

IMAGE RECONSTRUCTION IN COMPUTED TOMOGRAPHY

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MSC. RADIO- IMAGING TECHNOLOGY (FINAL YEAR)

INTRODUCTION TO COMPUTED TOMOGRAPHY

- ▶ Computed tomography was invented in 1972 by British engineer Godfrey Hounsfield of EMI laboratories, England and by South African born physicist Allan Cormack of Tufts University, Massachusetts.
- ▶ The term “computed tomography” (CT) or Computed Axial Tomography (CAT), refers to a computerized x-ray imaging procedure in which a narrow beam of x-rays is aimed at a patient and quickly rotated around the body, producing signals that are detected by series of detectors which are processed by machine’s computer to generate cross sectional images or “slices” of the body.
- ▶ CT is based on the fundamental principle that the density of tissue passed by x-ray beam can be measured from calculation of attenuation coefficient.
- ▶ The first CT scanner was installed between 1974 and 1976.
- ▶ Over time many improvements are done in speed, patients comfort and resolution.

GENERATIONS OF CT

- ▶ **1ST Generation** - X-ray tube and two detectors are connected and move together by translation and then rotation, pencil beam used.
- ▶ **2ND Generation** - Multiple detectors (around 30) arranged in a row, Translation and rotation movement, fan beam used.
- ▶ **3RD Generation** - Multiple detectors (30° - 40° arc) arranged in row, complete rotation of tube and detectors around the patient, 30° - 40° arc.
- ▶ **4TH Generation** - The rotating x-ray tube is positioned within stationary, circular array of detectors.
- ▶ **5TH Generation** - EBCT scanner
- ▶ **6TH Generation** -
- ▶ **7TH Generation** -

STEPS FOR CT IMAGE FORMATION

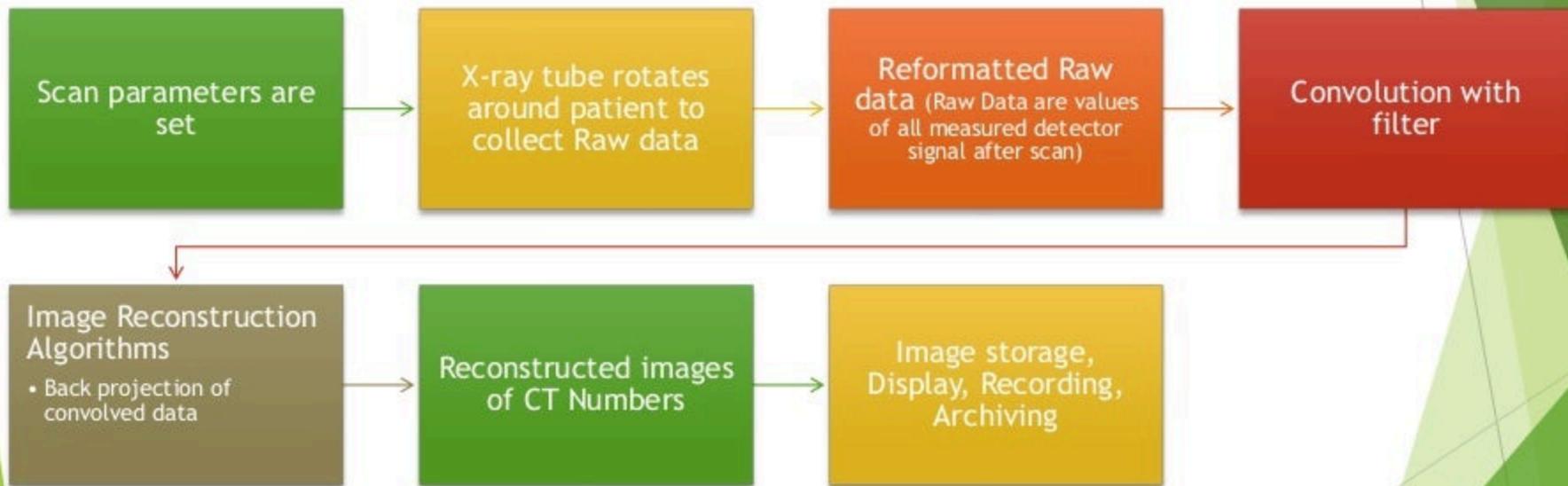
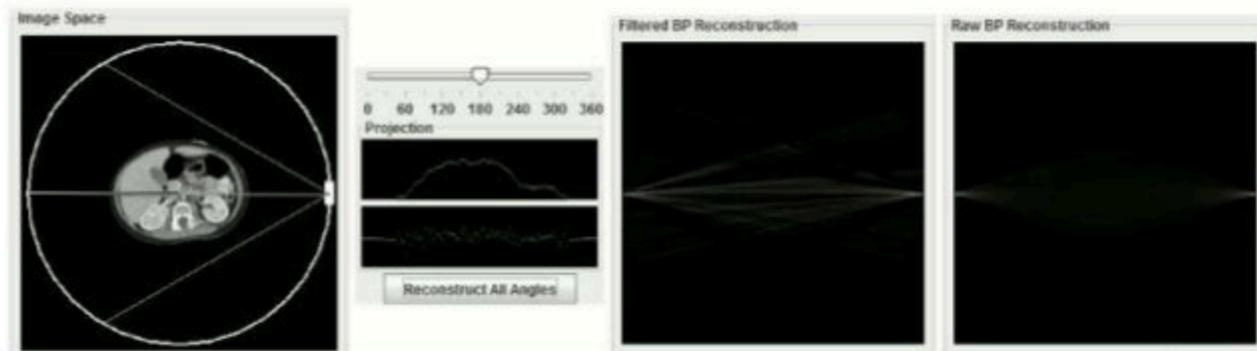


IMAGE RECONSTRUCTION

- ▶ Image reconstruction is a mathematical process that generates tomographic images from x-ray projection data acquired at many different angles around the patient.
- ▶ The reconstruction process is based on use of an algorithm that uses the attenuation data measured by detectors to systematically build up the image for viewing and interpretation.
- ▶ Image reconstruction has fundamental impacts on image quality and radiation dose.



