



# **SNS COLLEGE OF TECHNOLOGY**

**Coimbatore-35  
An Autonomous Institution**

Accredited by NBA – AICTE and Accredited by NAAC – UGC with 'A+' Grade  
Approved by AICTE, New Delhi & Affiliated to Anna University, Chennai



## **DEPARTMENT OF INFORMATION TECHNOLOGY**

### **16IT302 – DESIGN AND ANALYSIS OF ALGORITHMS**

**III YEAR V SEM**

**UNIT-I-Introduction**

**TOPIC: Fundamentals of the Analysis of Algorithm Efficiency – Analysis Framework**

**Prepared by  
T.Shanmugapriya,AP/IT**



# FUNDAMENTALS OF THE ANALYSIS OF ALGORITHM EFFICIENCY – ANALYSIS FRAMEWORK



Subject :Design and Analysis of Algorithm  
Unit :I

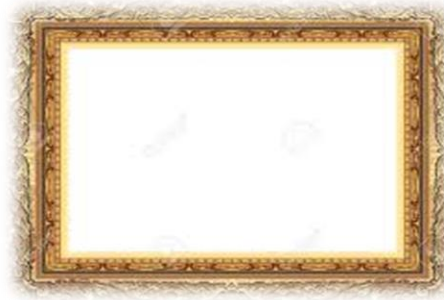




# Connection-to identify the topic from given image



**Answer: Analysis Framework**





# Fundamentals of the Analysis of Algorithm Efficiency



- Analysis Framework
- Asymptotic Notations and its properties
- Mathematical analysis for Recursive algorithms.
- Mathematical analysis for Non recursive algorithms.

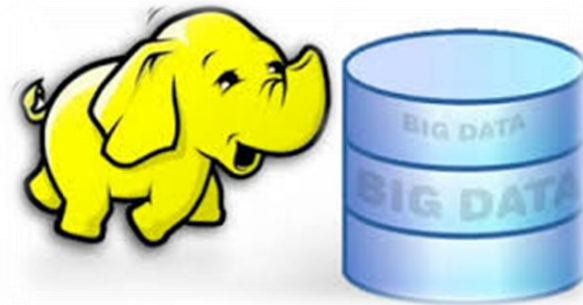




# Analysis Framework

There are two kinds of efficiencies to analyze the efficiency of any algorithm. They are:

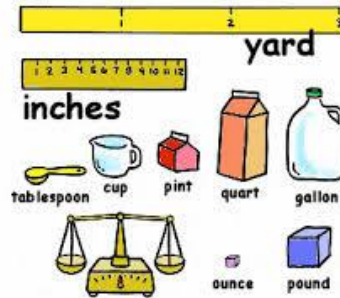
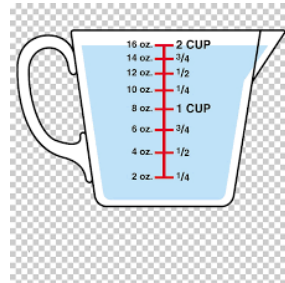
- *Time efficiency*, indicating how fast the algorithm runs, and
- *Space efficiency*, indicating how much extra memory it uses





**The algorithm analysis framework consists of the following:**

- Measuring an Input's Size
- Units for Measuring Running Time
- Orders of Growth
- Worst-Case, Best-Case, and Average-Case Efficiencies





# Orders of Growth



- A **difference in running times on small inputs** is not what really distinguishes efficient algorithms from inefficient ones.
- For example, the greatest common divisor of two small numbers, it is not immediately clear how much more efficient Euclid's algorithm is compared to the other algorithms, the difference in **algorithm efficiencies becomes clear** for larger numbers only.





# Worst-Case, Best-Case, and Average-Case Efficiencies



Consider Sequential Search algorithm some search key  $K$  **ALGORITHM** *SequentialSearch*( $A[0..n - 1], K$ )

//Searches for a given value in a given array by sequential search

//Input: An array  $A[0..n - 1]$  and a search key  $K$

//Output: The index of the first element in  $A$  that matches  $K$  or -1 if there are no matching elements

$i \leftarrow 0$

**while**  $i < n$  **and**  $A[i] \neq K$  **do**

$i \leftarrow i + 1$

**if**  $i < n$  **return**  $i$

**else return** -1

Clearly, the running time of this algorithm can be quite different for the same list size  $n$ .







# Worst-Case, Best-Case, and Average-Case Efficiencies

## *Worst-case efficiency:-*

- The *worst-case efficiency* of an algorithm is its efficiency for the worst case input of size  $n$ .
- The algorithm runs the longest among all possible inputs of that size.
- For the input of size  $n$ , the running time is  $C_{worst}(n) = n$ .

## *Best case efficiency*

- The *best-case efficiency* of an algorithm is its efficiency for the best case input of size  $n$ .
- The algorithm runs the fastest among all possible inputs of that size  $n$ .
- In sequential search, If we search a first element in list of size  $n$ . (*i.e.* first element equal to a search key), then the running time is

$$C_{best}(n) = 1.$$





# Worst-Case, Best-Case, and Average-Case Efficiencies



## *Average case efficiency*

- The Average case efficiency lies **between best case and worst case**.
- To analyze the algorithm's average case efficiency, we must make some assumptions about possible inputs of size  $n$ .

The standard assumptions are that

- The probability of a successful search is equal to  $p$  ( $0 \leq p \leq 1$ ) and
- The probability of the first match occurring in the  $i$ th position of the list is the same for every  $i$ .





# Assessment



**1. Two main measures for the efficiency of an algorithm are**

- A. Processor and memory
- B. Complexity and capacity
- C. Time and space
- D. Data and space

**2. Which of the following case does not exist in complexity theory?**

- A. Best case
- B. Worst case
- C. Average case
- D. Null case





Thank you!

