



# SNS COLLEGE OF TECHNOLOGY



Coimbatore-36.

An Autonomous Institution

Accredited by NBA – AICTE and Accredited by NAAC – UGC with ‘A+’ Grade  
Approved by AICTE, New Delhi & Affiliated to Anna University, Chennai

**COURSE CODE& NAME : 19CSB301 & AUTOMATA THEORY AND COMPILER  
DESIGN**

**III YEAR/ V SEMESTER**

**UNIT – I FINITE AUTOMATA AND REGULAR LANGUAGES**

**Topic: Central concepts of Automata Theory**

Dr.B.Vinodhini

Assistant Professor

Department of Computer Science and Engineering

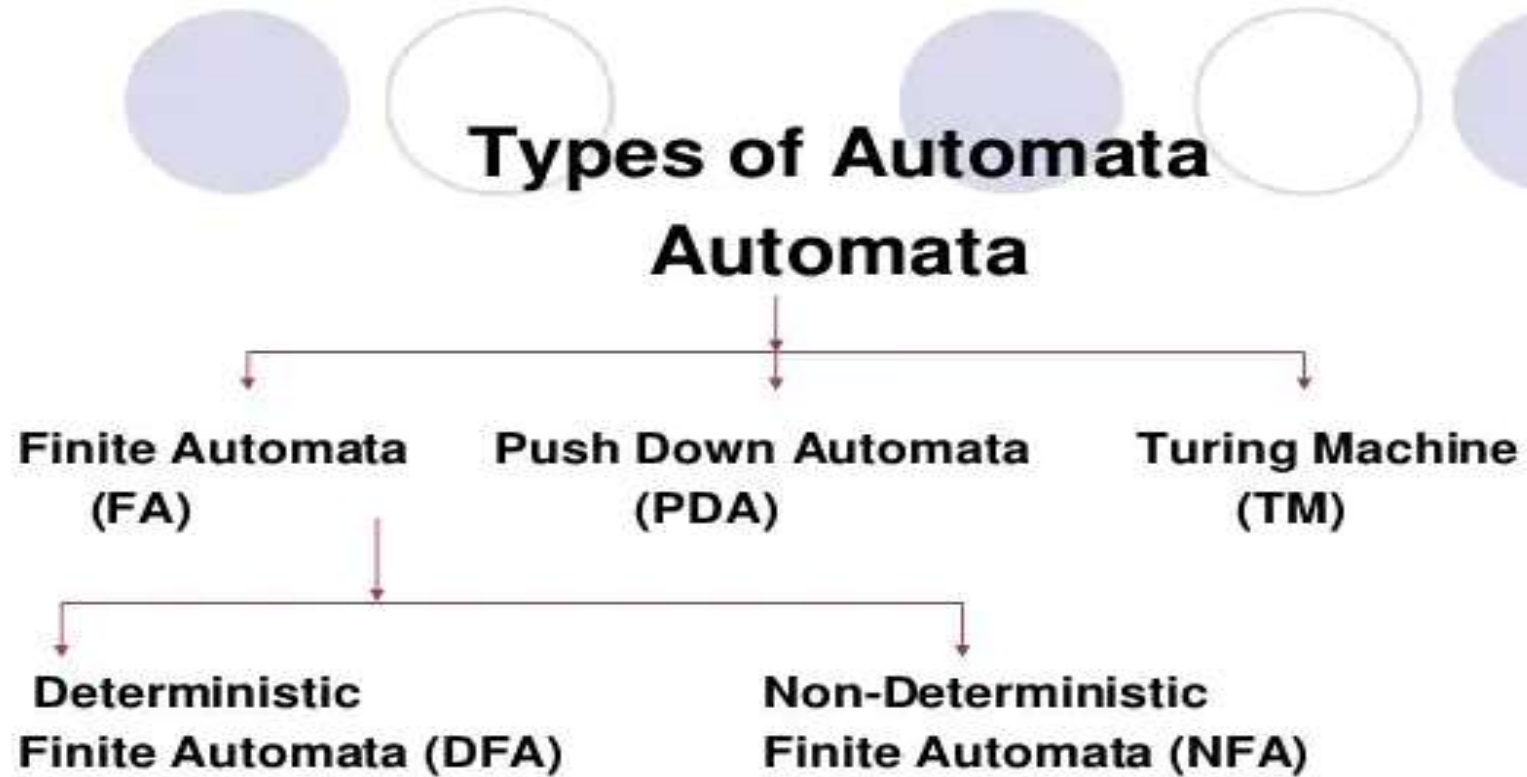


## *Introduction to Automata*

- Theory of automata is a theoretical branch of computer science and mathematical.
- It is the study of abstract machines and the computation problems that can be solved using these machines.
- The abstract machine is called the automata.
- The main motivation behind developing the automata theory was to develop methods to describe and analyse the dynamic behaviour of discrete systems.
- This automaton consists of states and transitions. The **State** is represented by **circles**, and the **Transitions** is represented by **arrows**.
- Automata is the kind of machine which takes some string as input and this input goes through a finite number of states and may enter in the final state.