BASIC TERMS

ALGORITHMS

- ▶ Defined as “set of rules or directions for getting a specific output from specific input”.
- ▶ Algorithm must always terminate after a finite number of steps.
- ▶ Algorithms can be represented in form of Flow chart, listing the series of Steps combined altogether by programming language like C++, Java etc. to form a software to do a specific job.
- ▶ CT reconstruction algorithms converts each attenuation coefficient values obtained splits it into intensity and location at object, Forming an image with specific grayscale.

IMAGE DOMAIN

► Images can be represented in two domain on the basis of how they are acquired.

a) SPATIAL LOCATION DOMAIN

All images displayed for viewing by humans are in spatial location domain. I.e. General radiography and CT acquire images in spatial domain.

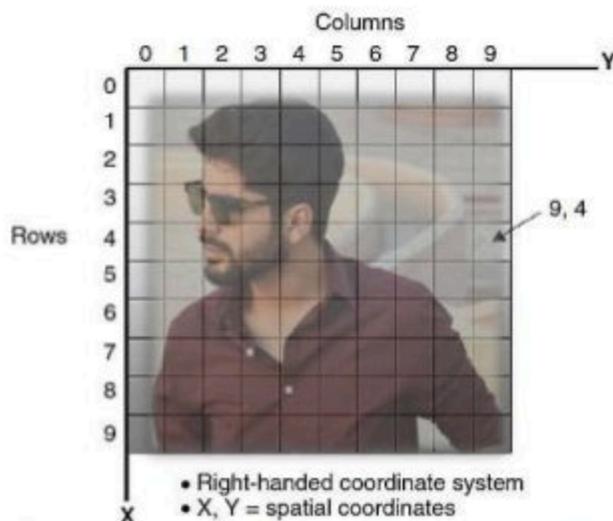


FIGURE 3-7 A right-handed coordinate system used to describe digital images in the spatial location domain. The exact location of a pixel can be found using columns and rows.

b) FREQUENCY DOMAIN

Images can also be acquired in spatial frequency domain i.e. MRI

Small structures within a Object produce higher frequencies that represent detail in image, large structure produces low frequencies and represent contrast information in image.

Represented as wave, number of signal changes per unit length

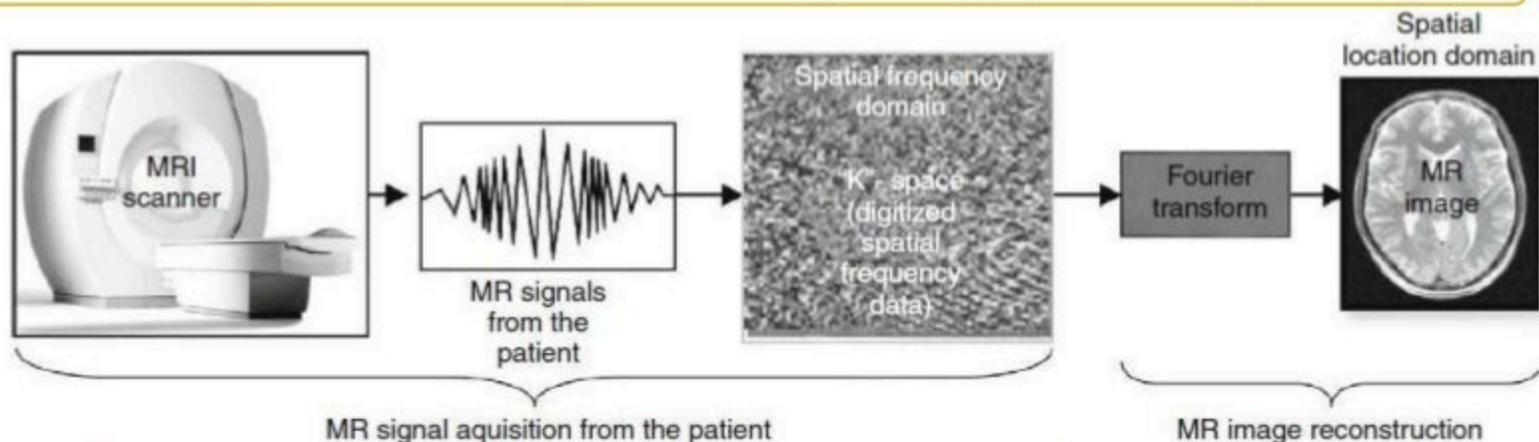
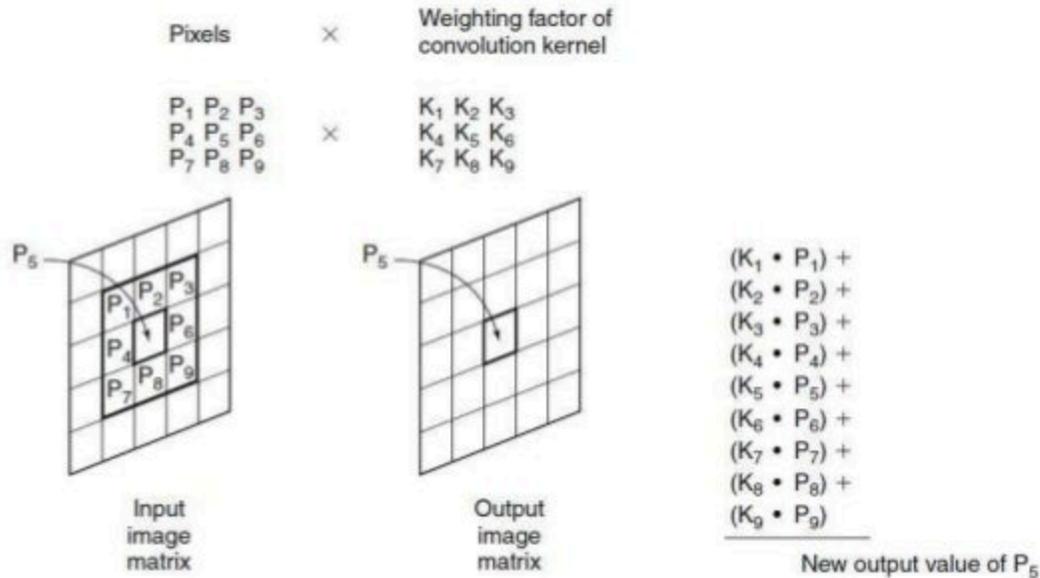


