



# SNS COLLEGE OF TECHNOLOGY

Coimbatore-36.

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**COURSE NAME : 19CSB301&Automata Theory and Compiler Design**

**III YEAR/ V SEMESTER**

**UNIT – III SYNTAX ANALYSIS AND SEMANTIC ANALYSIS**

**Topic: Bottom Up Parser\_LR Parser**

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## Bottom up parsing (Right most Derivations)

\* Terminals  $\rightarrow$  Non-Terminals  
leaf node  $\rightarrow$  Root Node (Start Symbol)

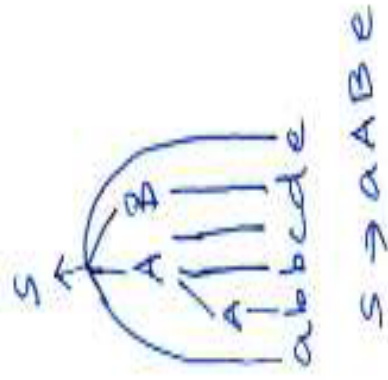
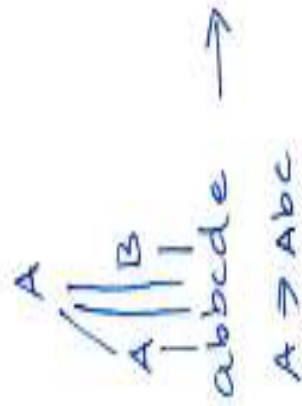
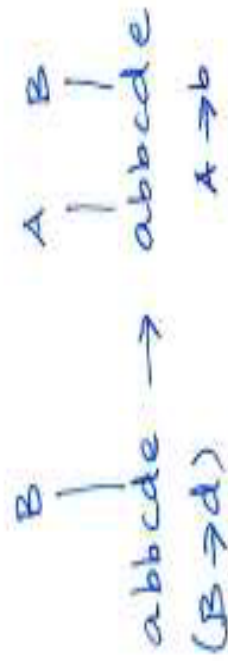
\* Example 1:

$S \rightarrow aABe$

$A \rightarrow Abc|b$

$B \rightarrow d$

Input: abcde

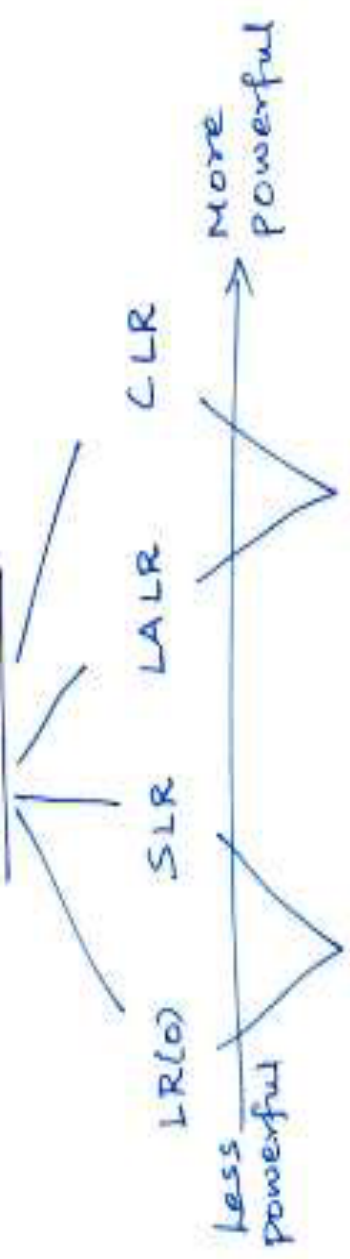




# Types of Bottom up parsing

Non-Recursive Shift Reduce parser

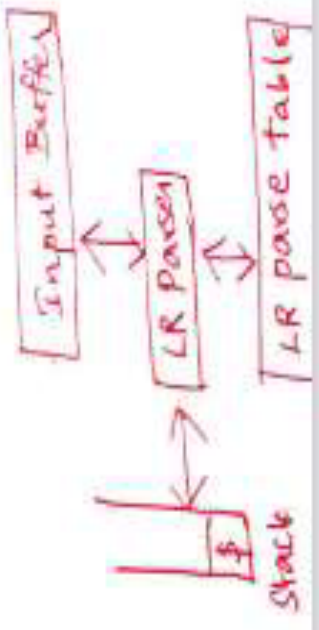
LR Parser



Operator precedence parser

LR(k)

