

SNS COLLEGE OF TECHNOLOGY

(An Autonomous Institution)



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DEPARTMENT OF MATHEMATICS

UNIT-I

MATRICES

Characteristic Equations:

Let A be a given matrix.

Let à be a Scalar.

The equation $|A-\lambda I|=0$ is called the Characteristic equation of the matrix A.

Note:

* For any Savuare matrix A, the Sum of the eigen Values of a matrix is equal to trace of the matrix.

* For a 2x2 matrix, the characteristic equation is,

$$\lambda^2 - c_1 \lambda + c_2 = 0$$

where $C_1 = Sum$ of the main diagonal elements $C_2 = |A|$

* For a 3x3 matrix, the characteristic equation is,

$$\lambda^3 - c, \lambda^2 + c_2 \lambda - c_3 = 0$$

where C, = Sum of the main diagonal elements

Cz = Sum of the minors of the main diagonal elements

C3 = 1A1.



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PROBLEMS :

① Find the Characteristic equation of
$$\begin{pmatrix} 1 & 2 \\ 0 & 2 \end{pmatrix}$$

Solution: Let
$$A = \begin{pmatrix} 1 & 2 \\ 0 & 2 \end{pmatrix}$$

The Characteristic equation is,

$$\lambda^2 - c_1 \lambda + c_2 = 0 \rightarrow 0$$

$$C_1 = 1 + 2 = 3$$

$$C_2 = \begin{bmatrix} 1 & 2 \\ 0 & 2 \end{bmatrix} = 2$$

subs C, & C2 in 10,

$$\lambda^2 - 3\lambda + 2 = 0$$

2) Find the Characteristic equation of
$$\begin{pmatrix} 2 & -3 & 1 \\ 3 & 1 & 3 \end{pmatrix}$$

Solution:

Let $A = \begin{pmatrix} 2 & -3 & 1 \\ 3 & 1 & 3 \end{pmatrix}$

The Characteristic equation is,

$$\lambda^3 - c_1 \lambda^2 + c_2 \lambda - c_3 = 0 \longrightarrow \bigcirc$$

$$C_1 = 2 + 1 - 4 = -1$$

$$C_2 = \begin{vmatrix} 1 & 3 \\ 2 & -4 \end{vmatrix} + \begin{vmatrix} 2 & 1 \\ -5 & -4 \end{vmatrix} + \begin{vmatrix} 2 & -3 \\ 3 & 1 \end{vmatrix}$$

$$= -10 - 3 + 11 = -2$$

$$C_3 = \begin{vmatrix} 2 & -3 & 1 \\ 3 & 1 & 3 \\ -5 & 2 & -4 \end{vmatrix} = 0$$



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Subs
$$C_1, C_2 \ \ \ \ \ C_3$$
 in \bigcirc ,
$$\lambda^3 + \lambda^2 - 2 \ \lambda = 0$$

Problems:

Find the Characteristic polynomial of

$$\begin{pmatrix} 11 & -4 & -7 \\ 7 & -2 & -5 \end{pmatrix} \qquad \stackrel{\text{Soln}}{=} : \lambda^3 - 3\lambda^3 + 2\lambda = 0$$

(5)
$$\begin{pmatrix} 1 & 1 & 3 \\ 1 & 5 & 1 \\ 3 & 1 & 1 \end{pmatrix}$$
 $\frac{3}{200}: \lambda^3 - 7\lambda^2 + 36 = 0$