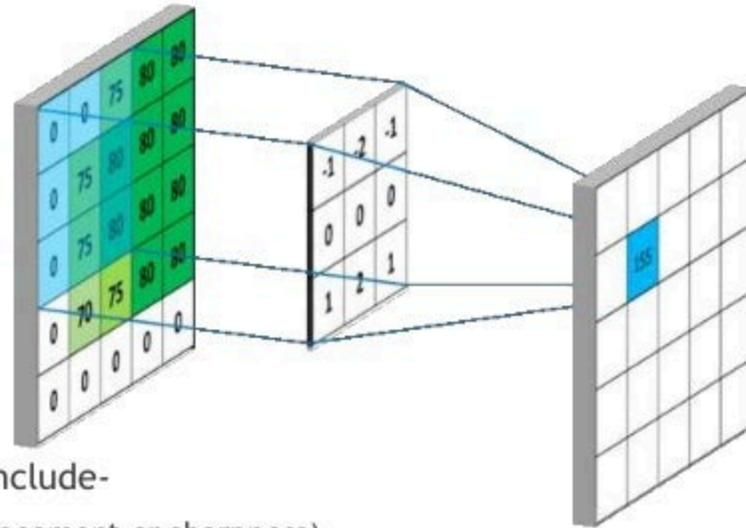
FIGURE 3-26 The major processes of MRI signal acquisition to image display. First, magnetic resonance (MR) signals are acquired from the patient, who is placed in the magnet during the imaging procedure. These signals are high and low frequencies collected from the patient. The signals are subsequently digitized and stored in what is referred to as “k” space, a frequency domain space. (Image courtesy Philips Medical Systems.)

CONVOLUTION

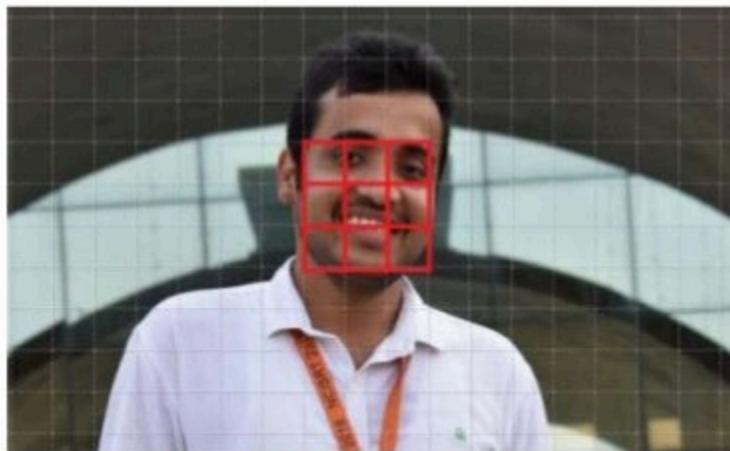
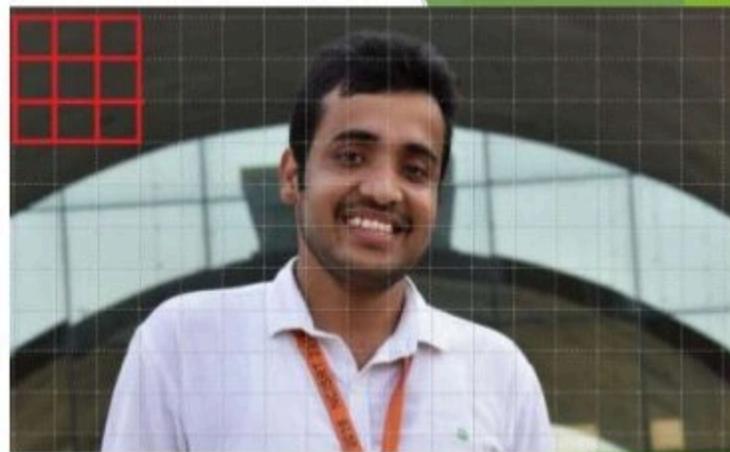
- ▶ Convolution is a mathematical way of combining two signals to form third signal. i.e. Convolution kernel and input image to form output image.
- ▶ The value of output pixel depends on a group of pixel in input image that surround the input pixel in interest.
- ▶ Convolution Kernel or mask is basically the average pixel weightage of Specific number of Pixel. Generally, 3 X 3 size kernel is used.



