

SNS COLLEGE OF TECHNOLOGY



(An Autonomous Institution) Coimbatore-641035.

UNIT 3- GRAPHS

Connectivity

path:

A pair In a graph is a requence VI, Va, ... VK Of Vood 9000, each adjacent to the heat.

Length of the path:

The No. of edges appearing In the sequence of path

Growets:

A closed path 90 which all the odges were destined is called a concert.

Cyclec:

A corcuet an which all the vostaces are distanct is a cyclec.

An desected graph is said to be connected 95 connected graph: any par of nodes are leachable from one another. a, there is a path blow any pair of nodes.

Strongly connected:

A gample degraph & said to be strongly connected of too any past of nodes of the graph both the nates of the past are reachable from obe anothon.

weakly connected:

A simple digraph is said to be wearly connected 96 9t 13 Connected as an undbrected graph on which the direct an of the edges is neglected.

Unflaterally connected:

A gemple degraph is said to be unitationally connected, of food any power of nodes of the graph at least one of the nodes of the past & Heachable from the other node.

Note: 1). A uc is we but a we is not necessarily UC.

2) A BC 18 both USWC.



SNS COLLEGE OF TECHNOLOGY



(An Autonomous Institution) Coimbatore-641035.

UNIT 3- GRAPHS

Connectivity

Theosem 4: A sample graph coath is vertices and K component Cannot have more than (h-K)(h-Kf1) edges. A sample geaph with n veitices and to compone can have atmost (n-k)(n-K++) edges. Pecol: Let n, na, ..., nx be the no. of vortices in each of K components of the graph G. Then $n_1 + n_2 + \dots + n_K = n = |V(61)|$ $\frac{n}{2} n_i = n \rightarrow (1)$ Nows $\leq (n_i - 1) = (n_i - 1) + (n_2 - 1) + \dots + (n_K - 1)$ $=\underbrace{\kappa}_{i-1}$ $n_i - \kappa$ $\frac{\kappa}{1-1}(h_1-1) = h-\kappa$ Squaring on both 59des. $[x](n,-1)^{2} = (n-k)^{2}$ (n,-1)2+ (n2-1)2+...+ (nx-1)2 = 12+ x2-2nx $n_1^2 + 1 - 2n_1 + n_2^2 + 1 - 2n_2 + \dots + n_{K+1}^2 - 2n_K \leq n_1^2 + n_2^2 - 2n_K$ $(n_1^2 + n_2^2 + \dots + n_K^2) - 2n_1 - 2n_2 - \dots - 2n_K + 1 + 1 + 1 + \dots + 1 \leq n_1^2 + 2n_1^2 - 2n_1^2 + 2n_1^2 +$ $\frac{k}{1-1} p_1^2 - a(p_1 + p_2 + \dots + p_K) + k \leq p_1^2 + k^2 - 2p_K$ $\sum_{i=1}^{k} n_{i}^{2} = 2n + k \leq n^{2} + k^{2} - 2nk$ $\sum_{i=1}^{k} n_{i}^{2} \leq n^{2} + k^{2} - 2nk + 2n - k \rightarrow (2)$ By them. 3, G & simple and maximum be. of edges of G1 90 Gts component is $\frac{b_i}{a}$ $\frac{b_i}{a}$.



SNS COLLEGE OF TECHNOLOGY



(An Autonomous Institution) Coimbatore-641035.

UNIT 3- GRAPHS

Connectivity

Maximum No. of edges of GI

$$=\frac{1}{1-1} \frac{h_1(h_1-1)}{2}$$

$$=\frac{1}{1-1} \frac{h_1^2-h_1^2}{2}$$

$$=\frac{1}{1-1} \left[\frac{1}{1-1} \frac{h_1^2-h_1^2}{2}\right]$$

$$=\frac{1}{1-1} \left[\frac{1}{1-1} \frac{h_1^2-h_1^2}{2}\right]$$

$$=\frac{1}{1-1} \left[\frac{1}{1-1} \frac{h_1^2-h_1^2-h_1^2}{2}\right]$$

$$=\frac{1}{1-1} \left[\frac{1}{1-1} \frac{h_1^2-h$$