



SNS College of Technology, Coimbatore-35. (An Autonomous Institution) Internal Assessment -III Academic Year 2022-2023(Odd) Third Semester Department of Mathematics 19MAT201- Transforms and Partial Differential Equations



## Time: 1.30 Hours

## Maximum Marks: 50

| PART – A (5 x 2 = 10 MARKS)<br>ANSWER ALL QUESTIONS   |    |   |     |               |
|---|----|---|-----|---------------|
| 1.  |    | Find the nature of pde $3u_{xx}+4u_{xy}+6u_{yy}-2u_x-u=0$   | CO4 | (Rem)         |
| 2.  |    | What are the various possible solutions of one dimensional heat equations?  | CO4 | (Und)         |
| 3.  |    | A rod 10 cm long has its ends A and B kept at 20 °c and 70 °c respectively until steady state conditions prevail. Find the steady temperature in the rod.   | CO4 | (App)         |
| 4.  |    | Form the Difference Equation $y = A2^n$   | CO5 | (App)         |
| 5.  |    | State the initial and finial value theorem  | CO5 | (App)         |
| PART -B (13+13+14 = 40 MARKS)<br>ANSWER ALL QUESTIONS |    |   |     |               |
| 6.  | a) | A rod of length 30cm has its ends A and B kept at 20°C and 80 °C until steady state conditions prevail. The temperature at each end is then suddenly reduced to 0°C and kept so. Find the resulting temperature function $u(x, t) x=0$ at A.  | CO4 | (App)<br>(13) |
|   |    | (or)  |     |               |
|   | b) | A tightly stretched string with fixed end points x=0 and x=1 is<br>initially at rest in its equilibrium position. If its set vibrating string<br>giving each point a velocity $y = \lambda x(l - x)$ . Find the displacement of<br>any point on the string at a distance of x from one end at a time t. | CO4 | (App)<br>(13) |

| 7. | a)    | Solve the difference equation using z transform  |     |               |
|----|-------|--|-----|---------------|
|    |       | $y_{n+2} + 6y_{n+1} + 9y_n = 2^n$ given that $y_0 = y_1 = 0$   | CO5 | (App)<br>(13) |
|    |       | (or)   |     |               |
|    | b) i) | Find $z(cosat)$ and $z(sinat)$   | CO5 | (Ana)<br>(7)  |
|    | ii)   | Using convolution theorem find $Z^{-1}\left[\frac{z^2}{(z-a)(z-b)}\right]$   | CO5 | (App)<br>(6)  |
| 8. | a) i) | A string is stretched and fastened at two points x=0 and x=1 apart.<br>Motion is started by displacing the string into the form $y = k(lx - x^2)$ from which it is released at time t = 0. Find the displacement of any point on the string at a distance of x from one end at a time t. | CO4 | (App)<br>14   |
|    |       | (or)   |     |               |
|    | b) i) | Find $z^{-1}\left[\frac{z^2}{(z+2)(z^2+4)}\right]$ using Partial fraction method   | CO5 | (Ana)<br>(7)  |
|    | ii)   | Elaborate the applications of Z-Transform in real life Engineering<br>and Industry fields.   | CO5 | (App)<br>(7)  |
|    |       |  |     | (7            |

**Rem/Und:** Remember/ Understand App: Apply Ana: Analyze Eva: Evaluate Cre: Create