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#### **DEPARTMENT OF MATHEMATICS** UNIT – IV FUNCTIONS OF SEVERAL VARIABLES

METHOD OF LAGRANGIAN'S MULTIPLIERS We can find an extreme value of the function f(x, y, 3) subject to the constrained y(x,y,3)=0 Define F(x,y,3) = 2 (x, y,3) + 2 g(x, y,3) where I is an undetermined constant called the Lagrangian multipliers. By solving the eqn.  $\frac{\partial F}{\partial x} = 0$ ,  $\frac{\partial F}{\partial y} = 0$ ,  $\frac{\partial F}{\partial z} = 0$ ,  $\frac{\partial F}{\partial y} = 0$ , we exper the Values of x, y, z and & Tusing & value find x, y, z, find the values of the maximum or minimum by substituting x, y, z in f(x, y, z). i) Find the minimum value of 22+ y2+ 32, yiven that an + by + C3 = P Let  $j = n^2 + y^2 + z^2$  and g = an + by + cz - pF(n,y,3)= Z(n,y,3)+ 7 g(n,y,3) = x2+y2+32+ > [an+by+c3-P]



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$$\begin{array}{l} \partial F = 2n + \alpha \gamma \\ \Rightarrow \partial F = 0 \Rightarrow 2n + \alpha \gamma = 0 \\ \Rightarrow n = - \frac{\lambda \alpha}{2} \\ \partial F = 2y + b \gamma \\ \Rightarrow \partial F = 0 \Rightarrow 2y + b \gamma = 0 \\ \Rightarrow y = - \frac{\lambda b}{2} \\ \partial F = 2\beta + c \gamma \\ \Rightarrow \partial F = 0 \Rightarrow 2\beta + c \gamma = 0 \\ \Rightarrow \beta = - \frac{\lambda c}{2} \\ \partial F = 0 \Rightarrow 2\beta + c \gamma = 0 \\ \Rightarrow \beta = - \frac{\lambda c}{2} \\ \partial F = 0 \Rightarrow 2\beta + c \gamma = 0 \\ \Rightarrow \beta = - \frac{\lambda c}{2} \\ \partial F = 0 \Rightarrow \alpha + by + c \gamma = p \\ = - \frac{\lambda c}{2} \int \alpha^2 + b^2 + c^2 \int \beta = p \\ = -\frac{\lambda c}{2} \int \alpha^2 + b^2 + c^2 \int \beta = p \\ = -\frac{\lambda c}{2} \int \alpha^2 + b^2 + c^2 \int \beta = p \\ = -\frac{\lambda c}{2} \int \alpha^2 + b^2 + c^2 \int \beta = p \\ = -\frac{\lambda c}{2} \int \alpha^2 + b^2 + c^2 \int \beta = p \\ = -\frac{\lambda c}{2} \int \alpha^2 + b^2 + c^2 \int \beta = p \\ = -\frac{\lambda c}{2} \int \alpha^2 + b^2 + c^2 \int \beta = p \\ = -\frac{\lambda c}{2} \int \alpha^2 + b^2 + c^2 \int \beta = p \\ = -\frac{\lambda c}{2} \int \alpha^2 + b^2 + c^2 \int \beta = p \\ = -\frac{\lambda c}{2} \int \alpha^2 + b^2 + c^2 \int \beta = p \\ = -\frac{\lambda c}{2} \int \alpha^2 + b^2 + c^2 \int \beta = p \\ = -\frac{\lambda c}{2} \int \alpha^2 + b^2 + c^2 \int \beta = p \\ = -\frac{\lambda c}{2} \int \alpha^2 + b^2 + c^2 \int \beta = p \\ = -\frac{\lambda c}{2} \int \alpha^2 + b^2 + c^2 \int \beta = p \\ = -\frac{\lambda c}{2} \int \alpha^2 + b^2 + c^2 \int \beta = p \\ = -\frac{\lambda c}{2} \int \alpha^2 + b^2 + c^2 \int \beta = p \\ = -\frac{\lambda c}{2} \int \alpha^2 + b^2 + c^2 \int \beta = p \\ = -\frac{\lambda c}{2} \int \alpha^2 + b^2 + c^2 \int \beta = p \\ = -\frac{\lambda c}{2} \int \alpha^2 + b^2 + c^2 \int \beta = p \\ = -\frac{\lambda c}{2} \int \alpha^2 + b^2 + c^2 \int \beta = p \\ = -\frac{\lambda c}{2} \int \alpha^2 + b^2 + c^2 \int \beta = p \\ = -\frac{\lambda c}{2} \int \beta + c^2 + b^2 + c^2 \int \beta = p \\ = -\frac{\lambda c}{2} \int \beta + c^2 + c^2$$



