

SHEAR:

A rectangular reinforced concrete beam is simply supported on masonry walls 300mm thick and 7m c/c. The beam has to carry, in addition to its own weight, a distributed live load of 8kN/m and a dead load of 4kN/m. The simply supported beam is provided with 3 nos. 16mm diameter at bottom. Design a beam for shear. Consider size of the beam is 250 x 500mm. M20 & Fe415 combinations are used.

GIVEN:

Live load = 8kN/m, Dead load (excluding self.wt) = 4kN/m

Area of tension steel, $A_{st} = 3-16\text{mm}\phi$

Overall size of beam = 250 x 500mm

Span, $L = 7\text{m c/c}$. Width = 300mm.

Grade, $f_{ck} = 20\text{N/mm}^2$, $f_y = 415\text{N/mm}^2$

LOAD CALCULATION:

Live load = 8kN/m

Dead load (excluding self-weight) = 4kN/m

Self-weight of beam = $0.25 \times 0.5 \times 25 = 3.125\text{ kN/m}$

Total load, $w = 15.125\text{ kN/m}$.

Factored load = $1.5 \times 15.125 = 22.69\text{ kN/m}$.

$$\begin{aligned} \text{Shear force at } \left. \begin{array}{l} \text{support } \downarrow \\ \text{support } \uparrow \end{array} \right\} &= \frac{wL}{2} = \frac{22.69 \times 7}{2} \\ &= 79.415\text{ kN}. \end{aligned}$$

Critical shear occurs at a distance effective depth 'd' from face of a masonry wall.

Overall depth of beam, $D = 500\text{mm}$ and also

Provide 20mm ϕ bar.

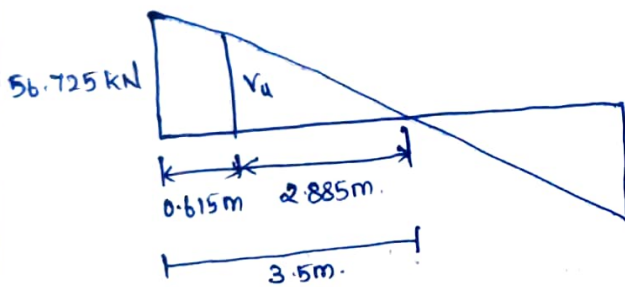
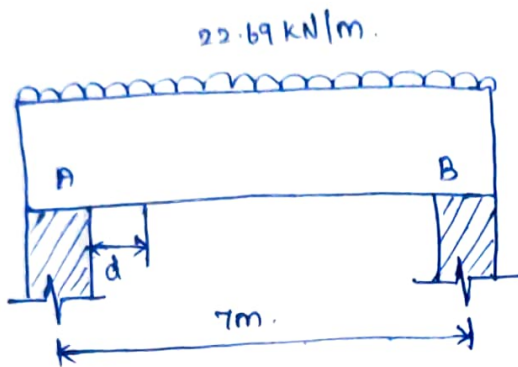
$$\text{Effective depth, } d = D - \text{clear cover} - \phi/2$$

$$= 500 - 25 - 20/2 = 465$$

Critical shear location from centre of support

$$= d + \frac{\text{masonry wall thickness}}{2}$$

$$= 465 + \frac{300}{2} = 615 \text{ mm} = 0.615 \text{ m}$$



Factored shear force, V_u at critical section can be calculated by similar triangle principle,

$$\frac{79.415}{3.5} = \frac{V_u}{2.885} \Rightarrow V_u = 65.46 \text{ kN}$$

$$\text{Nominal shear stress, } \tau_v = \frac{V_u}{bd}$$

$$\tau_v = \frac{65.46 \times 10^3}{250 \times 465} = 0.56 \text{ N/mm}^2$$

From Pg. no-73, Table 20.

$$\text{Maximum shear stress, } \tau_{\text{max}} = 2.8 \text{ N/mm}^2$$

3.

$\tau_v < \tau_{max}$, hence given section size is adequate.

Shear resisted by concrete } $V_{uc} = \text{Shear stress} \times \text{Eff. c/s area}$

$$V_{uc} = \tau_c \times bd.$$

$$P_t = \frac{100 A_{st}}{bd} = \frac{100 \times 3 \times \pi/4 \times 16^2}{250 \times 465} = 0.52\%$$

From pg. no-73, Table 19,

P_t	τ_c
$x_1 = 0.5$	$y_1 = 0.48$
$x_2 = 0.75$	$y_2 = 0.56$
$x = 0.52$	$y = ?$

$$y = y_1 + \frac{y_2 - y_1}{x_2 - x_1} (x - x_1) = 0.48 + \frac{0.56 - 0.48}{0.75 - 0.50} (0.52 - 0.5)$$

$$y = \tau_c = 0.4864 \text{ N/mm}^2$$

$$V_{uc} = 0.4864 \times 250 \times 465 = 56544 \text{ N} = 56.54 \text{ kN}.$$

Shear to be resisted by stirrups, } $V_{us} = V_u - V_{uc}$

$$V_{us} = 65.46 - 56.54 = 8.92 \text{ kN}.$$

Spacing between stirrups, S_v can be determined by taking least value of the following 4 cases.

Provide 2 legged 8mm ϕ stirrups.

$$a) S_v = \frac{0.87 f_y A_{st} d}{V_{us}}$$

$$= \frac{0.87 \times 415 \times 2 \times \frac{\pi}{4} \times 8^2 \times 465}{8.92 \times 10^3} = 1882.15 \text{ mm}$$

$$S_v < 1882.15 \text{ mm c/c}$$

$$b) S_v < 0.75d \Rightarrow S_v = 0.75 \times 465 = 348.75 \text{ mm.}$$

$$c) S_v = 450 \text{ mm.}$$

$$d) S_{vmax} = \frac{2.175 f_y A_{st}}{b}$$

$$= \frac{2.175 \times 415 \times 2 \times \frac{\pi}{4} \times 8^2}{250}$$

$$= 361.05 \text{ mm.}$$

Provide 2 legged 8mm ϕ stirrups at 340mm c/c.