

SNS COLLEGE OF TECHNOLOGY

(An Autonomous Institution) Coimbatore-641035.



UNIT 3- GRAPHS

Euler and Hamilton Graphs

A connected graph 9s Ewerlan 9th evy. Verte, Theorem: 6 Is of even degree. Ploop: Let G be an Eulerian graph. we've to prove, all the vertices are of even dagree Since GI 98 Eulorlan, GI contains an Euler circut Both the colges e, and en that contrabutes 1 to the degree of Up and 20 degree of Up 25 atteast 2. In tracing this concilt, we can trad an edge enters the vortex and another edge leaves the vortex, wonth built & to the degree of vortex. THE & touch for all the vertices and so each vortex is of degree 2, which is an even no, If or is an Ewlerlan graph, then each vortex of the graph is of even degree. Convoysely, let G be a graph such that all the vestifices are of even degree. TO PROVE: Gr is an Euley grouph. we shall construct an Euler cercuit and to prove GIBS an Fully graph. Let u be the autithary vertex in G. Beginning with a form a concert C: V, VI, Var, Vn-1,V Thas as possible become each vortex is of even degree we can leave a vortex along an edge not used to enter it. This totaceng stops only at the vortex become Vis also of even degree and we started from V. Thus we get a vorwet. If c godudes all the edges of C, then c is an Euler wrult. Hence, G is Eulerian.



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Suppose c does not contain all the edges of GI. consider the subgraph H of GI by deleting all the edges of c from GI and Vertzgass not gholdent with the glemathing edges.

Note that all the vortifices of H are of even degree. Since Gibs connected, H and C musit have a common vortex U.

Beginnfing with u, construct a concrit c, for H. Now combine c and C, to form a larger circuit Cg. If it watalos all the edges of G, then G is Eulerian. otherwise continue this process until we get an Eulosean circuit.

B9DCO GIPC f9D9te, the procedure 6911 come to the end wifth an eulergan concuit.

Hence G & Eulongan.