- ▶ During convolution, the kernel moves across the image pixel by pixel. Each pixel in input image, its surrounding and kernel are used to compute the value of corresponding output pixel.

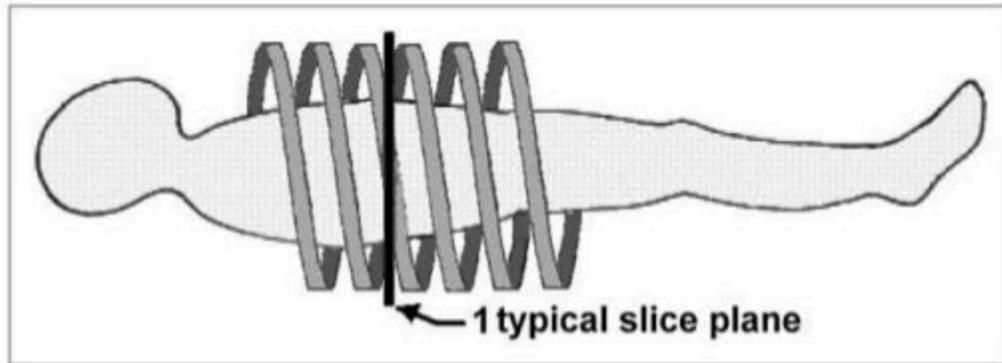


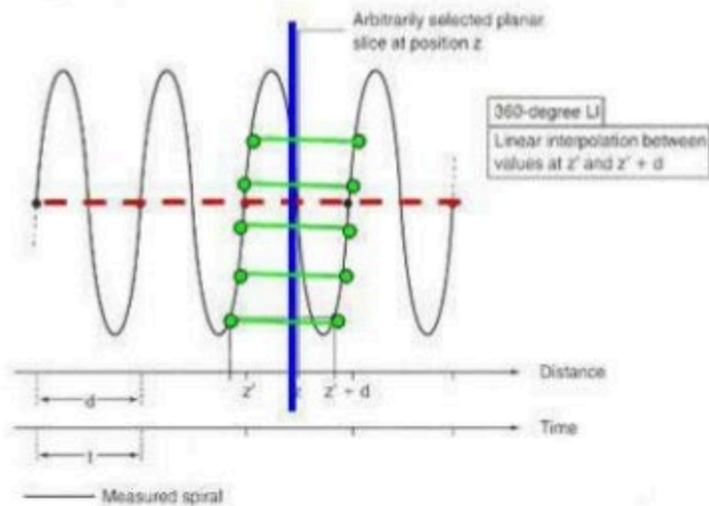
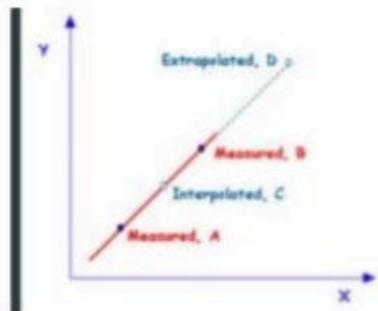
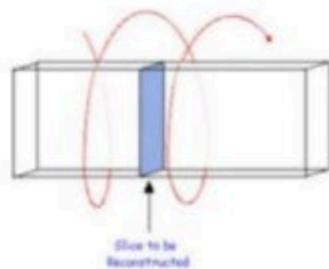
- ▶ Various convolution filters include-
 - ▶ High pass filter (Edge enhancement or sharpness)
 - ▶ Low pass filter (smoothing)
 - ▶ Un sharp masking (Image restoration)



INTERPOLATION

- ▶ Estimation of unknown value between known values is called interpolation technique.
- ▶ Used in spiral CT images reconstruction.
- ▶ A transverse planer image can be reconstructed at any position along the axis of patient.
- ▶ Interpolation can be used in frequency domain to re-grid the radial sampling to uniform sampling.
- ▶ Image interpolation creates a number of new slices between known slices in order to obtain isotropic volume image.





Interpolation process

TYPES OF IMAGE RECONSTRUCTION

1. Simple Back projection
2. Iterative method
3. Analytic method
 - I. Fourier reconstruction algorithms
 - II. Filtered back projections

1. SIMPLE BACK PROJECTION METHOD

- ▶ Also called as “summation method” or “linear superposition method” first used by Oldendorf (1961), Khul and Edwards (1963).
- ▶ Not used in commercial CT scanners.
- ▶ This involves "smearing back" the projection across the image at the angle it was acquired.
- ▶ Rays from two or more projections are superimposed or back projected they produce a crude reproduction of original object.
- ▶ Some produced images are ‘starred’ and ‘blurred’ that makes it unsuitable for medical diagnosis.
- ▶ In order to reconstruct the image 180° data is required with fan beam angle. The remaining 180° are the mirror of first. (It does not matter which way a photon travels through tissue, it will be attenuated the same amount)

- Can be best explained with a Graphical or numerical approach.