# Types of Automata





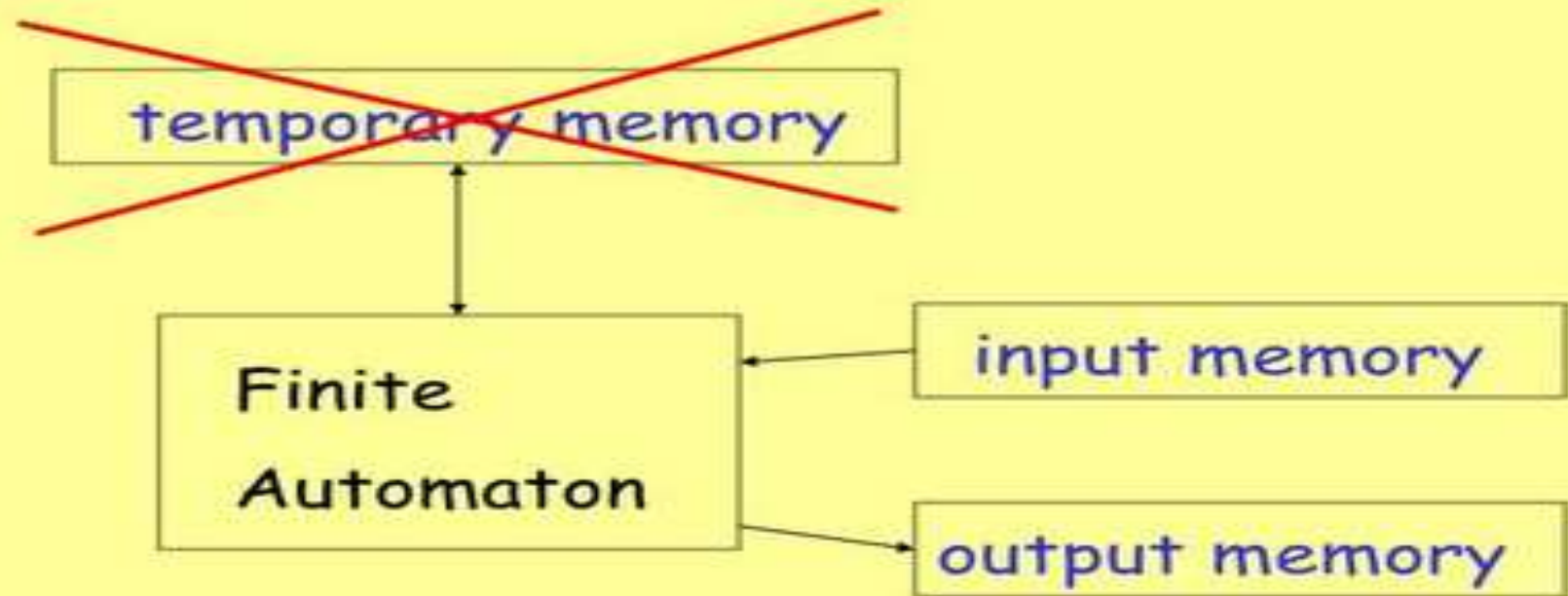
# *Types of Automata*

Automata are distinguished by the temporary memory

- **Finite Automata:** no temporary memory
- **Pushdown Automata:** stack
- **Turing Machines:** random access memory



