## SNS COLLEGE OF TECHNOLOGY

# DEPARTMENT OF ELECTRONICS \& COMMUNICATION ENGINEERING 

# 19ECB204 - LINEAR AND DIGITAL CIRCUITS 

II YEAR/ III SEMESTER

UNIT 3 - GATES AND MINIMIZATION TECHNIQUES

TOPIC 8 - QUINE- MC CLUSKEY METHOD OF MINIMIZATION

## WHY QUINE- MC CLUSKEY METHOD OF MINIMIZATION?

$>k$ map is difficult to simplify the Boolean functions having more than 5 variables.
$>$ Quine-McClukey tabular method is a tabular method based on the concept of prime implicants.

## QUINE- MC CLUSKEY METHOD OF

 MINIMIZATION
## Prime Implicants(PI)

$>$ Group of minterms which cannot be combined with any other minterms or groups.

## Essential Prime implicants (EPI)

$\Rightarrow$ The essential prime implicant is a prime implicant in which one or more minterm are unique.
$>$ Contains atleast one minterm which is not contained in any other.

## QUINE- MC CLUSKEY METHOD OF MINIMIZATION

## Prime Implicants(PI) - Two parts

Part 1 - Find all prime implicants by an Exhaustive search.

Part 2 - Identify the Essential prime implicants obtained in part 1 and select from the remaining prime implicants which can give the perfect minimized expression

## QUINE- MC CLUSKEY METHOD OF MINIMIZATION

Eg.
Simplify the following boolean expression using k map and verify it using Quine - Mc Cluskey method.
$Y(A, B, C, D)=\sum m(0,1,3,7,8,9,11,15)$


## QUINE- MC CLUSKEY METHOD OF MINIMIZATION

>Arrange all the minterms accordingly to number of one's contained and from the groups having no one's, one 1's, two 1's, three 1's and so on...

| Group | Minterm | Representation In <br> Binary form <br> ABCD |  |
| :---: | :---: | :--- | :--- |
| 1 | m 0 | 0000 | Zero 1's |
| 2 | m 1 | 0001 | one 1's |
| m 8 | 1000 | two 1's |  |
| 3 | m 3 | 0011 | three 1's |
|  | m 9 | 1001 |  |
| 4 | m 7 | 0111 | four 1's |
| 5 | m 15 | 1111 |  |

## ACTIVITY



## Combination of Minterms into groups of

 two| Group | Minterm | Binary Representation A B C D |
| :---: | :---: | :---: |
| 0 | $\begin{aligned} & \mathrm{m0} \mathrm{~m} 1 \\ & \mathrm{m0} \text { _ } \mathrm{m} 8 \end{aligned}$ | $\left\lvert\, \begin{array}{lll} 0 & 0 & 0 \\ -- & 0 & -- \\ \hline \end{array}\right.$ |
| 1 | $\begin{aligned} & \mathrm{m} 1 \_\mathrm{m} 3 \\ & \mathrm{~m} 1 \_\mathrm{m} 9 \\ & \mathrm{~m} 8 \_\mathrm{m} 9 \end{aligned}$ | $\left\lvert\, \begin{array}{lll} 0 & 0 & --1 \\ -- & 0 & 0 \\ 1 & 0 & 1 \end{array}\right.$ |
| 2 | $\begin{aligned} & \mathrm{m} 3 \_m 7 \\ & \mathrm{~m} 3 \_\mathrm{m} 11 \\ & \mathrm{~m} 9 \_m 11 \end{aligned}$ | $\left\lvert\, \begin{array}{cccc} 0 & -- & 1 & 1 \\ --0 & 0 & 1 \\ 1 & 0 & 0 & -- \end{array}\right.$ |
| 3 | $\begin{aligned} & \mathrm{m} 7 \_\mathrm{m} 15 \\ & \mathrm{~m} 11 \_\mathrm{m} 15 \end{aligned}$ | $\begin{array}{\|ccc} --1 & 1 & 1 \\ 1 & -1 & 1 \end{array}$ |

## Combination of Minterms into groups of

 four| Group | Minterm | Binary RepresentationA B C D |  |
| :---: | :---: | :---: | :---: |
| 0 | $\begin{aligned} & \mathrm{m0} \mathrm{~m}_{1} \mathrm{~m} 1 \_\mathrm{m} 8 \_\mathrm{m} 9 \\ & \mathrm{m0} \mathrm{~m} 8 \_\mathrm{m} 1 \_\mathrm{m} 9 \end{aligned}$ | $\begin{array}{llll} \hline-- & 0 & 0 & -- \\ -- & 0 & 0 & -- \end{array}$ | $B^{\prime} C^{\prime}$ |
| 1 | $\begin{aligned} & \mathrm{m} 1 \_\mathrm{m} 3 \_\mathrm{m} 9 \_\mathrm{m} 11 \\ & \mathrm{~m} 1 \_\mathrm{m} 9 \_m 3 \_\mathrm{m} 11 \end{aligned}$ | $\left\lvert\, \begin{array}{llll} \hline-- & 0 & -- & 1 \\ -- & 0 & -- & 1 \end{array}\right.$ | B'D |
| 2 | $\begin{aligned} & \mathrm{m} 3 \_\mathrm{m} 7 \_\mathrm{m} 11 \_\mathrm{m} 15 \\ & \mathrm{~m} 5 \_\mathrm{m} 11 \_\mathrm{m} 7 \_\mathrm{m} 15 \end{aligned}$ | $\begin{array}{llll} -- & -- & 1 & 1 \\ -- & -- & 1 & 1 \end{array}$ | CD |

## $Y(A, B, C, D)=B^{\prime} C^{\prime}+B^{\prime} D+C D$

Combination of Minterms into groups of
four


## ASSESSMENTS

1.What is the another name for Quine Mc Cluskey method?
2.The starting point of the tabulation method that specifies the function is the----
3.Unchecked terms in the table forms are-----------
4. What is the first tabulation method?
5.State Prime Implicants.

THANK YOU

