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(An Autonomous Institution)
Coimbatore – 641 035
DEPARTMENT OF MATHEMATICS
UNIT-1 PROBABILITY AND RANDOM VARIABLES



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Conditional probability:

The Conditional probability of an event B assuming that the event A has happened, is defined as,

$$P(B|A) = \frac{P(A\cap B)}{P(A)}$$
, provided $P(A) \neq 0$

Similarly,

$$P(A|B) = \frac{P(A \cap B)}{P(B)}$$
, provided $P(B) \neq 0$

Theorem:

If A and B are independent, then prove that

- 1. A and B are independent
- 2. A and B are independent
- 3. A and B are independent.

$$I \cdot P(\overline{A} \cap B) = P(\overline{A}) \cdot P(B)$$

Consider,

B = (ANB) U (ANB)

P(B) = P [(ANB) U (ANB)]

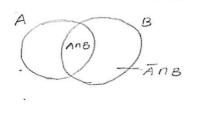
$$P(B) = P(A \cap B) + P(A \cap B)$$

$$= P(B) - P(A) P(B)$$

$$= P(B) [I - P(A)]$$

$$P(\overline{A} \cap B) = P(B) \cdot P(\overline{A})$$

. A and B are independent



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2. $P(A \cap \overline{B}) = P(A) \cdot P(\overline{B})$

Consider,

$$P(A \cap B) = P(A) - P(A \cap B)$$

$$= P(A) - P(A)P(B)$$

$$= P(A) [1 - P(B)]$$

$$P(AnB) = P(A) P(B)$$

P(An B) = P(A) P(B) . A and B are independen

3. P(AnB) = P(A).P(B)

Consider,

= I - P(AUB)

$$= 1 - \left[P(A) + P(B) - P(A \cap B) \right]$$

$$= 1 - \left[P(A) + P(B) - P(A) \cdot P(B) \right]$$

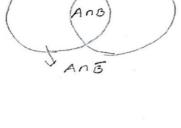
$$= 1 - P(A) - P(B) + P(A) \cdot P(B)$$

$$= P(\overline{A}) - P(B) \left[I - P(A) \right]$$

$$= P(\overline{A}) - P(B) \cdot P(\overline{A})$$

$$P(\bar{A} \cap \bar{B}) = P(\bar{A}) P(\bar{B})$$

A and B are independent.



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$$= P(\overline{A}) - P(B) P(\overline{A})$$

$$= P(\overline{A}) [1 - P(B)]$$

$$P(\overline{A} \cap \overline{B}) = P(\overline{A}) P(\overline{B})$$
Hence \overline{A} and \overline{B} are independent.

Hence proved

J. A bag containe 3 Red and 1 white balls. Two balls are drawn without leplacement. Two balls are drawn without both balls are what is the probability that both balls are led?

Soln:

Deauting a Red ball in the 1st dian is

$$P(\overline{A}) = \frac{3C_1}{7C_1} = \frac{3}{7}$$

that first deawn is Red bout = P(B/A)

:
$$P(B/A) = \frac{2C_1}{6C_1} = \frac{1}{3}$$

we know that

$$P(B|A) = \frac{P(A)B}{P(A)}$$

$$P(AnB) = P(B|A) P(A)$$

$$= \frac{3}{7}$$

$$P(AnB) = \frac{1}{7}$$

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