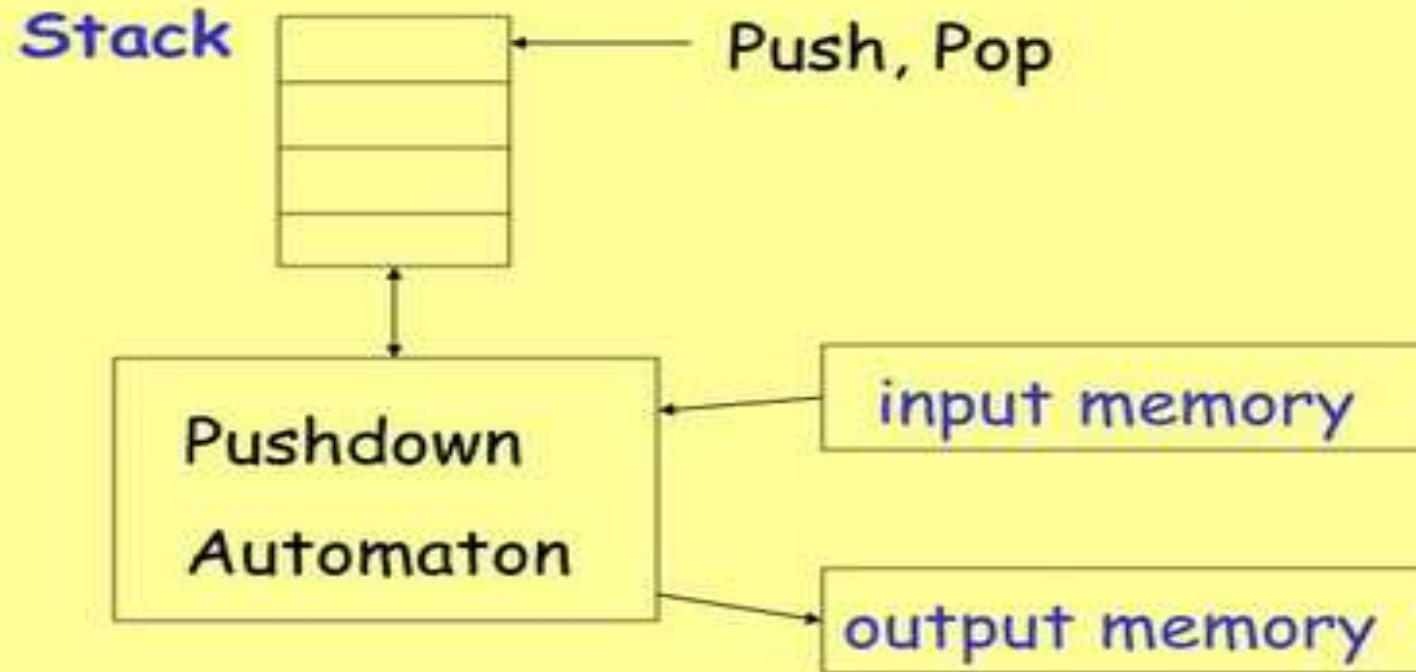
# Types of Automata



Example: Vending Machines  
(small computing power)



# Types of Automata

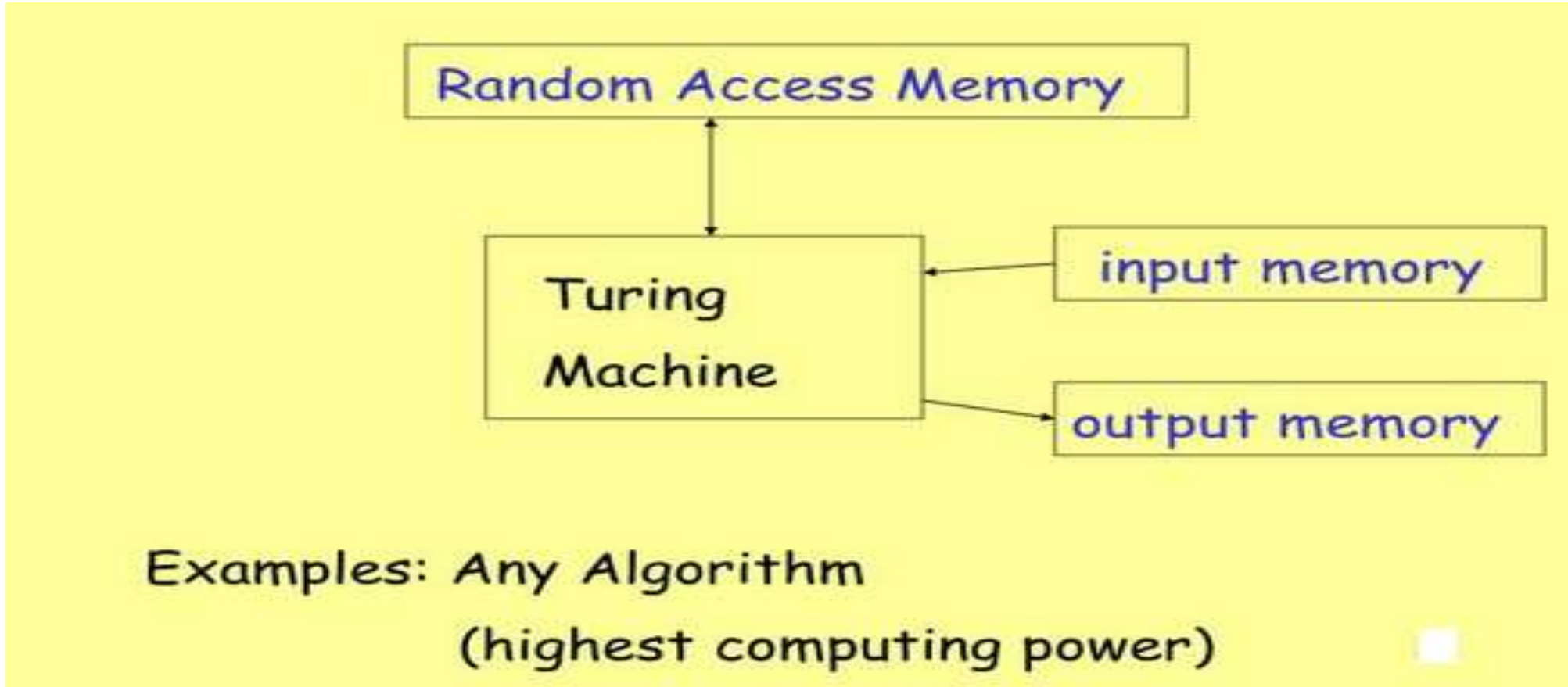


Example: Compilers for Programming Languages  
(medium computing power)