- Left to Right processing i/p
- Right most Derivations
- k (lookahead)



- SLR - simple LR
- LALR - lookahead LR
- CLR - Canonical LR



# SHIFT REDUCE PARSING

Shift-reduce parsing is a type of bottom-up parsing that attempts to construct a parse tree for an input string beginning at the leaves (the bottom) and working up towards the root (the top).

Example:

**Consider the grammar:**

- $S \rightarrow aABe$
- $A \rightarrow Abc \mid b$
- $B \rightarrow d$

The sentence to be recognized is abcde.

REDUCTION (LEFTMOST)	RIGHTMOST DERIVATION
abcde	$S \rightarrow aABe$
aAbcde	$\rightarrow aAde$
aAde	$\rightarrow aAbcde$
aABe	$\rightarrow abcde$
S	

The reductions trace out the right-most derivation in reverse.



# Handles

## Handles:

A handle of a string is a substring that matches the right side of a production, and whose reduction to the non-terminal on the left side of the production represents one step along the reverse of a rightmost derivation.

## **Example:**

Consider the grammar:

$$\begin{aligned}
 E &\rightarrow E+E \\
 E &\rightarrow E * E \\
 E &\rightarrow (E) \\
 E &\rightarrow id
 \end{aligned}$$

$$\begin{aligned}
 E &\rightarrow \underline{E+E} \\
 &\rightarrow \underline{E+E} * E \\
 &\rightarrow E + \underline{E * id_3} \\
 &\rightarrow E + \underline{id_2} * id_3 \\
 &\rightarrow \underline{id_1} + id_2 * id_3
 \end{aligned}$$

In the above derivation the underlined substrings are called **handles**.

## Handle pruning:

A rightmost derivation in reverse can be obtained by “**handle pruning**”. (i.e.) if  $w$  is a sentence or string of the grammar at hand, then  $w = \gamma_n$  where  $\gamma_n$  is the  $n^{\text{th}}$  right-sentinel form of some rightmost derivation.





## Stack Implementation of Shift Reduce Parsing

Stack	Input	Action
\$	id <sub>1</sub> +id <sub>2</sub> *id <sub>3</sub> \$	shift
\$ id <sub>1</sub>	+id <sub>2</sub> *id <sub>3</sub> \$	reduce by E→id
\$ E	+id <sub>2</sub> *id <sub>3</sub> \$	shift
\$ E+	id <sub>2</sub> *id <sub>3</sub> \$	shift
\$ E+id <sub>2</sub>	*id <sub>3</sub> \$	reduce by E→id
\$ E+E	*id <sub>3</sub> \$	shift
\$ E+E*	id <sub>3</sub> \$	shift
\$ E+E*id <sub>3</sub>	\$	reduce by E→id
\$ E+E*E	\$	reduce by E→ E *E
\$ E+E	\$	reduce by E→ E+E
\$ E	\$	accept

