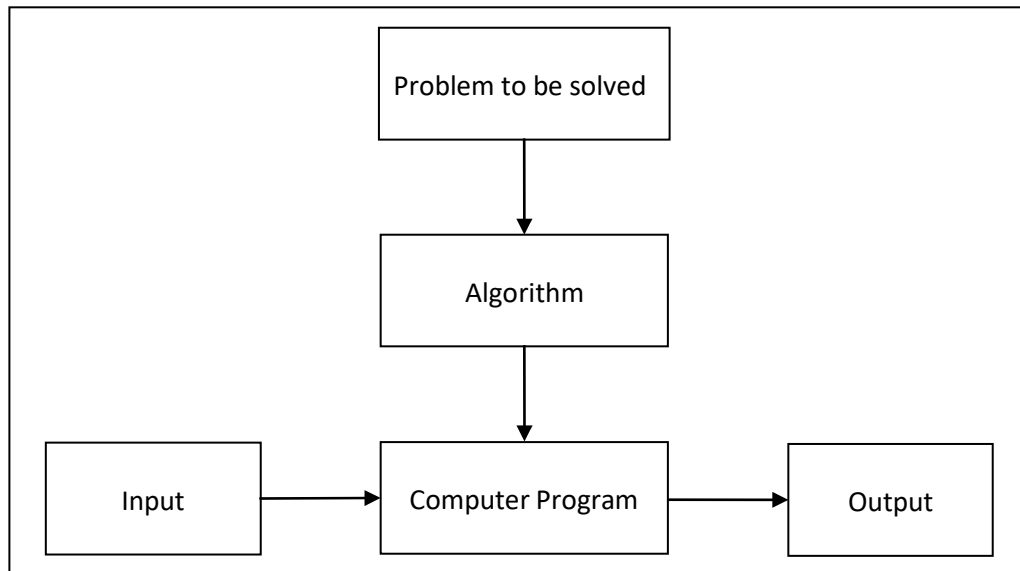


## UNIT I INTRODUCTION

### 1.1 NOTION OF AN ALGORITHM

An *algorithm* is a sequence of unambiguous instructions for solving a problem, i.e., for obtaining a required output for any legitimate input in a finite amount of time.



**FIGURE 1.1** The notion of the algorithm.

It is a step by step procedure with the input to solve the problem in a finite amount of time to obtain the required output.

#### **The notion of the algorithm illustrates some important points:**

- The non-ambiguity requirement for each step of an algorithm cannot be compromised.
- The range of inputs for which an algorithm works has to be specified carefully.
- The same algorithm can be represented in several different ways.
- There may exist several algorithms for solving the same problem.
- Algorithms for the same problem can be based on very different ideas and can solve the problem with dramatically different speeds.

#### **Characteristics of an algorithm:**

**Input:** Zero / more quantities are externally supplied.

**Output:** At least one quantity is produced.

**Definiteness:** Each instruction is clear and unambiguous.

**Finiteness:** If the instructions of an algorithm is traced then for all cases the algorithm must terminate after a finite number of steps.

**Efficiency:** Every instruction must be very basic and runs in short time.

### Steps for writing an algorithm:

1. An algorithm is a procedure. It has two parts; the first part is **head** and the second part is **body**.
2. The Head section consists of keyword **Algorithm** and Name of the algorithm with parameter list. E.g. Algorithm name1(p1, p2,...,p3)  
The head section also has the following:  
**//Problem Description:**  
**//Input:**  
**//Output:**
3. In the body of an algorithm various programming constructs like **if, for, while** and somestements like assignments are used.
4. The compound statements may be enclosed with { and } brackets. **if, for, while** can beclosed by **endif, endfor, endwhile** respectively. Proper indention is must for block.
5. Comments are written using // at the beginning.
6. The **identifier** should begin by a letter and not by digit. It contains alpha numeric lettersafter first letter. No need to mention data types.
7. The left arrow “←” used as assignment operator. E.g.  $v \leftarrow 10$
8. **Boolean** operators (TRUE, FALSE), **Logical** operators (AND, OR, NOT) and **Relational** operators (<, <=, >, >=, =, ≠, <>) are also used.
9. Input and Output can be done using **read** and **write**.
10. **Array[], if then else condition, branch** and **loop** can be also used in algorithm.

### Example:

The greatest common divisor(GCD) of two nonnegative integers  $m$  and  $n$  (not-both-zero), denoted  $\text{gcd}(m, n)$ , is defined as the largest integer that divides both  $m$  and  $n$  evenly, i.e., with a remainder of zero.

**Euclid's algorithm** is based on applying repeatedly the equality  $\text{gcd}(m, n) = \text{gcd}(n, m \bmod n)$ , where  $m \bmod n$  is the remainder of the division of  $m$  by  $n$ , until  $m \bmod n$  is equal to 0. Since  $\text{gcd}(m, 0) = m$ , the last value of  $m$  is also the greatest common divisor of the initial  $m$  and  $n$ .

$\text{gcd}(60, 24)$  can be computed as follows: $\text{gcd}(60, 24) = \text{gcd}(24, 12) = \text{gcd}(12, 0) = 12$ .

### Euclid's algorithm for computing $\text{gcd}(m, n)$ in simple steps

**Step 1** If  $n = 0$ , return the value of  $m$  as the answer and stop; otherwise, proceed to Step 2.

**Step 2** Divide  $m$  by  $n$  and assign the value of the remainder to  $r$ .

**Step 3** Assign the value of  $n$  to  $m$  and the value of  $r$  to  $n$ . Go to Step 1.

### Euclid's algorithm for computing $\text{gcd}(m, n)$ expressed in pseudocode

**ALGORITHM** *Euclid\_gcd(m, n)*

```
//Computes gcd( $m$ ,  $n$ ) by Euclid's algorithm
//Input: Two nonnegative, not-both-zero integers  $m$  and  $n$ 
//Output: Greatest common divisor of  $m$  and  $n$ 
while  $n \neq 0$  do
     $r$ 
     $\leftarrow m$ 
    mod
     $n$ 
     $m \leftarrow$ 
     $n$ 
     $n \leftarrow r$ 
return  $m$ 
```