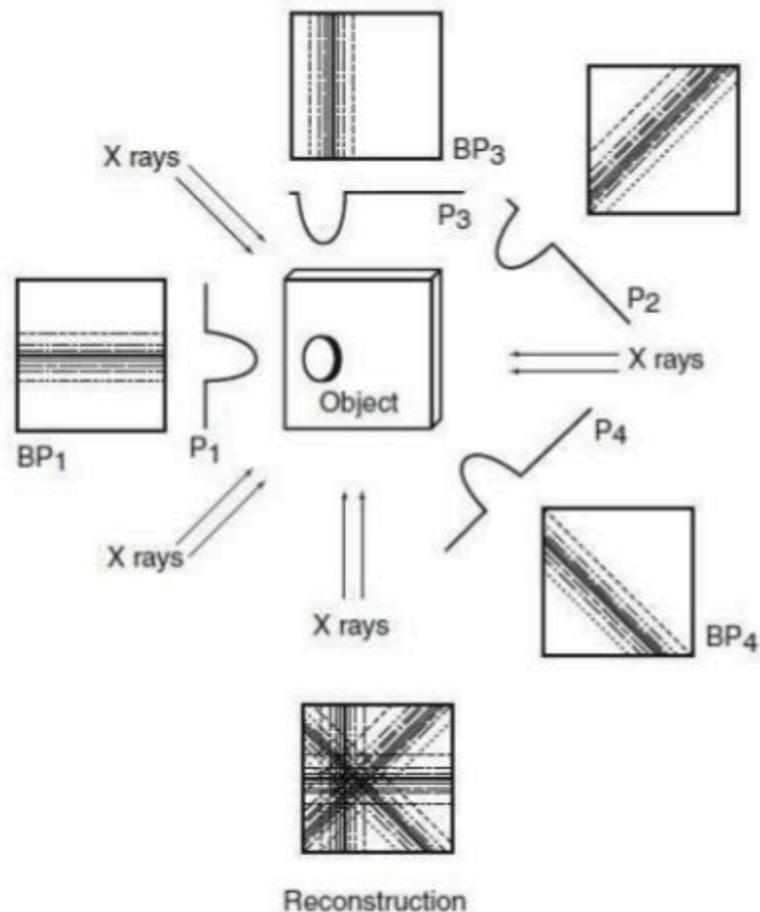
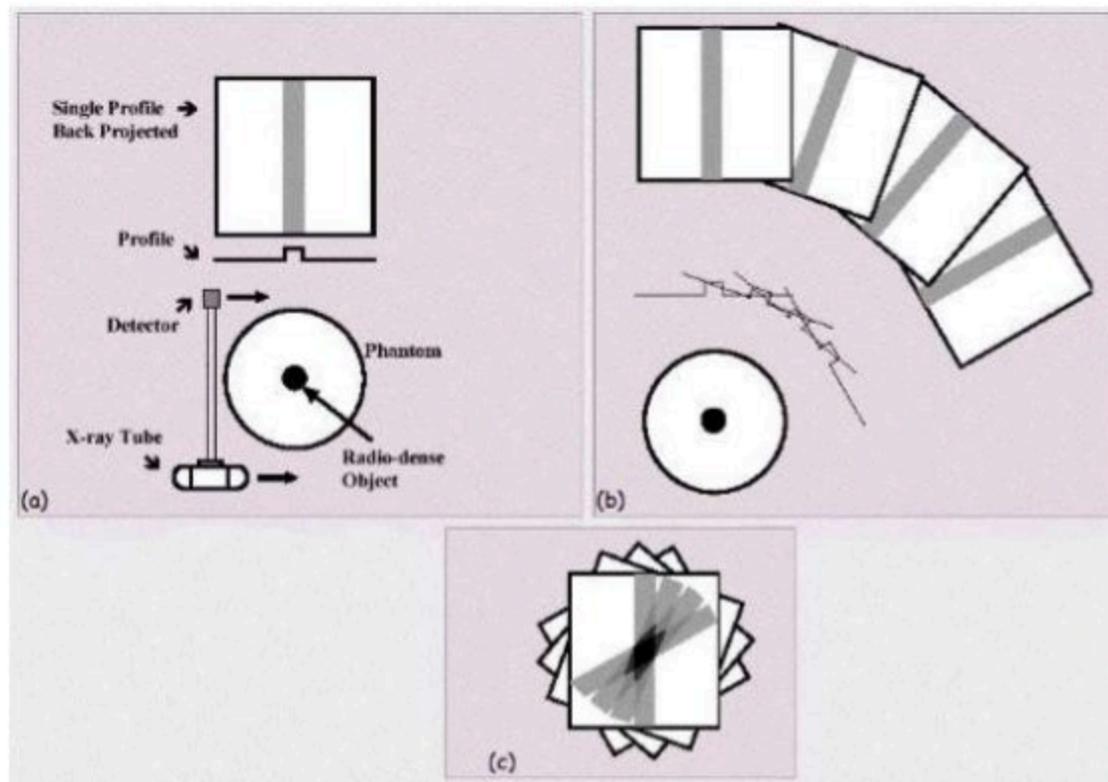


Fig : Graphical representation of Back projection Reconstruction Technique

3	2	0 degree		45 degree	0 degree		45 degree		90 degree	
1		↓	↓		1	5	1 (0+1)	8 (5+3)	3	10
	2	0	2	90degree	1	5	4 (1+3)	8 (5+3)	8	12
	4	1	3							
0		1	5			0	2	0	6	6
3	3			135 degree	1	3	3	9	9	15
Projected Data					Divided by common divisor 3		subtract Constant value 6		135 degree	
1, 5, 0, 3, 3, 2, 4, 2, 3, 1										

Fig : Mathematical representation of Back projection Reconstruction Technique

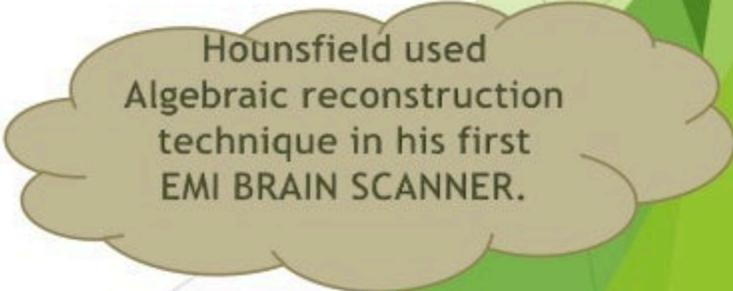
- ▶ Problem with back projection includes mainly severe blurring in computed images.



