



SNS COLLEGE OF TECHNOLOGY

(An Autonomous Institution)

16AE201/ Aero Engineering Thermodynamics
Unit -4/ VAPOUR POWER CYCLES

SOLVED PROBLEMS – DUAL CYCLE

The compression ratio of an air standard dual cycle is 12 and the maximum pressure on the cycle is limited to 70bar. The pressure and temperature of the cycle at the beginning of compression process are 1bar and 300K. Calculate the thermal efficiency and Mean Effective Pressure. Assume cylinder bore = 250mm, Stroke length = 300mm, $C_p=1.005\text{KJ/Kg K}$, $C_v=0.718\text{KJ/Kg K}$.

Given data:

Assume $Q_{s1} = Q_{s2}$

Compression ratio (r) = 12

Maximum pressure (P_3) = (P_4) = 7000 KN/m²

Temperature (T_1) = 300 K

Diameter (d) = 0.25m

Stroke length (l) = 0.3m

To find:

Dual cycle efficiency (η_{dual})

Mean Effective Pressure (P_m)

Solution:

$$\frac{T_2}{T_1} = \left[\frac{V_2}{V_1} \right]^{\gamma-1}$$
$$= [r]^{\gamma-1}$$

$$T_2 = 300 [12]^{1.4-1}$$

$$T_2 = 810.58\text{K}$$

$$\frac{P_2}{P_1} = \left[\frac{V_1}{V_2} \right]^{\gamma}$$

$$P_2 = [12]^{1.4} \times 100$$

$$P_2 = 3242.3\text{KN/m}^2$$

By process 2-3:

$$\frac{P_2}{T_2} = \frac{P_3}{T_3}$$

$$\frac{P_3}{P_2} = \frac{T_3}{T_2}$$

$$T_3 = \left[\frac{7000}{3242.3} \right] 810.58$$

$$T_3 = 1750\text{K}$$

Assuming $Q_{s1} = Q_{s2}$

$$mC_v[T_3 - T_2] = mC_p[T_4 - T_3]$$

$$0.718 [1750 - 810.58] = 1.005 [T_4 - 1750]$$

$$T_4 = 2421.15\text{K}$$

By process 4-5:

$$\frac{T_4}{T_5} = \left[\frac{V_5}{V_4} \right]^{\gamma-1}$$

$$= \left[\frac{r}{\rho} \right]^{1.4-1}$$

We know that, $\rho = \frac{V_4}{V_3} = \frac{T_4}{T_3} = \frac{2421.15}{1750} = 1.38$

$$\frac{T_4}{T_5} = \left[\frac{12}{1.38} \right]^{0.4}$$

$$T_5 = \frac{2421.15}{\left(\frac{12}{1.38} \right)^{0.4}}$$

$$T_5 = 1019.3\text{K}$$

Heat supplied $Q_s = 2 \times m C_v \times [T_3 - T_2]$

$$= 2 \times 1 \times 0.718 \times [1750 - 810.58]$$

$$Q_s = 1349 \text{ KJ/Kg}$$

Heat rejected $Q_r = m C_v [T_5 - T_1]$

$$Q_r = 516.45 \text{ KJ/Kg}$$

$$\eta_{\text{dual}} = \frac{Q_s - Q_r}{Q_s} = \frac{832.55}{1349} \times 100$$

$$\eta_{\text{dual}} = 61.72\%$$

Stroke volume $(V_s) = \frac{\pi}{4} \times d^2 \times l$

$$= \frac{\pi}{4} \times 0.25^2 \times 0.3$$

$$V_s = 0.0147 \text{ m}^3$$

Mean Effective Pressure (P_m) $= W/V_s$

$$= 832.58/0.0147$$

$$P_m = 56535 \text{ KN/m}^2$$