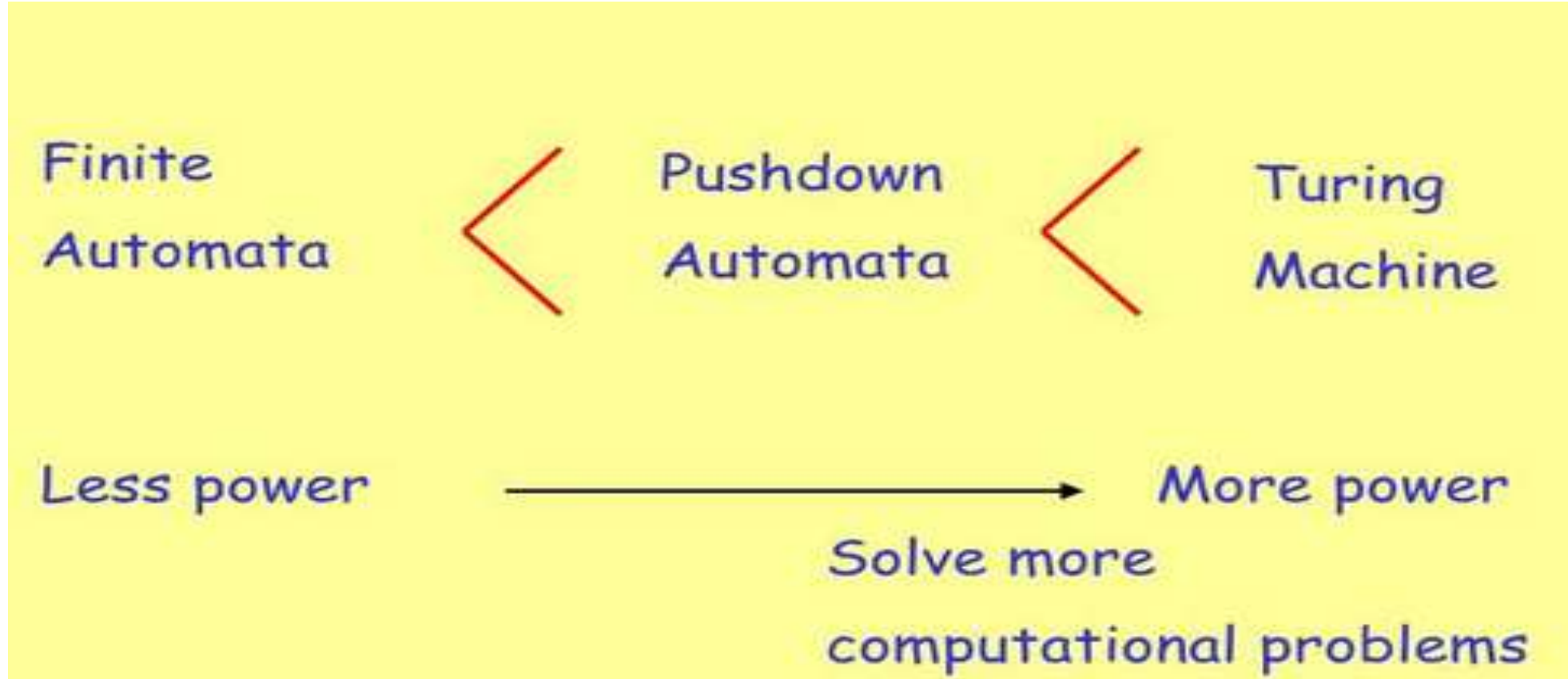


# Types of Automata





# Types of Automata







# Types of Automata

Model	Language Recognition	Memory Management	Implementation
<b>Finite Automata</b>	Regular Languages	No temporary memory	Elevators, Vending Machines, Traffic Light, Neural Network (small computing power)
<b>Pushdown Automata</b>	Context-free Languages	Stack	Compilers for Programming Languages (medium computing power)
<b>Turing machine</b>	Unrestricted Grammar, Lambda Calculus (Computable Languages)	Random access memory	Any Algorithm (highest computing power)



## *Key Terminologies*

### **Symbols:**

Symbols are an entity or individual objects, which can be any letter, alphabet or any picture.

