

SNS COLLEGE OF TECHNOLOGY An Autonomous Institution Coimbatore-35

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DEPARTMENT OF ELECTRONICS & COMMUNICATION ENGINEERING 19ECB212 – DIGITAL SIGNAL PROCESSING

II YEAR/ IV SEMESTER

UNIT 2 – IIR FILTER DESIGN

TOPIC – REALIZATION STRUCTURES FOR IIR FILTERS





Z TRANSFORM

- Z transform is used for the analysis of discrete time signals.
- It is more broad compared to Discrete Time Fourier Transform
- It is very much useful in discrete time signals as well as system analysis
- x(n) and X(Z) is called Z transform pair



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LTI DT SYSTEM

System Transfer Function: Ratio of the output to the input. \bullet



Frequency Response: lacksquare



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DIFFERENCE EQUATION

- **Difference Equation:** It is an efficient way to implement discrete time ${\bullet}$ systems
- The convolution of input sequence x(n) and unit sample response h(n)ulletgives the output y(n)

$$y(n) = \sum_{k=-\infty}^{\infty} x(k) h(n)$$

Two types of systems depending upon the length of unit sample response lacksquareh(k)

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-k



LTI DISCRETE TIME SYSTEMS

Finite Impulse Response (FIR) Systems: Unit sample response (or) Impulse response h(n) has finite no. of terms

$$y(n) = \sum_{k=0}^{M-1} h(k) x$$

Infinite Impulse Response (IIR) Systems: Length of Unit sample response (or) Impulse response h(n) is infinite $y(n) = \sum_{k=1}^{\infty} h(k) x(n-k)$

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(n-k)



LTI DISCRETE TIME SYSTEMS

Recursive Systems: Output y(n) depends on present and past inputs as well as past output

$$y(n) = \sum_{k=0}^{n} x(x)$$

Non Recursive Systems: Output y(n) depends on present and past input.



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$$=\sum_{k=0}^{M}h(k) x(n-k)$$



BLOCK DI&GRAM

- The discrete time systems are represented by block diagrams.
- They are also called structures of discrete time systems.
- It can be classified into four types
- 1. Direct Form I
- 2. Direct Form II
- 3. Cascade Form and
- 4. Parallel Form

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ELEMENTARY BLOCKS



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ELEMENTARY BLOCKS



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$$y(n) = x1(n)*x2(n)$$



BLOCK DIAGRAM REPRESENTATION

y(n) = y(n-1) x(n-1) + 0.5 x(n)



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BLOCK DIAGRAM REPRESENTATION

 $H(z) = 1/1 - a z^{-1}$



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BLOCK DIAGRAM REPRESENTATION

$$y[n] = a_1 y[n-1] + a_2 y[n-2]$$



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$2] + b_0 x[n]$



GENERAL DIRECT FORM I



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DIRECT FORM II

$$H(z) = \frac{\sum_{k=0}^{M} b_{k} z^{k}}{1 + \sum_{k=1}^{N} a_{k} z^{k}}$$

$$H(z) = \frac{Y(z)}{X(z)} \xrightarrow{2} \frac{Y(z)}{W(z)} \cdot \frac{W(z)}{X(z)} \xrightarrow{2}$$

$$H_{1}(z) = \frac{W(z)}{x(z)} = \frac{1}{1 + \sum_{k=1}^{N} a_{k} z^{k}}$$

$$H_{2}(z) = \frac{Y(z)}{W(z)} = \frac{H}{W(z)} = \frac{L}{K_{2}} b_{k} z^{-k}$$

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$\frac{W(z)}{X(z)} \cdot \frac{Y(z)}{W(z)}$





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DIRECT FORM I



y(n) = 3/4 y(n-1) - 1/8 y(n-2) + x(n) + 1/2 x(n-1)



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DIRECT FORM II



y(n) = 3/4 y(n-1) - 1/8 y(n-2) + x(n) + 1/2 x(n-1)



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DIRECT FORM I & II

System Function : Direct form I & TI Consider $H(z) = \frac{1 + 2z^{-1} + z^{-2}}{1 - 0.75z^{-1} + 0.125z^{-2}}$ $H(x) = \frac{Y(x)}{X(x)} = \frac{1+2x^{-2}}{1-0.15x^{1}+x^{-2}}$ $X(z) + 2z' X(z) + z^{2} X(z) = Y(z) - 0.75z' Y(z) + 0.125z^{2} Y(z)$ x(m) + 2 x(m-1) + x(m-2) = y(m) - 0.75 y(m-1) + 0.125 y(m-2)-y(n) = x(n) + 2x(n-1) + x(n-2) + 0.75 y(n-1) - 0.125 y(n-2)

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DIRECT FORM I



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DIRECT FORM II



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CASCADE & PARALLEL FORM

Cascade form :-

$$H(z) = \frac{1+2z'+z}{1-0.75z'}$$

 $= \frac{(1+z')}{(1+z')} \frac{(1+z')}{(1+z')}$
(1-0.5z') (1-2)
(1-0.5z') (1-2)
 $H(z) = \frac{1+2z'+z}{1-0.75z'+z}$
 $= 8+\frac{-7+8z}{1-0.75z'}$
 $= 8+\frac{18}{1-0.5z'}$

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CASCADE FORM



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PARALLEL FORM



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ASSESSMENT

- 1. Define block diagram.
- 2. Mention the structures to represent block diagram.
- 3. The system transfer function of LTI DT system is
- 4. List the summary of elementary blocks to represent discrete time systems.
- 5. Identify the difference equation:



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