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# DEPARTMENT OF MATHEMATICS UNIT - IV INTERPOLATION, NUMERICAL DIFFERENTIATION & INTEGRATION

LAGRANGIAN INTERPOLATION

Let 
$$y=f(x)$$
 be a function which takes the values  $y_0, y_1, y_2, \dots, y_n$  corresponding to  $x_0, x_1, x_2, \dots, x_n$ .

Then Lagrangian interpolation form is  $y = f(x)$ 

$$= (x-x_1)(x-x_2) \cdot \dots (x-x_n) \quad y_0 + (x_0-x_1)(x_0-x_2) \cdot \dots (x-x_n) \quad y_1 + (x_1-x_0)(x_1-x_2) \cdot \dots (x_1-x_n)$$

$$= (x-x_0)(x-x_1) \cdot \dots (x_1-x_n) \quad y_1 + (x_1-x_0)(x_1-x_1) \cdot \dots (x_1-x_n)$$

Find the polynomial f(x) by using Lagrange's formula and hence find f(3) for





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$$\Re : 0 \quad 1 \quad 2.3.5$$

$$f(x) : 2 \quad 3 \quad 12 \quad 147$$

$$Soln: \quad \Re_0 = 0 \quad ; \quad \Re_0 = 2$$

$$\Re_1 = 1 \quad ; \quad \Re_1 = 3$$

$$\Re_2 = 2 \quad ; \quad \Re_2 = 12$$

$$\Re_3 = 5 \quad ; \quad \Re_3 = 147$$

By Lagrange's Interpolation Jornala, we have
$$y = \frac{1}{(\pi)} = \frac{(\pi - \chi_1)(\pi - \chi_2)(\pi - \chi_3)}{(\chi_0 - \chi_1)(\pi_0 - \chi_2)(\pi_0 - \chi_3)} y_0 + \frac{(\chi_1 - \chi_0)(\pi_1 - \chi_2)(\pi_1 - \chi_3)}{(\chi_1 - \chi_0)(\pi_1 - \chi_2)(\pi_1 - \chi_3)} y_1 + \frac{(\chi_1 - \chi_0)(\pi_1 - \chi_1)(\pi_1 - \chi_3)}{(\chi_2 - \chi_0)(\pi_2 - \chi_1)(\pi_2 - \chi_3)} y_2 + \frac{(\chi_1 - \chi_0)(\pi_1 - \chi_1)(\pi_2 - \chi_3)}{(\chi_3 - \chi_0)(\pi_3 - \chi_1)(\pi_3 - \chi_2)} y_3$$





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$$= \frac{(\varkappa-1)(\varkappa-2)(\varkappa-5)}{(0-1)(0-2)(0-5)} (2) + \frac{(\varkappa-0)(\varkappa-2)(\varkappa-5)}{(1-0)(1-2)(1-5)}$$

$$+ \frac{(\varkappa-0)(\varkappa-1)(\varkappa-5)}{(2-0)(2-1)(2-5)} (12) + \frac{(\varkappa-0)(\varkappa-1)(\varkappa-2)}{(5-0)(5-1)(5-2)} (147)$$

$$= (\varkappa-1)(\varkappa-2)(\varkappa-5) (2) + \varkappa(\varkappa-2)(\varkappa-5) (3)$$

$$= (\varkappa-1)(\varkappa-2)(\varkappa-5) (12) + \varkappa(\varkappa-1)(\varkappa-2) (147)$$

$$= \varkappa^{2} + \varkappa^{2} - \frac{6}{10}$$

$$= (3-1)(3-2)(3-5) (2) + \varkappa(3-1)(3-2) (3+5)$$

$$= (3-1)(3-5) (12) + \frac{3(3-1)(3-2)}{4} (3-2) (3+7)$$

$$= \frac{8}{10} - \frac{18}{4} + 24 + \frac{147}{60} = 35$$





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Find the missing been in the following table using Lagrange's intespolation. Solu: 31. 3 9 2-18

### INVERSE INTERPOLATION:

The process of finding a value of x jos the corresponding value of y is called inverse interpolation Inverse interpolation Jamula is

$$3(3^{2}-3^{2})(3^{2}-3^{2}) - - - (3^{2}-3^{2})$$

$$(3^{2}-3^{2})(3^{2}-3^{2}) - - - (3^{2}-3^{2})$$

$$(3^{2}-3^{2})(3^{2}-3^{2}) - - - (3^{2}-3^{2})$$

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) Find the age corresponding to the annuity value 13.6 yeven the table

Age (x): 38 35 40 45 50 Annuity valuely): 15.9 14.9 14.1 13.3 12.5

 $\chi = (y - y_1) * (y - y_2)(y - y_3)(y - y_4)$   $(y_0 - y_1) (y_0 - y_2) (y_0 - y_3) (y_0 - y_4)$   $(y_0 - y_1) (y_0 - y_2) (y_0 - y_3) (y_0 - y_4)$ (4-30) (4-31) (4-33) (4-74)  $(y_{1}-y_{2})(y_{1}-y_{2})(y_{1}-y_{3})(y_{1}-y_{4})$ (y-y<sub>0</sub>) (y-y<sub>1</sub>) (y-y<sub>3</sub>) (y-y<sub>6</sub>) (y2-40) (y2-41) (y2-43) (y2-44) (y-y0)(y-y1)(y-y2)(y-y4) x3+  $\frac{(y_{4}-y_{0})(y_{3}-y_{1})(y_{3}-y_{2})(y_{3}-y_{4})}{(y_{4}-y_{0})(y_{4}-y_{2})(y_{4}-y_{3})} \times_{4}$ 





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$$= \frac{(13.6 - 14.4)(13.6 - 14.1)(13.6 - 13.3)(13.6 - 12.5)}{(16.4 - 14.4)(15.4 - 14.1)(15.4 - 14.1)(15.4 - 12.5)} \times 30 + \frac{(13.6 - 15.4)(13.6 - 14.1)(13.6 - 13.3)(13.6 - 12.5)}{(14.4 - 15.4)(14.4 - 14.4)(13.6 - 13.3)(13.6 - 12.5)} \times 35 + \frac{(13.6 - 15.4)(13.6 - 14.4)(13.6 - 13.3)(13.6 - 12.5)}{(14.1 - 15.4)(14.1 - 14.4)(14.1 - 13.3)(14.1 - 12.5)} \times 40 + \frac{(13.6 - 15.4)(13.6 - 14.4)(13.6 - 14.1)(13.6 - 12.5)}{(13.6 - 15.4)(13.6 - 14.4)(13.6 - 14.1)(13.6 - 13.3)} \times 45 + \frac{(13.6 - 15.4)(13.6 - 14.4)(13.6 - 13.3)}{(13.6 - 15.4)(13.6 - 14.1)(13.6 - 13.3)} \times 50 + \frac{(13.5 - 15.4)(13.5 - 14.4)(13.5 - 14.1)(13.5 - 14.3)}{(13.5 - 15.4)(13.5 - 14.4)(13.5 - 14.3)}$$