### **Example:**

1, a, b, #

### **Alphabets:**

Alphabets are a finite set of symbols. It is denoted by  $\Sigma$ .

Examples

$\Sigma = \{a, b\}$     $\Sigma = \{A, B, C, D\}$     $\Sigma = \{0, 1, 2\}$     $\Sigma = \{0, 1, \dots, 5\}$



## *Key Terminologies*

### **String:**

It is a finite collection of symbols from the alphabet. The string is denoted by  $w$ .

### **Example 1:**

If  $\Sigma = \{a, b\}$ , various string that can be generated from  $\Sigma$  are  $\{ab, aa, aaa, bb, bbb, ba, aba.....\}$ .

A string with zero occurrences of symbols is known as an empty string. It is represented by  $\epsilon$ .

The number of symbols in a string  $w$  is called the length of a string. It is denoted by  $|w|$ .



## *Key Terminologies*

### **Language( Set of Strings with Rules)**

A language is a collection of appropriate string. A language which is formed over  $\Sigma$  can be **Finite** or **Infinite**.

#### **Example: 1**

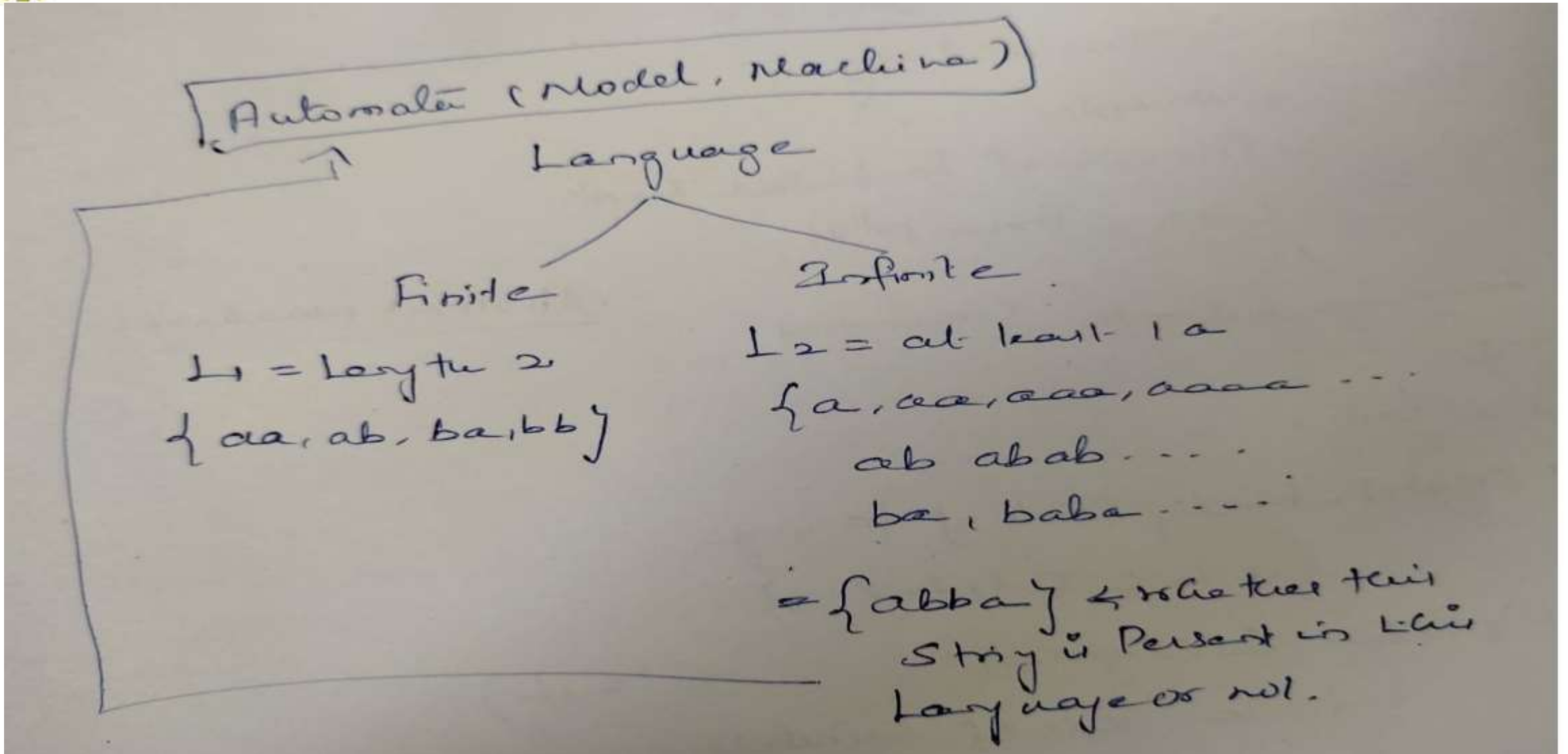
$L1 = \{\text{Set of string of length 2}\} = \{aa, bb, ba, bb\}$  **Finite Language**

