UNIT II – Brute Force and Divide and Conquer

• Brute Force Design Technique

- Selection Sort
- Bubble Sort

- Sequential Search

- Closest pair and Convex hull problem
- Travelling Salesman problem
- Knapsack problem
- Assignment problem

Sequential Search – Traditional method

- Worst case O(n) element not found/ search element is in last position of list
- Best case O(1) element found at 1st position

*

• Average case – element found at mid position of the list

```
#include<stdio.h>
void main()
Ł
    int a[100], n, i;
    printf("\n enter the array elements");
    scanf("%d",&n);
    for(i=0;i<n;i++)</pre>
    Ł
        scanf("%d",&a[i]);
    printf("\n enter the element to search");
    scanf("%d", &n);
    printf("\n searching");
    for(i=0;i<n;i++)</pre>
        if(a[i]==n)
            printf("\n Element found %d at position %d",a[i],i+1);
             exit(0);
```

Sequential Search

• Extra trick in implementing sequential search – append the search element to the last position in the list

55	60	70	32	23	89	32
A[0]	A[1]	A[2]	A[3]	A[4]	A[5]	Search key A[n]

ALGORITHM SequentialSearch2(A[0..n], K)

```
//Implements sequential search with a search key as a sentinel

//Input: An array A of n elements and a search key K

//Output: The index of the first element in A[0.n - 1] whose value is

// equal to K or -1 if no such element is found

A[n] \leftarrow K

i \leftarrow 0

while A[i] \neq K do

i \leftarrow i + 1

if i < n return i

else return -1
```

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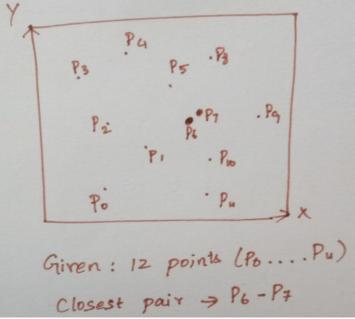
Closest pair problem

- Geometric problem
- Straight forward approach Finite set of points in the plane
- Applications : computational geometry and operations research
- Google map- nearby restaurants
- *Problem statement: find the two closest points in a set of points*
- <u>Solution:</u>

- Assumption:
 - 2-dimensional space
 - (x,y) Cartesian coordinates
 - Distance between 2 points $P_i = (x_i, y_i)$, $P_j = (x_j, y_j)$ Euclidean distance

$$d(p_i, p_j) = \sqrt{(x_i - x_j)^2 + (y_i - y_j)^2}.$$

Closest pair problem



ALGORITHM BruteForceClosestPair(P)

*

//Finds distance between two closest points in the plane by brute force //Input: A list P of n ($n \ge 2$) points $p_1(x_1, y_1), \ldots, p_n(x_n, y_n)$ //Output: The distance between the closest pair of points $d \leftarrow \infty$ for $i \leftarrow 1$ to n - 1 do for $j \leftarrow i + 1$ to n do $d \leftarrow \min(d, sqrt((x_i - x_j)^2 + (y_i - y_j)^2))$ //sqrt is square root return d

Analysis of Closest-pair problem

1.Problem size : n
2.Basic operation : Euclidean Distance
3.Count of basic operation-----→
4.Efficiency – worst case

DAA-UNIT II-M

Chocket pair problem = Count of basic operation

$$C(n) = \sum_{l=1}^{n-1} \sum_{j=l+1}^{n} 2$$

$$= 2 \sum_{l=1}^{n-1} \sum_{j=l+1}^{n} 1$$

$$= 2 \sum_{l=1}^{n-1} (n-(l+1)+1)$$

$$= 2 \sum_{l=1}^{n-1} (n-(l+1)+1)$$

$$= 2 \left[n \left(\sum_{l=1}^{n-1} 1\right) - \left(\sum_{l=1}^{n-1} \frac{1}{2}\right)\right]$$

$$= 2 \left[n \left(\sum_{l=1}^{n-1} 1\right) - \left(\sum_{l=1}^{n-1} \frac{1}{2}\right)\right]$$