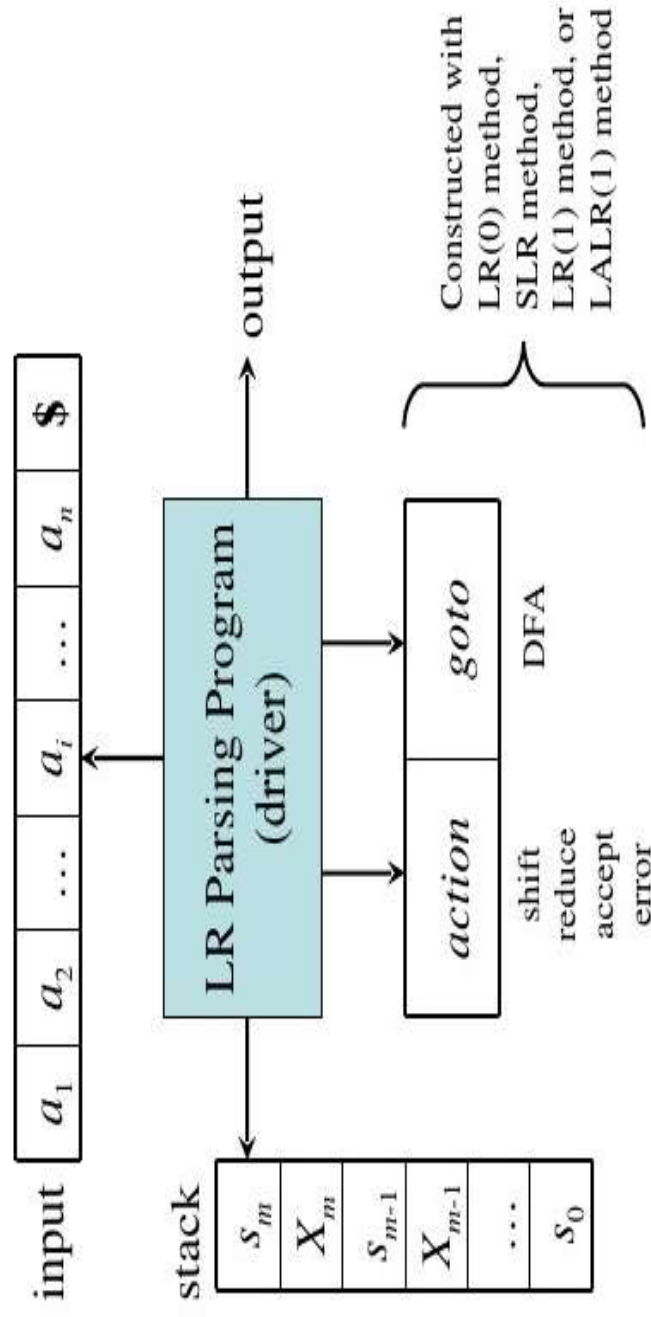
### Actions in shift-reduce parser:

- shift – The next input symbol is shifted onto the top of the stack.
- reduce – The parser replaces the handle within a stack with a non-terminal.
- accept – The parser announces successful completion of parsing.
- error – The parser discovers that a syntax error has occurred and calls an error recovery routine.



# LR Parsing Method

## Model of an LR Parser





## LR Parsing Algorithm



**Input:** An input string  $w$  and an LR parsing table with functions *action* and *goto* for grammar  $G$ .

**Output:** If  $w$  is in  $L(G)$ , a bottom-up-parse for  $w$ ; otherwise, an error indication.

**Method:** Initially, the parser has  $s_0$  on its stack, where  $s_0$  is the initial state, and  $w\$$  in the input buffer. The parser then executes the following program :

```
set  $ip$  to point to the first input symbol of  $w\$$ ;  
repeat forever begin  
  let  $s$  be the state on top of the stack and  
   $a$  the symbol pointed to by  $ip$ ;  
  if  $action[s, a] = shift\ s'$  then begin  
    push  $a$  then  $s'$  on top of the stack;  
    advance  $ip$  to the next input symbol  
  end  
  else if  $action[s, a] = reduce\ A \rightarrow \beta$  then begin  
    pop  $2 * |\beta|$  symbols off the stack;  
    let  $s'$  be the state now on top of the stack;  
    push  $A$  then  $goto[s', A]$  on top of the stack;  
    output the production  $A \rightarrow \beta$   
  end  
  else if  $action[s, a] = accept$  then  
    return  
  else error()  
end
```