#### **Example: 2**

$L2 = \{\text{Set of all strings starts with 'a'}\} = \{a, aa, aaa, abb, abbb, ababb\}$   
**Infinite Language**



# Key Terminologies





# Key Terminologies

Empty String, Length of String, reverse of String, Power of alphabet, Power of String

$$\Sigma = \{a,b\} \quad \wedge \quad a \quad b \quad aa \quad ab$$

**Empty String** string that has no letter, also known as **Null string**, denoted by  $\Lambda$ ,  $\lambda$  or  $\epsilon$   
It's length is Zero (0)

**Length of String** is the number of letters in a string, denoted by  $|s|$   
Example:  $s = abab \quad |s| = 4 \quad \text{or} \quad \text{length}(s) = 4 \quad \text{or} \quad \text{length}(abab) = 4$

**Reverse of String** Is obtained by writing letters of string in reverse order, denoted by  $\text{Rev}(s)$  or  $\overset{\curvearrowright}{s}$  Or  $\text{Reverse}(s)$   
Example:  $s = abab \quad \text{Rev}(s) = baba \quad \text{Reverse}(s) = baba$

**Power of Alphabet** Determines that the strings made from alphabet will be of length equal to power of alphabet  
 $\Sigma = \{a,b\}^2 \quad \{aa, ab, ba, bb\}$  Total number of letters in alphabet  $\longrightarrow n^m \quad \overset{\text{Length/power}}{2^2 = 4}$

**Power of string** Determines the length of string  
 $(bab)^2 = babbab$   
 $ba^2b = baab$





# Power of Alphabet

power set of Alphabet

i) Kleen plus

ii) Kleen closure

Kleen closure  $\rightarrow \Sigma^*$

$$\begin{aligned}\Sigma^* &= \Sigma^0 \cup \Sigma^1 \cup \dots \cup \Sigma^n \\ &= \epsilon \cup \Sigma^1 \cup \Sigma^2 \cup \dots \cup \Sigma^n\end{aligned}$$

Kleen plus  $\rightarrow \Sigma^+ = \Sigma^* - \epsilon$

$$\Sigma^+ = \Sigma^* - \epsilon = \Sigma \cup \Sigma^2 \cup \Sigma^3 \cup \dots \cup \Sigma^n$$



# Power of Alphabet

Kleene Star/ Closure/Operator **VS** Kleener Closure/Plus/Positive , Lexicographic Order

**Kleene Star**  
**Kleene Closure**  
**Kleene Operator**

It is undermined power, represent infinite number of terms can be made including empty string

Denoted by \*

**Kleene Plus**  
**Kleene Positive**  
**Positive Closure**

It is undermined power, represent infinite number of terms can be made except empty string

Denoted by +

**Lexicographic order** Method of Sequencing a language in which strings are grouped by their length (i.e. strings of shortest length first)

**Power of Alphabet** Determines that the strings made from alphabet will be of length equal to power of alphabet

$\Sigma = \{a,b\}$

$\Sigma^2 = \{a,b\}^2$

$\Sigma^2$  {aa, ab, ba, bb}

$\Sigma^* = \{a,b\}^*$

$\Sigma^*$  { ^ , a, b, aa, ab, ba, bb, aaa, aab, ... }

$\Sigma^+ = \{a,b\}^+$

$\Sigma^+$  { a, b, aa, ab, ba, bb, aaa, aab, ... }

**Power of string**

Determines the length of string

$ba^2b = baab$

$ba^*b = bb$  or  $bab$  or  $baab$  or  $baaaaaaab$

$ba^+b = bab$  or  $baab$  or  $baaaaaaab$



# Power of Alphabet

Power of  $\Sigma$        $\Sigma = \{a, b\}$

$\Sigma^0 =$  Set of all strings with length '0' =  $\lambda, \epsilon$        $2^0$

$\Sigma^1 =$  " " " " " "      1       $\{a, b\}$        $2^1$

$\Sigma^2 =$  " " " " " "      2

$\Sigma^3 =$  " " " " " "      3       $\Sigma \cdot \Sigma = \{a, b\} \cdot \{a, b\} = \{aa, ab, ba, bb\}$        $2^2$

$\Sigma^4 =$  " " " " " "      4       $\Sigma \cdot \Sigma \cdot \Sigma = \{a, b\} \cdot \{a, b\} \cdot \{a, b\} = \{aaa, aab, aba, abb, baa, bab, bba, bbb\}$        $2^3$

...

$\Sigma^*$  (Kleene closure) =  $\{a, b\}^*$        $2^n$       Infinite language.



