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SNS College of Technology, Coimbatore-35.<br>(An Autonomous Institution)<br>Internal Assessment -III<br>Academic Year 2022-2023(Odd)<br>Third Semester<br>Department of Mathematics<br>19MAT201- Transforms and Partial Differential Equations

Time: $\mathbf{1 . 3 0}$ Hours
Maximum Marks: 50

| PART-A (5 $\times 2=10$ MARKS $)$ ANSWER ALL QUESTIONS |  |  |  | BLooms |
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| 1. |  | Find the nature of pde $3 u_{x x}+4 u_{x y}+6 u_{y y}-2 u_{x}-u=0$ | CO4 | (Rem) |
| 2. |  | What are the various possible solutions of one dimensional heat equations? | CO4 | (Und) |
| 3. |  | A rod 10 cm long has its ends A and B kept at $20^{\circ} \mathrm{c}$ and $70^{\circ} \mathrm{C}$ respectively until steady state conditions prevail. Find the steady temperature in the rod. | CO4 | (App) |
| 4. |  | Form the Difference Equation $y=A 2^{n}$ | CO5 | (App) |
| 5. |  | State the initial and finial value theorem | CO5 | (App) |
| PART -B ( $\mathbf{1 3 + 1 3 + 1 4 = 4 0 ~ M A R K S ) ~}$ ANSWER ALL QUESTIONS |  |  |  |  |
| 6. | a) | A rod of length 30 cm has its ends A and B kept at $20^{\circ} \mathrm{C}$ and $80^{\circ} \mathrm{C}$ until steady state conditions prevail. The temperature at each end is then suddenly reduced to $0^{\circ} \mathrm{C}$ and kept so. Find the resulting temperature function $\mathrm{u}(\mathrm{x}, \mathrm{t}) \mathrm{x}=0$ at A . | CO4 | (App) <br> (13) |
|  |  | (or) |  |  |
|  | b) | A tightly stretched string with fixed end points $x=0$ and $x=1$ is initially at rest in its equilibrium position. If its set vibrating string giving each point a velocity $y=\lambda x(l-x)$. Find the displacement of any point on the string at a distance of x from one end at a time t . | CO4 | (App) <br> (13) |


| 7. | a) | Solve the difference equation using z transform $y_{n+2}+6 y_{n+1}+9 y_{n}=2^{n} \text { given that } y_{0}=y_{1}=0$ | CO5 | $\begin{gathered} (\mathrm{App}) \\ (13) \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: |
|  |  | (or) |  |  |
|  | b) i) <br> ii) | Find $z(\cos a t)$ and $z($ sinat $)$ Using convolution theorem find $Z^{-1}\left[\frac{z^{2}}{(z-a)(z-b)}\right]$ | $\begin{aligned} & \mathrm{CO} 5 \\ & \mathrm{CO} \end{aligned}$ | (Ana) <br> (7) <br> (App) <br> (6) |
| 8. | a) i) | A string is stretched and fastened at two points $\mathrm{x}=0$ and $\mathrm{x}=1$ apart. Motion is started by displacing the string into the form $y=k\left(l x-x^{2}\right)$ from which it is released at time $t=0$. Find the displacement of any point on the string at a distance of $x$ from one end at a time $t$. | CO4 | $\begin{gathered} \text { (App) } \\ 14 \end{gathered}$ |
|  |  | (or) |  |  |
|  | b) i) <br> ii) | Find $z^{-1}\left[\frac{z^{2}}{(z+2)\left(z^{2}+4\right)}\right]$ using Partial fraction method <br> Elaborate the applications of Z-Transform in real life Engineering and Industry fields. | $\begin{aligned} & \mathrm{CO} 5 \\ & \mathrm{CO} 5 \end{aligned}$ | (Ana) <br> (7) <br> (App) <br> (7) |