### LR(0) parser

Q.  $S \rightarrow AA$   
 $A \rightarrow aA|b$

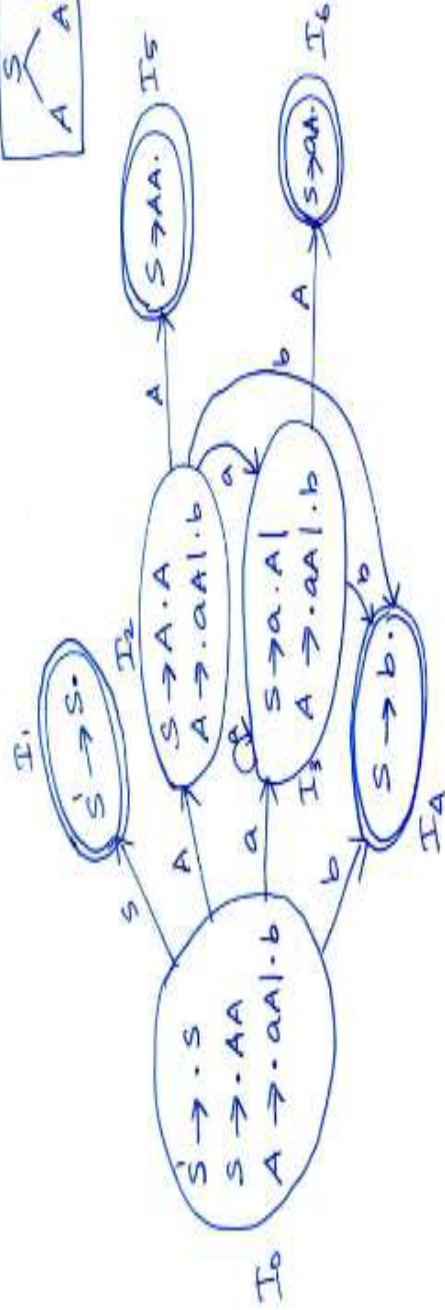
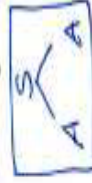
Step 1: Augmented Grammar

$S' \rightarrow S$   
 $S \rightarrow AA$   
 $A \rightarrow aA|b$

Step 2: Canonical LR(0) items

LR(0) items  $\rightarrow$  productions  $\rightarrow$

$S \rightarrow \cdot AA$  (yet to read)  
 $S \rightarrow A \cdot A$  (want to read A)  
 $S \rightarrow AA \cdot$  (completing read).



No. The production

- 1  $S \rightarrow AA$
- 2  $A \rightarrow aA$
- 3  $A \rightarrow b$



Step 3: parse Table

	Goto (Non-Termi)	Action (Terminals)
	A S	a b \$
I <sub>0</sub>	Z I	S <sub>3</sub> S <sub>4</sub>
I <sub>1</sub>		Accept
I <sub>2</sub>	5	S <sub>3</sub> S <sub>4</sub>
I <sub>3</sub>	6	S <sub>3</sub> S <sub>4</sub>
I <sub>4</sub>		r <sub>3</sub> r <sub>3</sub> r <sub>3</sub>
I <sub>5</sub>		r <sub>1</sub> r <sub>1</sub> r <sub>1</sub>
I <sub>6</sub>		r <sub>2</sub> r <sub>2</sub> r <sub>2</sub>

State  $\xrightarrow{T}$  Shift  
state  $\xrightarrow{N.T}$  Goto  
Final State  $\rightarrow$  Red



STACK	INPUT	ACTION
\$0	<u>a</u> abb\$	Shift a3
\$0a3	<u>a</u> bb\$	Shift a3
\$0a3a3	<u>bb</u> \$	Shift b4
\$0a3a3b4	<u>b</u> \$	Shift b4
\$0a3a3A6	<u>b</u> \$	Reduce (R3) 3rd production (3A → b)
3 → A → 6	<u>b</u> \$	Reduce (R2) 2. A → aA
\$0A2	<u>b</u> \$	Reduce (R2)
\$0A2	<u>\$</u>	Shift b4
\$0A2A5	<u>\$</u>	Reduce (R3) (3. A → b)
\$0S1	<u>\$</u>	Reduce (R1) (1. S → AA)
		Accept.



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19CSB301/ATCDI/Unit III/Bottom Up  
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