# *Types of Grammar*



# Types of Grammar

## • *Grammar in Automata*

- $G = (V, T, P, S)$
- V – Non-Terminals / Variables / Auxillary Symbols (A,B,C,....)
  - Takes part in generation of sentence (Not a part of sentence)
- T – Terminals (small-case letters a,b,c,....)
- P – Production Rules
- S – Start Symbol

## Example1

$V = \{S\}$

$T = \{a, b\}$

$P = \{S \rightarrow aSbS, S \rightarrow bSaS, S \rightarrow \epsilon\}$

$S = \{S\}$

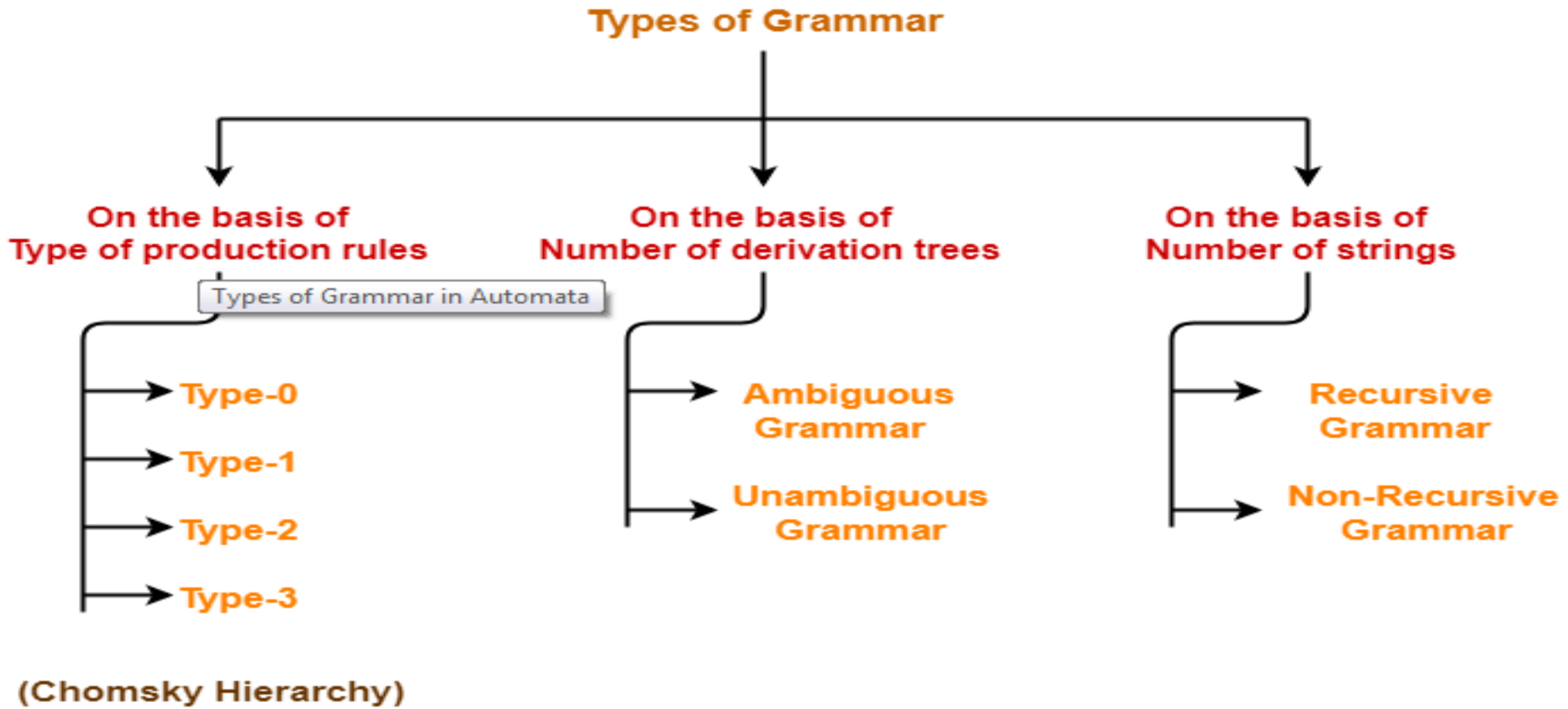
## Example2

$V = \{S, A, B\}$

$T = \{a, b\}$

$P = \{S \rightarrow ABA, A \rightarrow BB, B \rightarrow ab, AA \rightarrow b\}$