Appearance of star like structure

2. Iterative reconstruction

- ▶ Successful approximation method.
- ▶ An iterative reconstruction starts with an assumption (all points in matrix have same value) and compares this assumption with measured value, make corrections to bring two into agreement and repeats the process over and over again until assumed and measured value are same or within acceptable limits'.
- ▶ Techniques includes:-
 - ▶ Simultaneous iterative reconstruction technique
 - ▶ Iterative least square technique
 - ▶ Algebraic reconstruction technique.



Hounsfield used Algebraic reconstruction technique in his first EMI BRAIN SCANNER.

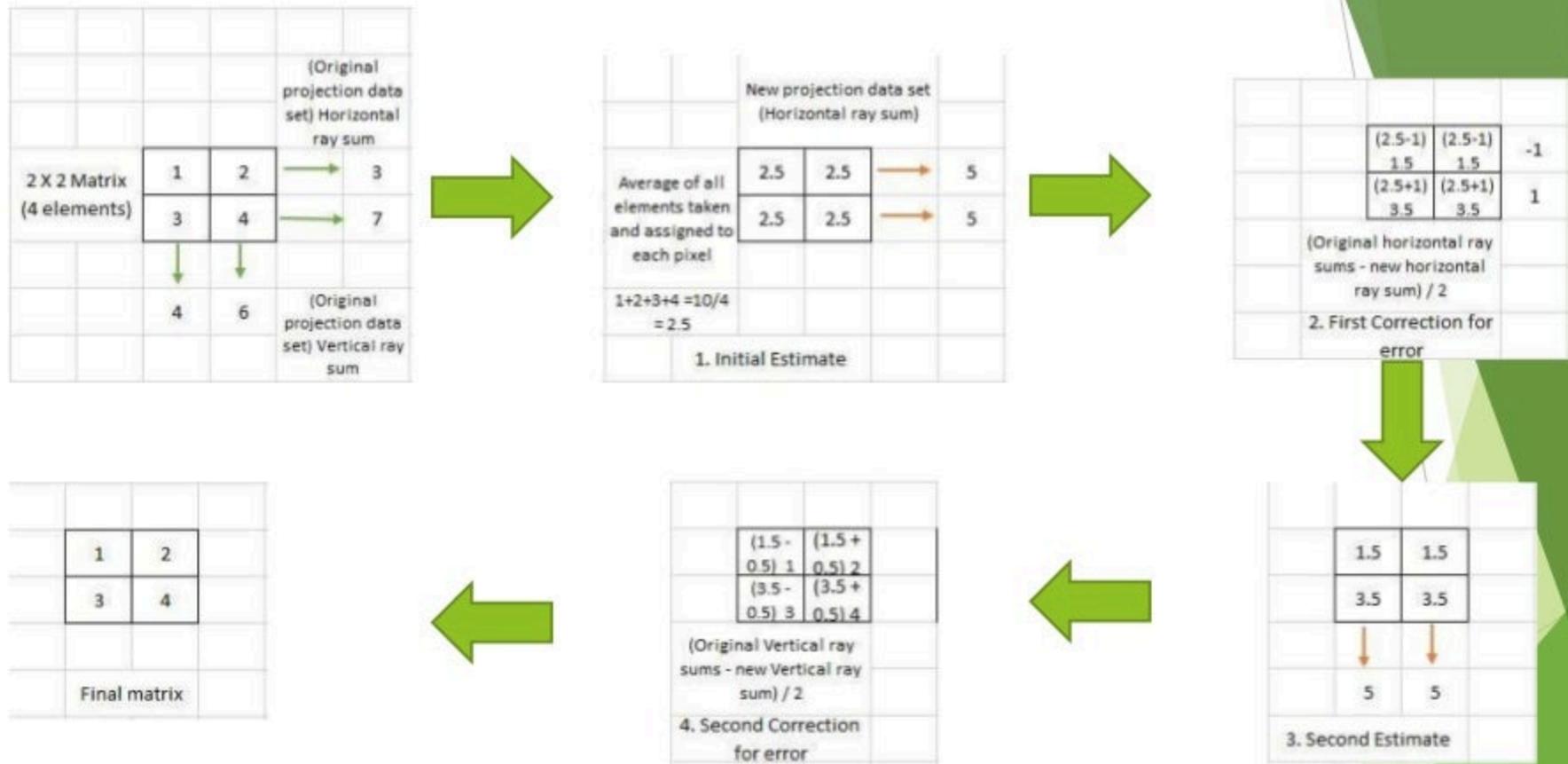


Fig : Mathematical representation of Iterative Reconstruction Technique

Limitations of iterative reconstruction method

- ▶ Difficult to obtain accurate ray sum because of quantum noise and patient motion.
- ▶ Takes too long to generate the reconstructed image because the iteration can be done only after all projection data sets have been obtained.