$$= 2 \left[n (n-1) - \frac{n(n-1)}{2}\right]$$

$$= 2 \left[n (n-1) - \frac{n(n-1)}{2}\right]$$

$$= 2 \left[n (n-1) - \frac{n(n-1)}{2}\right]$$

$$= 2 (n^{2} - n) - n^{2} + n$$

$$= 2 n^{2} - 2n - n + n$$

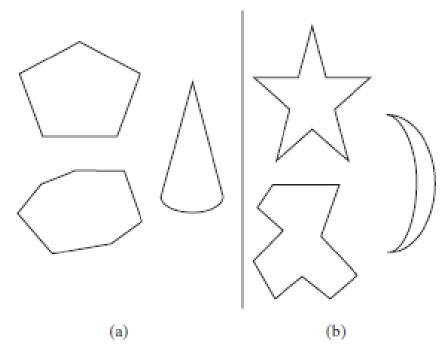
$$= 2 n^{2} - 2n - n + n$$

$$= (n-1)n \in O(n^{2})$$

$$= 2 (n^{2} - 1)n \in O(n^{2})$$

$$= 2 (n^{2} - 1)n \in O(n^{2})$$

Convex Hull



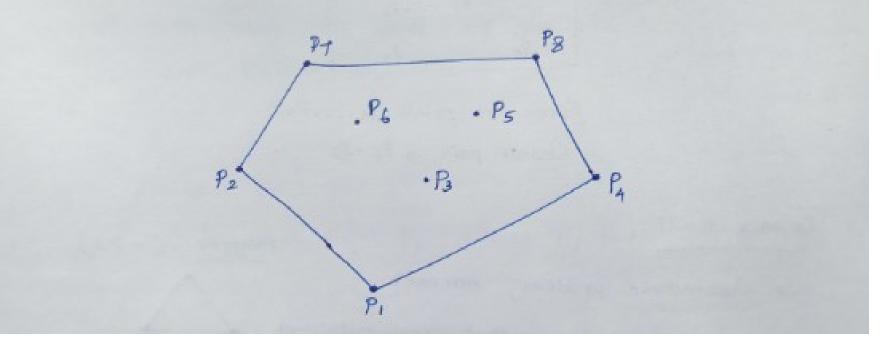
(a) Convex sets. (b) Sets that are not convex.

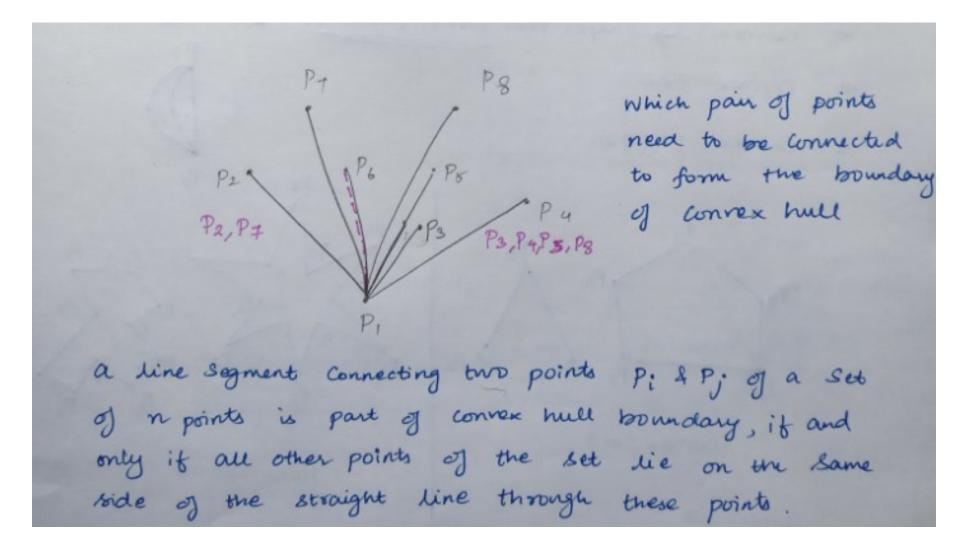
Comex Hull polygon (n>2) -* Geometric problem, Aircraft. Convex -> Shapes that cure outward + Convex Set * Convex polygon P3 86 P2 Convex Sets Not Convex (Curre inward) Convex Set Set of points in the plane is called convex, if for any two points P& a in set, the entire line segment with the endpoints at P & a belongs to the set.

Convex hull of Set S of points is the Smallest convex Set Containing S.

* Convex polygon -> Vertices. -> extreme points

Should not be a middle point of any line segment





Straigne line - 2 points
$$(x_1, y_1)$$
 (x_2, y_2)
 $ax + by - C$
Here $a = y_2 - y_1$
 $b = x_2 - x_2$
 $c = x_1y_2 - y_1x_2$
all points above the line $\Rightarrow ax + by > C$
 $all points below the line $\Rightarrow ax + by < c$ $for P_1, P_2$
 $for each point P_1$
 $for each point P_1$
 $for each point P_1$
 $for each point P_1$
 $for all other points P_k (P_k # P_1 + P_1)$
 $for all other points P_k is on one side of$
 $line segment, 3$
 P_1, P_2 (boundary of correx hull)$

Convex Hull - Analysis

- Input size n (set of points)
- Basic operation
- Count of basic operation $-O(n^3)$
- Worst case