

## SNS COLLEGE OF TECHNOLOGY COIMBATORE - 641 035. (An Autonomous Institution)



## DEPARTMENT OF MECHANICAL ENGINEERING

19MEB201 - Fluid Mechanics and Machinery
UNIT -2 FLOW THROUGH CIRCULAR CONDUITS
NOTES

FMM-UNIT-TT FLOW THROUGH FLAT PLATE AND CIRCULAR CONDUITS VISCOUS FLOW - Introduction: The chapter deals with the flow of flords which are visions and floring at Very low velocity. At low velocity the flood moves in Layer . Each Layer of flood Slides over the adjacent Layer Layers the velocity gurdient du seints and hence a shear stress  $J = \mu d\mu$  acts on the Layers The following Cases will be Considered in this Flow of viscous fund through Circular 2. Flow of visions fund between two 3. Kinetic energy Correction and momentum Correction backors 4. Power absorbed in visions flow through
(a) Journal bearings (b) Foot Step bearings FLOW of VISCOUS FLUID THROUGH CIRCULAR

For the Flow of visions flind through circular pipe, the velocity to average velocity, the shear stress distribution and drop of Pressure for a given length to be determined.

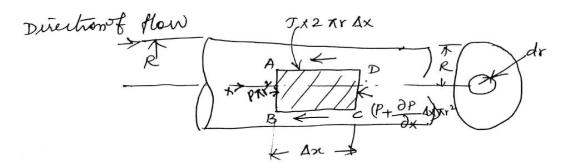
The flow through the circular pipe will be viscous or Larrienar, if the leynolds number (Re) is Less than 2000. The enpresent for Reynold rumber is given by

Re = PVD M

P- Density of flowing through Pype V- Average velocity of flord

D- Deameter of pipe

M- viscounty of flish



Viscous flow through a pipe

Consider a horsonly pipe of radius R. The viscous flind is flowing from left to right in the pipe as shown in figure

(a) consider or flish element of radius?

Slidning in a Gybriducial flish element of
radius (r+dr) Let the Longth of flish
element be Dx If P is the intensity of
Pressure on the face AB.

Then the intensity of Pressure on face CD will be  $(P + \frac{\partial P}{\partial x} \Delta x)$ . Then the forces arting on the flood element are

- 1. The Presence force PXTY' on face AB
- 2. The Pressure force (P+ \frac{\partial P}{\partial x} Ax) \times \gamma^2 on face CD
- 3. The shear force  $J \times 2\pi r \Delta \pi$  on the Swifner of fund element. Its there is no acceleration hence the Summation of all forces in the direction of flow must be Zero  $P\pi r^2 (P + \frac{\partial P}{\partial \pi}) \pi r^2 \Im \times 2\pi r \times \Delta \pi = 0$   $-\frac{\partial P}{\partial x} \Delta \pi + 2\pi r^2 \Im \times 2\pi r \times \Delta \pi = 0$

Flow of Vicenia P.

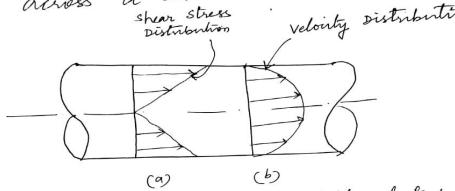
$$\frac{-\partial P}{\partial x} \cdot y - 2T = 0$$

$$\int J = -\frac{\partial P}{\partial x} \frac{y}{2} - 1$$

$$\int \int \frac{dy}{dx} dx = 0$$

$$\int \int \int \int \frac{dy}{dx} dx = 0$$

The Shear Stress I across a Section Vairies across a section is Shear stress distribution Constant. Hence a section is linear velocity Distribution



Shear Stress and velocity distribution across a Section

(i) Velocity Distribution:

to obtain the velocity distribution across a Section, the value of shear stress J= h dy is substituted in Em - 1 but in the relation J= h du yis measured from the pipe wall. Some y = R - r and dy = -drJ = h = du = - fe du

Substituting the value in Egn() rie get

- h' du - dr. 24.2

 $\frac{du}{dr} = \frac{1}{2\mu} \frac{\partial p}{\partial x} \cdot r$ 

Integrating this above Egration rist or me yes

 $u = \frac{1}{4h} \frac{\partial P}{\partial n} r^2 + C \qquad (2)$ 

where C is the constant of urbigation and its Value is obtained from the boundary Conditions that at r=R u=0 iteration

 $r = R \quad u = 0 \quad \text{ilertian}$   $0 = \frac{1}{4h} \frac{\partial p}{\partial x} R^2 + C$ 

