

(An Autonomous Institution) Coimbatore - 641 035 DEPARTMENT OF MATHEMATICS UNIT-1 PROBABILITY AND RANDOM VARIABLES



Probabalaty:

plobabo Rty is a concept which we use to deal with uncontainty.

- * we use purbability 90 dayly life to make deustons when you don't know for swee what the outcome will be. For example,
 - 1. Most probably it will main today
 - I doubt that he will win the stace.
 - 3. Chances we high that the pulles of Petrol will go up.

APPROations:

- * modeling of text and web data
- * Speech recognition
- * Robotacs
- * Network traffic and system Relpability modeling
- * Probabilities analyses of algorithms and
- * Machine learning and data mining
- * Cryptography



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Terms solated with Probability: Exportment:

An experiment which, though repeated under essentially identical conditions does not give unique nesults but may nesult in any one of the several possible outcomes

Out come:

A Hesulf of an exposement is called an out come.

sample space:

A Sample space is the collection of air possible out comos.

Trial:

Postorming an experiment is known as total

Event:

The outcomes of the experiment are known as Event.

Types of Events:

* Mutually Exclusive Events:

It the occurence of one event excludes the occurrence of another event, such events mutually exclusive events

* Exhaustive Events:

A set of events is called exhaustavo, of all the events together consume the entire. Sample Space.

Independent event: If the occurrence of one event has no influence Over the occurrence of the other event.



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Published of an event:

J. Find the purbability of getting

ii), an odd number 9n a 19e.

$$S = \{1, 2, 3, 4, 5, 6\}$$

$$P(A) = \frac{1}{6} ; P(B) = \frac{3}{6} = \frac{1}{2}.$$

2] It a corn is tossed, then what is the Probabolity of getting head?

$$S = \{H,T\}$$

$$P(Head) = \frac{1}{2}$$

3] If you flip a balanced win twice, what is the peobability of getting atleast one head?

S= {HH, HT, TH, TT}

P(atleast one head)
= 3
H



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Axtoms of pubability:

- J. For any event A, $P(A) \geq 0$
- 2]. psubability of the sample space 5 % P(S)=1
- 3]. If A_1, A_2, \ldots are disjoint events, then $P[A_1 \cup A_2 \cup \ldots] = P[A_1] + P[A_2] + \ldots \quad [A_n] = \emptyset]$

Rosults:

- i). P[\$J=0 impossible event
- iv. P[A] = 1- P[A]
 - iii) P(AnB)= P(AUB)
 - IV). P(AUB) = P(ADB)
 - V). P[AVB) = P(A) + P(B) A&B are mutually exclusive events
 - VI). P(AMB) = P(A). P(B) A&B are independent
 - Vii). P(AUB) = P(A) + P(B) P(ANB)
 - Viii) P(ACUBC) = P(ANB)C ; P(ACNBC) = P(AUB)C
 - ix). P(A+B)= P(AUB); P(AB) = P(ANB)

problems.

J. If P(A) = 0.4, P(B) = 0.7 and P(ADB) = 0.3.

Frnd P(AnB) and P(AUB)

Soln :

$$P(\bar{A}) = 1 - P(A) = 1 - 0.4 = 0.6$$

$$P(\overline{B}) = 1 - P(B) = 1 - 0.7 = 0.3$$

$$P(\overline{A}\overline{D}) = P(\overline{A}\overline{D}) = 1 - P(\overline{A}\overline{D})$$

= $1 - [P(A) + P(B) - P(\overline{A}\overline{D})]$



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$$=1-[0.4+0.7-0.3] = 1-0.8 = 0.2$$

 $P(\overline{A}\overline{B}) = 0.2$
 $P(\overline{A}\overline{B}) = P(\overline{A}\overline{B}) = 1-P(\overline{A}\overline{B})$
 $=1-0.3$
 $P(\overline{A}\overline{B}) = 0.7$

R. If A and B one even with
$$P(A) = \frac{3}{8}$$
, $P(B) = \frac{1}{2}$ and $P(A \cap B) = \frac{1}{4}$. $P(A \cap B) = \frac{3}{4}$



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$$P(A \cup B) = P(A) + P(B) - P(A \cap B)$$

$$P(B) = P(A \cup B) - P(A) + P(A \cap B)$$

$$= \frac{3}{4} - \frac{1}{3} + \frac{1}{4} = \frac{9 - 4 + 3}{12}$$

$$P(B) = \frac{8}{12} = \frac{2}{3}$$

4). A bag containing 6 red, 4 black and T blue, 10 white, Fire balls are drawn at Houndom, what is the peobability that two of them eve led and one is black, two is blue.

Soln. GR. ABLA TB IOW = 27 Prob = 6C2 × 4C1 × 7C2 = 8×5× 4×7×6×8×4×8×2×1(nc1=n) ×1×××1×24×26×25×24×23 9x 13 8 13 $=\frac{14}{897}=0.015$

A bag containing 5 white balle, 6 green balls. Three balls eve drawn with 5]. leplacement. what is the chance that

- All are same color
- They are alternatively different color. 11)



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1). All one game color

Plots =
$$\frac{\text{Effent}}{\text{All}}$$
 one white on All one Green

$$= \frac{5c_3}{11c_3} + \frac{bc_3}{11c_3}$$

$$= \frac{\cancel{5} \times \cancel{4} \times \cancel{3} \times \cancel{3} \times \cancel{4} \times \cancel{4}}{\cancel{3} \times \cancel{4} \times \cancel{3} \times \cancel{4} \times \cancel{4}} + \frac{\cancel{5} \times \cancel{5} \times \cancel{4} \times \cancel{3} \times \cancel{2} \times \cancel{4}}{\cancel{3} \times \cancel{4} \times \cancel{3} \times \cancel{4} \times \cancel{4}} + \frac{\cancel{5} \times \cancel{5} \times \cancel{4} \times \cancel{4} \times \cancel{4} \times \cancel{4} \times \cancel{4}}{\cancel{3} \times \cancel{4} \times \cancel{4} \times \cancel{4} \times \cancel{4} \times \cancel{4}} + \frac{\cancel{5} \times \cancel{5} \times \cancel{5} \times \cancel{4} \times \cancel{4} \times \cancel{4}}{\cancel{3} \times \cancel{4} \times \cancel{4} \times \cancel{4} \times \cancel{4}} + \frac{\cancel{5} \times \cancel{5} \times \cancel{$$



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$$= P(WGW) + P(GWG)$$

$$= \frac{5C_1 \frac{6C_1}{11C_1}}{11C_1} \frac{6C_1}{10C_1} \frac{4C_1}{9C_1} + \frac{6C_1}{11C_1} \frac{5C_1}{10C_1} \frac{5C_1}{9C_1}$$

$$= \frac{5 \times \cancel{8} \times 4}{11 \times \cancel{9} \times \cancel{9}_3} + \frac{\cancel{8} \times \cancel{8} \times 5}{11 \times \cancel{9} \times \cancel{9}_3}$$

$$= \frac{4}{33} + \frac{5}{33} = \frac{9}{33} = \frac{3}{11} = 0.27$$