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 $\therefore n = -\frac{2}{2} = n = \frac{pa}{a^2 + b^2 + c^2}$  $y = -\frac{\lambda b}{\lambda^2} \implies y = \frac{pb}{\alpha^2 + b^2 + c^2}$  $3 = -\frac{\lambda c}{2} \implies 3 = \frac{pc}{\alpha^2 + b^2 + c^2}$ 3ub x, y, z in 2 $2 = x^2 + y^2 + z^2$  $= \left(\frac{pa}{a^{2}+b^{2}+c^{2}}\right)^{2} + \left(\frac{pb}{a^{2}+b^{2}+c^{2}}\right)^{2} + \left(\frac{pc}{a^{2}+b^{2}+c^{2}}\right)^{2}$  $= \frac{p^{2}(a^{2}+b^{2}+c^{2})^{2}}{(a^{2}+b^{2}+c^{2})^{2}}$  $=\frac{p^2}{a^2+b^2+c^2}$ 





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A sectangular box open at the top is to thave a  
volume of 32 cc. Final the dimension of the box,  
that require the least material for the construction.  
Let the dimension of the box be 
$$x, y, z$$
.  
Volume =  $xyz$ .  
Volume =  $2yz$ .  
Volume =  $2yz$ .  
Volume =  $2yz$ .  
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 $zzze = 2$ 



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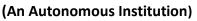


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(Dxn =) ny + 223 +. 7ny3 =0 (2) xy => xy + 2 yz + 2 xyz = 0 2713-243 =0 ⇒ ス= 9 Solve 223: 2 xy: xy+ 293+ 7xy 3=0 (3×3: 243+233+2743=0 24-232=0 ⇒ 4=23. ·· x=y=23 Sub? . n=y= 23 in ()  $2(+2(\frac{\alpha}{2})+3(2)(\frac{\alpha}{2})=0$  $n+x+\frac{3n^2}{2}=0$  $=) \frac{2\pi^2}{2} = -\pi\pi$ =) 2 = - 4/2







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#### DEPARTMENT OF MATHEMATICS **UNIT - IV FUNCTIONS OF SEVERAL VARIABLES**

Aub n=y= 23 in @ 2+23+ 2(23)=0 y+2 y+ 2 y.y =0 =) y = -4/3mb n= y= 23 h 3 24+27+274 =0 2(23)+2(23)+7(23)(23)=0 43+43+43=2=0 2+#37=0 => 3=-2/2 OF = 243-32 =) === =) >143 = 32 =)  $-\frac{4}{2} \times -\frac{4}{3} \times -\frac{2}{3} = 32$ ヨー1=ス ゆうカニー1. : n= 4, y=4, 3=2 ·· = ny+ 2y3+23n. = 4(4)+2(4)(2)+2(2)(4) = 16+16+16 = 48



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### DEPARTMENT OF MATHEMATICS UNIT – IV FUNCTIONS OF SEVERAL VARIABLES

Find the dimensions of the rectangeder box without top of mani capacity with surface ana 432 Squ. metre. Ans: 21= y = 23, 12, 12, 6. 2 = 864 cubic metics.