 $C = -\frac{1}{4\mu} \frac{\partial P}{\partial x} R^2$ 

Substituting this value of c in Eqn (2) we get  $u = \frac{1}{4\mu} \cdot \frac{\partial P}{\partial x} r^2 - \frac{1}{4\mu} \cdot \frac{\partial P}{\partial x} R^2$ 

In equation 3 we get value of  $\mu = \frac{dP}{dP}$  and R are constant, which overing the velocity a value with the square of Them equation 3) is a equation of Parabola

This shows that the velocity distribution across the Section of a pipe is Parabolic. (1) Ratio of maximum velocity to Average Velocity The velocity is maximum, when is equalities 3) Thus mornimm Velocity Uness is obtained Uman =  $-\frac{1}{4h} \frac{\partial P}{\partial X} R^2$  — The average velocity u is obtained by dividing the discharge of the flind across the Section by the area of the pipe (KR2). The Discharge Gacross the Section is obtained by Considering to flow through a circular ring element of radius rand threekness dr as Shown in Ag b. The flird flowing per Second through this elementary ring da = Velouty at a radius x x Area of ring element = UXZAY dr. - 1 dp (R2-Y2) x2Ardr  $= \int_{-\frac{1}{4h}}^{R} \frac{\partial P}{\partial n} (R^2 - r^2) \chi_2 R r dr$ 

 $=\frac{1}{4\mu}\left(\frac{-\partial P}{\partial x}\right)2\pi\int_{-\infty}^{\infty}\left(R^{2}-r^{2}\right)r.dr.$ 

$$\begin{aligned}
\Theta &= \frac{1}{4\pi} \left( \frac{\partial p}{\partial n} \right) & 2\pi \int_{0}^{R} \left( R^{2} - r^{2} \right) r \cdot dr. \\
&= \frac{1}{4\pi} \left( \frac{\partial p}{\partial x} \right) & 2\pi \int_{0}^{R} \left( R^{2} r - r^{3} \right) dr. \\
&= \frac{1}{4\pi} \left( \frac{\partial p}{\partial x} \right) & 2\pi \int_{0}^{R^{2} r^{2}} \frac{r^{2}}{r^{2}} \frac{r^{4}}{r^{4}} \right) \\
&= \frac{1}{4\pi} \left( \frac{\partial p}{\partial x} \right) & x^{2}\pi \int_{0}^{R^{4}} \frac{r^{4}}{r^{2}} \frac{r^{4}}{r^{4}} \right) \\
&= \frac{1}{4\pi} \left( \frac{\partial p}{\partial x} \right) & x^{2}\pi \int_{0}^{R^{4}} \frac{r^{4}}{r^{4}} \frac{r^{4}}{r^{4}} \right) \\
&= \frac{1}{4\pi} \left( \frac{\partial p}{\partial x} \right) & x^{2}\pi \int_{0}^{R^{4}} \frac{r^{4}}{r^{4}} \frac{r^{4}}{r^{4}} \right) \\
&= \frac{1}{4\pi} \left( \frac{\partial p}{\partial x} \right) & x^{2}\pi \int_{0}^{R^{4}} \frac{r^{4}}{r^{4}} \frac{r^{4}}{r^{4}} \frac{r^{4}}{r^{4}} \right) \\
&= \frac{1}{4\pi} \left( \frac{\partial p}{\partial x} \right) & x^{2}\pi \int_{0}^{R^{4}} \frac{r^{4}}{r^{4}} \frac{r^{4}}{r^{4}} \frac{r^{4}}{r^{4}} \frac{r^{4}}{r^{4}} \frac{r^{4}}{r^{4}} \right) \\
&= \frac{1}{4\pi} \left( \frac{\partial p}{\partial x} \right) & x^{2}\pi \int_{0}^{R^{4}} \frac{r^{4}}{r^{4}} \frac{r^{4}}{r^{4}}$$

-. Ratso of maximum velocity to Average Velocity = 2.

 $\frac{\overline{U_{man}}}{\overline{U}} = 2$ 

3-8

$$\overline{u} = \frac{1}{8n} \left( \frac{\partial p}{\partial x} \right) R^2$$

Integrating the above equation Nort X NE Get

- J dip = J 8 h u dx

$$\frac{(P_1 - P_2)}{R^2} = \frac{P_1 \overline{u}}{R^2} \left( x_2 - x_1 \right)$$

$$= \frac{g h \overline{u}}{R^2} L \left( x_2 - x_1 = L \right)$$

$$= \frac{g h \overline{u} L}{\left( \frac{D}{2} \right)^2}$$

Loss of Preserve head = P1-12 Pi-P2 - by = 1/2 pg p2

Pg p2

Wagen poiseuille fromla

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