$S = \{S\}$



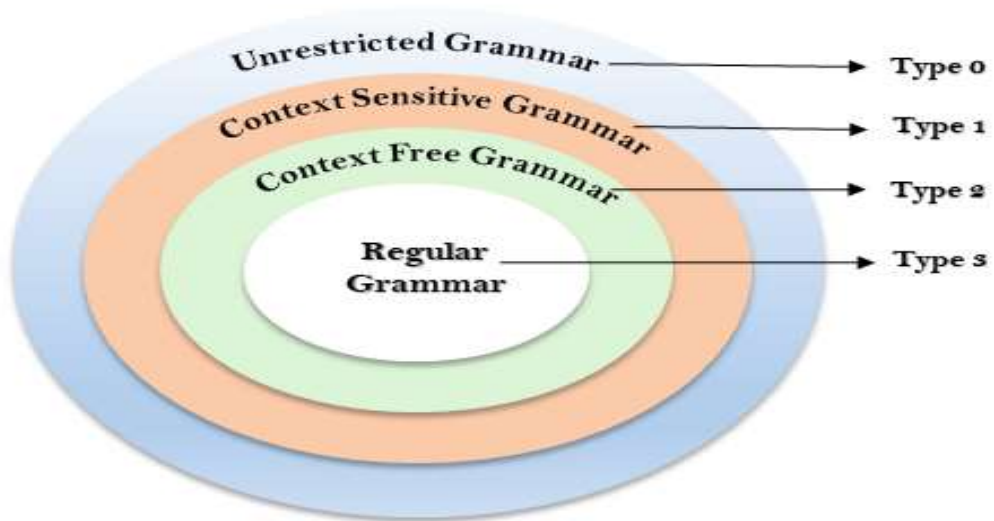




# Chomsky Hierarchy



Grammar Type	Grammar Accepted	Language Accepted	Automaton
Type 0	Unrestricted grammar	Recursively enumerable language	Turing Machine
Type 1	Context-sensitive grammar	Context-sensitive language	Linear-bounded automaton
Type 2	Context-free grammar	Context-free language	Pushdown automaton
Type 3	Regular grammar	Regular language	Finite state automaton



Type 3  $\subseteq$  Type 2, Type 1, Type 0  
Type 2  $\subseteq$  Type 1, Type 0  
Type 1  $\subseteq$  Type 0



# Chomsky Hierarchy



- Type 0 (Unrestricted)

- $\alpha \rightarrow \beta$
- $\alpha \in (V+T)^+ \leftarrow$  excluding  $\epsilon$
- $\beta \in (V+T)^* \leftarrow$  including  $\epsilon$
- $\alpha \neq \epsilon$

- Type 1 (Context Sensitive Grammar)

- $\alpha \rightarrow \beta$
- $|\alpha| \leq |\beta|$

- Type 2 (Context Free Grammar)

- $\alpha \rightarrow \beta$
- $\alpha \in V$
- $\beta \in (V+T)^*$

- Type 3 (Restricted)

- $V \rightarrow VT^*/T^*$  (Right Regular Language) OR  $T^*V/T^*$  (Left Regular language)
- Example:  $A \rightarrow aB, A \rightarrow a$



# Chomsky Hierarchy



## Rules

Type 0  $\rightarrow \alpha \neq \epsilon$

Type 1  $\rightarrow |\alpha| \leq |\beta|$

Type 2  $\rightarrow \alpha \in V, \beta \in (V+T)^*$

Type 3  $\rightarrow \alpha \rightarrow aB$  or  $\alpha \rightarrow a$

Examples of type of Grammar

$\alpha \rightarrow \beta$

e 0 :  $\alpha \neq \text{NULL}$

e 1 :  $|\alpha| \leq |\beta|$

e 2 :  $A \in V$

e 3 :  $A \rightarrow aB$  or  $A \rightarrow a$

2.)  $S \rightarrow Xa \checkmark$   
 $X \rightarrow a \checkmark$   
 $X \rightarrow aX \checkmark$   
 $X \rightarrow abcX$   
 $X \rightarrow \epsilon$

← Type 2

4.)  $AB \rightarrow AbB$   
 $A \rightarrow bcA$   
 $B \rightarrow b$

↓  
Type 1

3.)  $X \rightarrow \epsilon \checkmark$   
 $X \rightarrow a/aY \checkmark$   
 $Y \rightarrow b \checkmark$

↓  
Type 3

$S \rightarrow ACaB$   
 $Bc \rightarrow acB$   
 $CB \rightarrow DB$   
 $aD \rightarrow Db$

→ Type 1



# *References*

- John E. Hopcroft and Rajeev Motwani and Jeffrey D. Ullman, “Introduction to Automata Theory, Languages and Computation”, Second Edition, Pearson Education, New Delhi, (2007) (UNIT-I )
- Linz P. An introduction to formal languages and automata. Sixth edition, Jones and Bartlett Publishers; 2016.(UNIT-I)
- [Ramaiah k. Dasaradh](#) “Introduction to Automata and Compiler Design “ First Edition ,Prentice Hall India Learning Private Limited(2011)( UNIT-I to V)

