

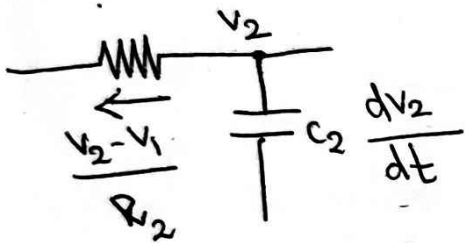
* At node 1 by kirchoff's current law

$$\frac{V_1}{R_1} + C_1 \frac{dV_1}{dt} + \frac{V_1 - V_2}{R_2} = \frac{e}{R_1}$$

* on taking laplace transform of above eqn with zero initial conditions

$$\frac{V_1(s)}{R_1} + C_1 s V_1(s) + \frac{V_1(s)}{R_2} - \frac{V_2(s)}{R_2} = \frac{E(s)}{R_1}$$

$$V_1(s) \left[\frac{1}{R_1} + s C_1 + \frac{1}{R_2} \right] - \frac{V_2(s)}{R_2} = \frac{E(s)}{R_1} \rightarrow (1)$$



* At node 2 by kirchoff's current law

$$\frac{V_2 - V_1}{R_2} + C_2 \frac{dV_2}{dt} = 0$$

* Apply Laplace transform with zero initial conditions.

$$\frac{V_2(s)}{R_2} - \frac{V_1(s)}{R_2} + C_2 s V_2(s) = 0$$

$$\frac{V_2(s)}{R_2} = \frac{V_1(s)}{R_2} + C_2 s V_2(s) = \left[\frac{1}{R_2} + s C_2 \right] V_2(s)$$

$$\therefore V_1(s) = [1 + s C_2 R_2] V_2(s) \rightarrow (2)$$

Sub for $V_1(s)$ from eqn (2) in eqn (1) we get

$$(1 + s R_2 C_2) V_2(s) \left[\frac{1}{R_1} + s C_1 + \frac{1}{R_2} \right] - \frac{V_2(s)}{R_2} = \frac{E(s)}{R_1}$$

$$\left[\frac{(1 + s R_2 C_2) (R_2 + R_1 + s C_1 R_1 R_2) - R_1}{R_1 R_2} \right] V_2(s) = \frac{E(s)}{R_1}$$

Transfer function :-

$$\frac{V_2(s)}{E(s)} = \frac{R_2}{[(1 + s R_2 C_2) (R_1 + R_2 + s C_1 R_1 R_2) - R_1]}$$