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DEPARTMENT OF MATHEMATICS

UNIT-I

DESIGN OF EXPERIMENTS

Experiment : A collection of data or measurements of some features of an object.

Treatments : Various objects of Comparison in a Comparative experiment are called theatments.

Experimental unit: The Smallest division of the experimental material to which we apply the Greatments.

Blocks: The whole experimental anits dre divided into Subgroups called blocks.

Experimental error: It is the error occured due to random Causes or chance causes or non-assignable factors which are beyond own control.

Basic principles of experimental design

- 1. Randomisation
- 2. Replication
- 3. Local control

Basic Designs of experiment

- 1. Completely Randomised Design (C.R.D Or one-way classification)
- 2. Randomised Block Design (R.B.D or Two-way classification)
- 3. Latin square Design (L.S.D or Three way classification)

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Analysis of Variance (ANOVA)

The analysis of variance is a widely used technique developed by Prof. R.A. Fisher.

Uses : It is used to test whether the means of a number of populations (more than two) are equal. Assumptions:

1. Each sample taken is a standom sample

2. Each one is independent of the other sample.

- 3. Populations from which samples are taken are normal.
- 4. Variances of the populations are equal.

Completely Randomised Design (One-way classification):

This is a one factor experiment.

procedure :

Step1 :

Null hypothesis : Ho : There is no significante difference between columns and errors.

Alternative hypothesis: H,: There is a significant difference between columns and errors.

Step 2 :

* Find N, number of given observation

- * Find T, total number of observation
- $\pm Find correction factor C = \frac{T^2}{N}$

Step 3 : Find :

* Mecone sum of squares of treatments $SST = \sum x_1^2 + \sum x_2^2 + \sum x_3^2 + \cdots - C.F$



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+ Sum of Squares of columns

$$SSC = \frac{(\Sigma X_1)^2}{c_1} + \frac{(\Sigma X_2)^2}{c_2} + \frac{(\Sigma X_3)^2}{c_3} + \dots - C.F$$

A Sum of Squares of errors

Stop 4 : ANOVA Table :

Source of Variation	Degree of freedom	Sum of Squares	Mean Sum of Squares	Variance ratio	Таые value
Between Columns	C-1	SSC	$MSC = \frac{SSC}{C-1}$	MSC (or) MSE	F _x (c-1, N-c) (or)
Between Errors	N-c	SSE	$MSE = \frac{SSE}{N-C}$	MSE MSC	E(N-C,C-1)

Step 5: Decision :

If Since $|F| < F_{x}$, we accept the hypothesis $|F| > F_{x}$, we reject the hypothesis.

Problem :

① A Aandom Sample is selected from each of these makes of ropes and their breaking strength are measured with the following results. Test whether the breaking strength of the ropes differ significantly.

	I	I	TT		
	70	100	60		
	72	110	65		
and the second second second	75	108	57		
	80	112	84	na Basaran Tanan	
	83	120	87		
	69	107	73	0.000	

16MA202-Statistics & Numerical Methods

P.GOMATHI/AP/MATHEMATICS



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Solution :

Step 1: Null hypothesis " Ho : There is no significant difference between Column and errors Accomptive hypothesis : H, : There is a significant

difference between column and evers

Step 2:

$$N = 18$$

 $T = 1576$
 $C \cdot F = T^{2}/N = \frac{1576^{2}}{18} = 137987.55$

Step 3:

			-					~		-
CC	T	-	5 %	+	5 %.	+	2 %		C.I	-
20		A					-			

X_1 X_2 X_3 X_1^2 X_2^2 X_3^2 70100504900100003600721106551841210042257510857562511664324980112846400125444056831138768891276975691071071144005329380770426289988492631028						
70 180 60 4700 1800 4225 72 110 65 5184 12100 4225 75 108 57 5625 11664 3249 80 112 84 6400 12544 7056 83 113 87 6889 12769 7569 83 113 87 6889 12769 7569 120 73 14400 5329 107 11449 5329	×,	≈_	×3	×,2	x, ^e	× 5
75 108 57 5625 11664 3249 80 112 84 6400 12544 7056 83 113 87 6889 12769 7569 83 113 87 6889 12769 7569 120 73 14400 5329 107 107 11449	70	100	60	4900	10000	3600
80 112 84 6400 12544 7056 83 113 87 6889 12769 7569 120 73 14400 5329 107 11449	72	110	65	5184	12100	4225
83 113 87 6889 12769 7569 120 73 14400 5329 107 11449	75	108	57	5625	11664	3249
83 113 120 73 14400 5329 107 11449	80	112	84	6400	12544	7056
120 73 14400 5329 107 11449	83	113	87	6889	1	
10 7		120	73		1	5329
380 770 426 28998 84926 31028		107			11449	
	380	770	42.6	28 998	84926	31028

SST = 28998 + 84926 + 31028 - 137987.55 = 6964.45

$$SSC = \frac{(5x_1)^2}{c_1} + \frac{(5x_2)^2}{c_2} + \frac{(5x_3)^2}{c_3} - C.F$$

= $\frac{(380)^2}{5} + \frac{(770)^2}{7} + \frac{(426)^2}{6} - 137987.55$
SSC = 587.8



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55 t - 55 t - 55 t

= 6964.45 - 58 36.44

SSE = 1126.01

Stop 4 : ANOVA Lable :

Source of Variation	Degree of freedom	Sum of Squares	Mean sum of sevuares	Variance Vatio	Table Value
Between Columns	c -1 = 3-1 = 2	95C = 5838.44	MSC = <u>SSC</u> C-1 = 2919.22	1 -	Fx (2,15 + 3.68
Between Errors	N-C = 18-3 = 15	SSE = 11 26.01	MSE = <u>SSE</u> N-C = 75.067		

Steps: Decision:

Since F>F, we reject the hypothesis.

... There is a significant difference between columns

and errors.

