{D} dv$$

Comparing two equations

$$\rho_v = \nabla \cdot \vec{D}$$

Differential or point form.

which is first of the four Maxwell's equations.

Equation states that the volume charge density is the same as the divergence of electric flux density.

(It relates the definition of divergence & also (WKT  $\rho_v$  is simply at charge per unit volume))

Advantages :-

Gauss' law provides an easy means of finding  $E$  or  $D$  for symmetrical charge distributions, such as a point charge, an infinite line charge, an infinite cylindrical surface charge & a spherical distribution of charge.

Proof of Gauss's law :-

Consider a point charge  $Q$  kept at the origin.

Consider a small area ' $ds$ ' on the surface of the sphere

Let  $d\psi$  be the flux crossing the surface.

$$d\psi = \vec{D} \cdot d\vec{s}$$

$$= D ds \cos\theta$$

$$d\psi = D ds \cos\theta$$

$$\vec{E} = \frac{\vec{D}}{\epsilon_0}$$

$$\vec{E} = \frac{\rho_s}{2\epsilon_0} \hat{z}$$

Gauss Divergence theorem

From gauss law

$$\iint \mathbf{D} \cdot d\mathbf{s} = Q$$

$$Q = \iiint \rho_v dv$$

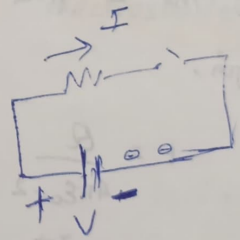
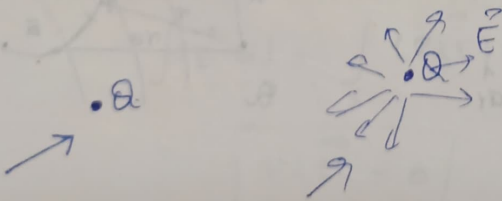
$$\iint \mathbf{D} \cdot d\mathbf{s} = \iiint \rho_v dv$$

$$\boxed{\iint \mathbf{D} \cdot d\mathbf{s} = \iiint \nabla \cdot \mathbf{D} dv}$$

from point form of gauss law,

$$\nabla \cdot \mathbf{D} = \rho_v$$

Electric Potential:



We wish to move a point charge  $Q$  from Point A to Point B in an electric field  $E$ . From coulomb's law, force on  $Q$  is  $F = QE$ , so that the work done by external force in displacing the charge by  $d\mathbf{l}$

$$dw = -F \cdot d\mathbf{l} = -QE \cdot d\mathbf{l}$$