3. Analytical method

- ▶ Current commercial scanner uses this method
- ▶ A mathematical technique known as Convolution or filtering is used.
- ▶ Technique employs a spatial filter to remove blurring artifacts.
- ▶ Two major types-
 1. Filtered back projection
 2. Fourier Reconstruction Algorithms

1. Filtered back projection

- ▶ Filtered back projection is also referred as Convolution method.
- ▶ The projection profile is filtered to remove the typical star like blurring that is characteristic of simple back projection.

All projection profiles are obtained.

Logarithm of data is obtained.

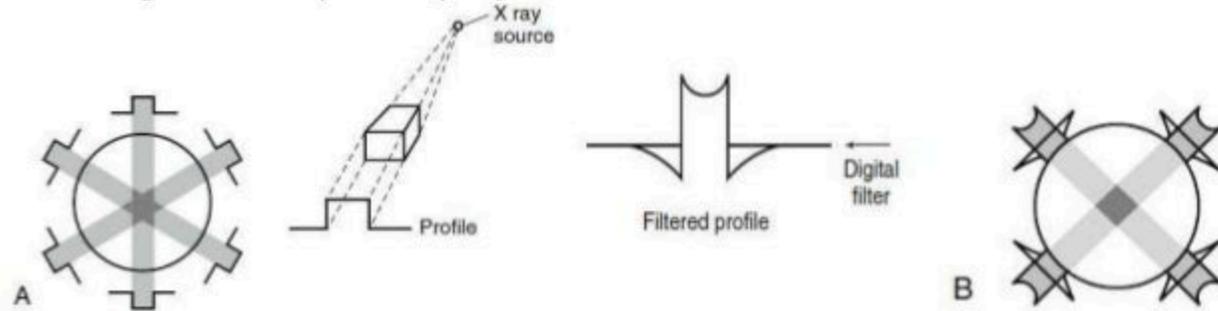
Logarithmic data are multiplied by digital filter to generate a set of filtered profile.

Filtered profile are back projected.

Filtered projections are summed and -ve & +ve components are then cancelled. Image free of blurring obtained.

Fig : Flowchart showing steps in filtered back projection

- ▶ Filtering refers to altering the projection data before we do the back-projections.
- ▶ This type of filter picks up sharp edges within the projection (and thus, in the underlying slice) and tends to ignore flat areas. Because the high pass filter actually creates negative pixels at the edges, it subtracts out the extra smearing caused by back projection.



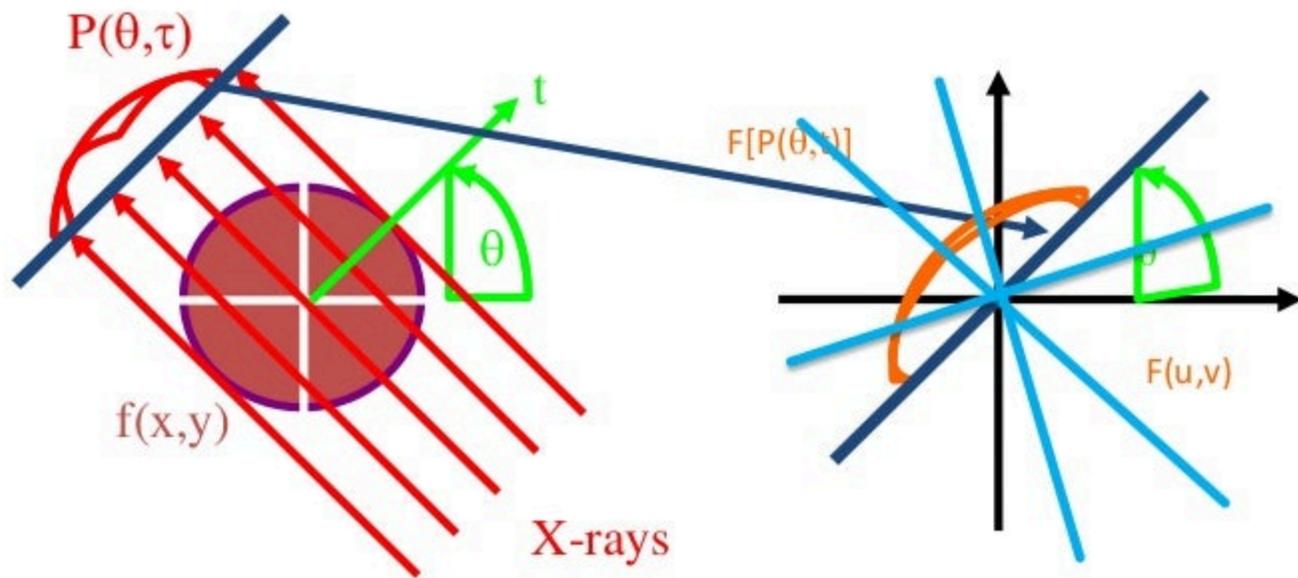
- ▶ The optimal way of eliminating the star like pattern is by use of Ramp filter.
- ▶ Ramp filter has the effect of filtering out low frequencies and passing high frequencies, with a linear behaviour in between. Thus with this filter, contrasting features (high-frequencies) are accentuated, while blurring (low-frequencies) is minimized.
- ▶ The combination of ramp filter and back projection is filtered back projection.

2. Fourier Reconstruction Algorithms

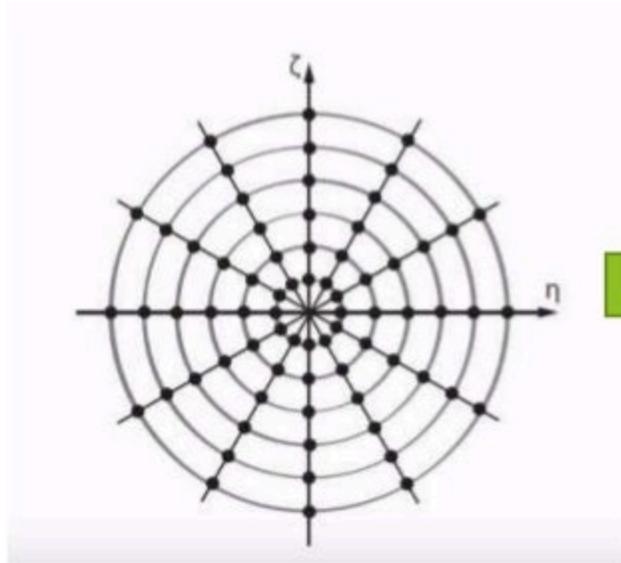
- ▶ A property of Fourier transform.
- ▶ Relates the projection data in spatial location domain to spatial frequency domain.
- ▶ Used in MRI image reconstruction.
- ▶ Unlike filtered back projection, this algorithm does not use any filtering as interpolation does the work of rearranging the image components in rectangular grid.
- ▶ Based on Fourier Slice Theorem.

Fourier Slice Theorem

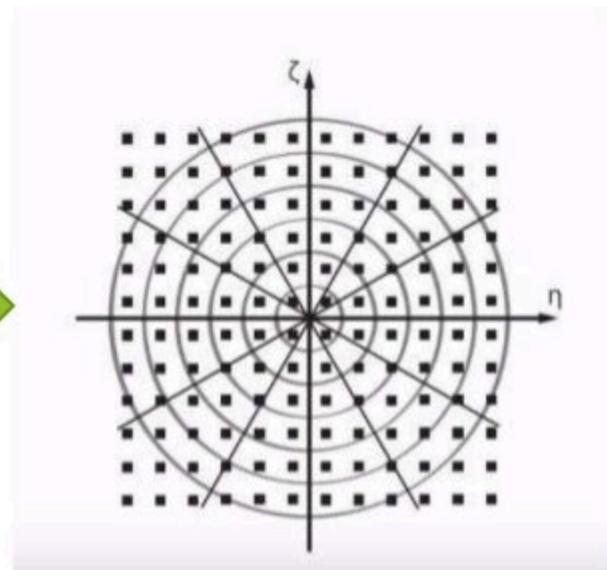
- Fourier slice theorem states that “The Fourier transform of the projection of an object at angle θ is equal to a slice of the Fourier transform of object along angle θ ”.



Fourier Slice Theorem



Interpolation

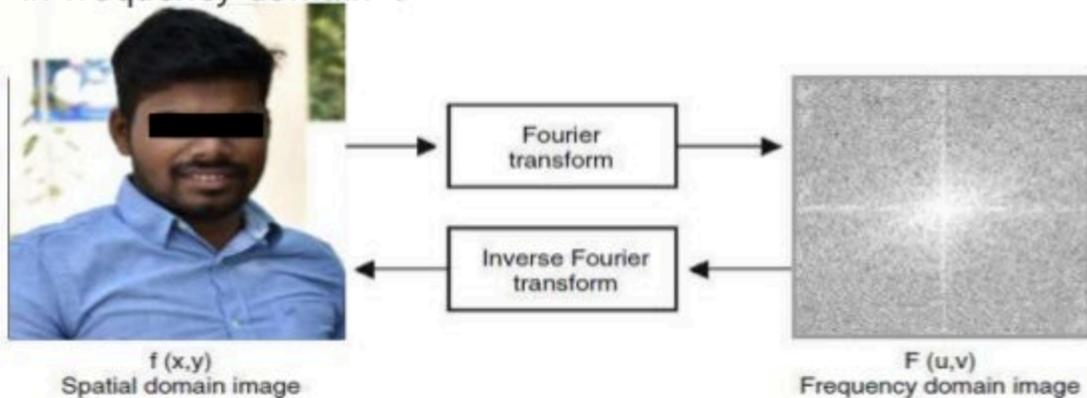


Projection data obtained in radial pattern

Regrid in uniform sample pattern

FOURIER TRANSFORM

- ▶ Developed by a mathematician Baron Jean-Baptiste-Joseph Fourier in 1807.
- ▶ Used in Radiology for image reconstruction in CT and MRI.
- ▶ Fourier transform is a “mathematical function that converts a signal in spatial domain to a signal in frequency domain”.



Divides a waveform into series of sine and cosine functions of different frequency and amplitude, which later can be separated

Fourier transform

Why ?

- ▶ The image in frequency domain can be manipulated (edge enhancement or smoothing) by changing amplitude of frequency components without losing the actual signal intensity.
- ▶ Computer can perform manipulations (digital image processing) i.e. MPR, VRT, MIP etc.
- ▶ Frequency information can be used to measure image quality through the point spread function, line spread function and modulation transfer function.

The object to be scanned is represented by function $f(x, y)$

Projection data are obtained , at least 180° , represented as spatial domain image.

Each projection data are transformed into frequency domain by Fourier transform.

CT uses Fast Fourier transform algorithm that acquire image in radial pattern thus must be converted into rectangular grid by interpolation technique.

Interpolated image is transformed into spatial domain image through inverse Fourier transform.

Fig : Flowchart showing steps in Fourier reconstruction algorithms

The background features abstract, overlapping geometric shapes in various shades of green, ranging from light lime to dark forest green. These shapes are primarily located on the left and right sides of the frame, leaving a large white central area. The shapes are layered, creating a sense of depth and movement.

Thank You