



# **SNS COLLEGE OF TECHNOLOGY**

**Coimbatore-35**  
**An Autonomous Institution**



Accredited by NBA – AICTE and Accredited by NAAC – UGC with 'A+' Grade  
Approved by AICTE, New Delhi & Affiliated to Anna University, Chennai

## **DEPARTMENT OF ELECTRONICS & COMMUNICATION ENGINEERING**

### **16EC303–VLSI DESIGN**

III YEAR/ V SEMESTER

UNIT 1 –MOS TRANSISTOR PRINCIPLE

TOPIC 6 –MOS- NON IDEAL IV CHARACTERISTICS



## OUTLINE



- TRANSISTOR I-V REVIEW
- NONIDEAL TRANSISTOR BEHAVIOR
  - VELOCITY SATURATION
  - CHANNEL LENGTH MODULATION
  - BODY EFFECT
  - LEAKAGE
  - TEMPERATURE SENSITIVITY
- ACTIVITY
- PROCESS AND ENVIRONMENTAL VARIATIONS
  - PROCESS CORNERS
- ASSESSMENT
- SUMMARY



## IDEAL TRANSISTOR I-V

Shockley 1<sup>st</sup> order transistor models

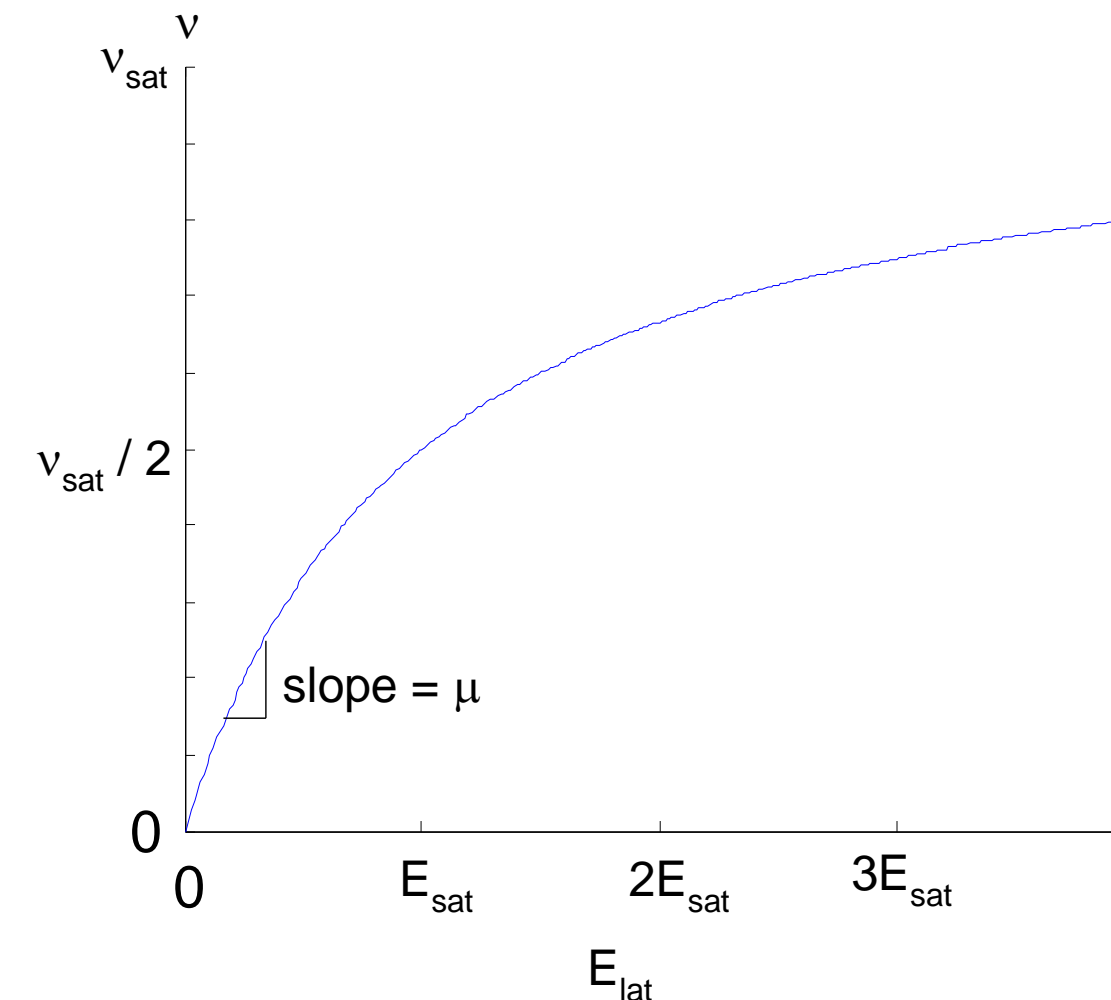
$$I_{ds} = \begin{cases} 0 & V_{gs} < V_t & \text{cutoff} \\ \beta \left( V_{gs} - V_t - \frac{V_{ds}}{2} \right) V_{ds} & V_{ds} < V_{dsat} & \text{linear} \\ \frac{\beta}{2} (V_{gs} - V_t)^2 & V_{ds} > V_{dsat} & \text{saturation} \end{cases}$$



## VELOCITY SATURATION



- We assumed carrier velocity is proportional to E-field
  - $v = \mu E_{lat} = \mu V_{ds}/L$
- At high fields, this ceases to be true
  - Carriers scatter off atoms
  - Velocity reaches  $v_{sat}$ 
    - Electrons:  $6-10 \times 10^6$  cm/s
    - Holes:  $4-8 \times 10^6$  cm/s
  - Better model





## VELOCITY SATURATION I-V EFFECTS



- Ideal transistor ON current increases with  $V_{DD}^2$

$$I_{ds} = \mu C_{ox} \frac{W}{L} \frac{(V_{gs} - V_t)^2}{2} = \frac{\beta}{2} (V_{gs} - V_t)^2$$

- Velocity-saturated ON current increases with  $V_{DD}$

$$I_{ds} = C_{ox} W (V_{gs} - V_t) v_{max}$$

- Real transistors are partially velocity saturated
  - Approximate with a-power law model
  - $I_{ds} \propto V_{DD}^a$
  - $-1 < a < 2$  determined empirically



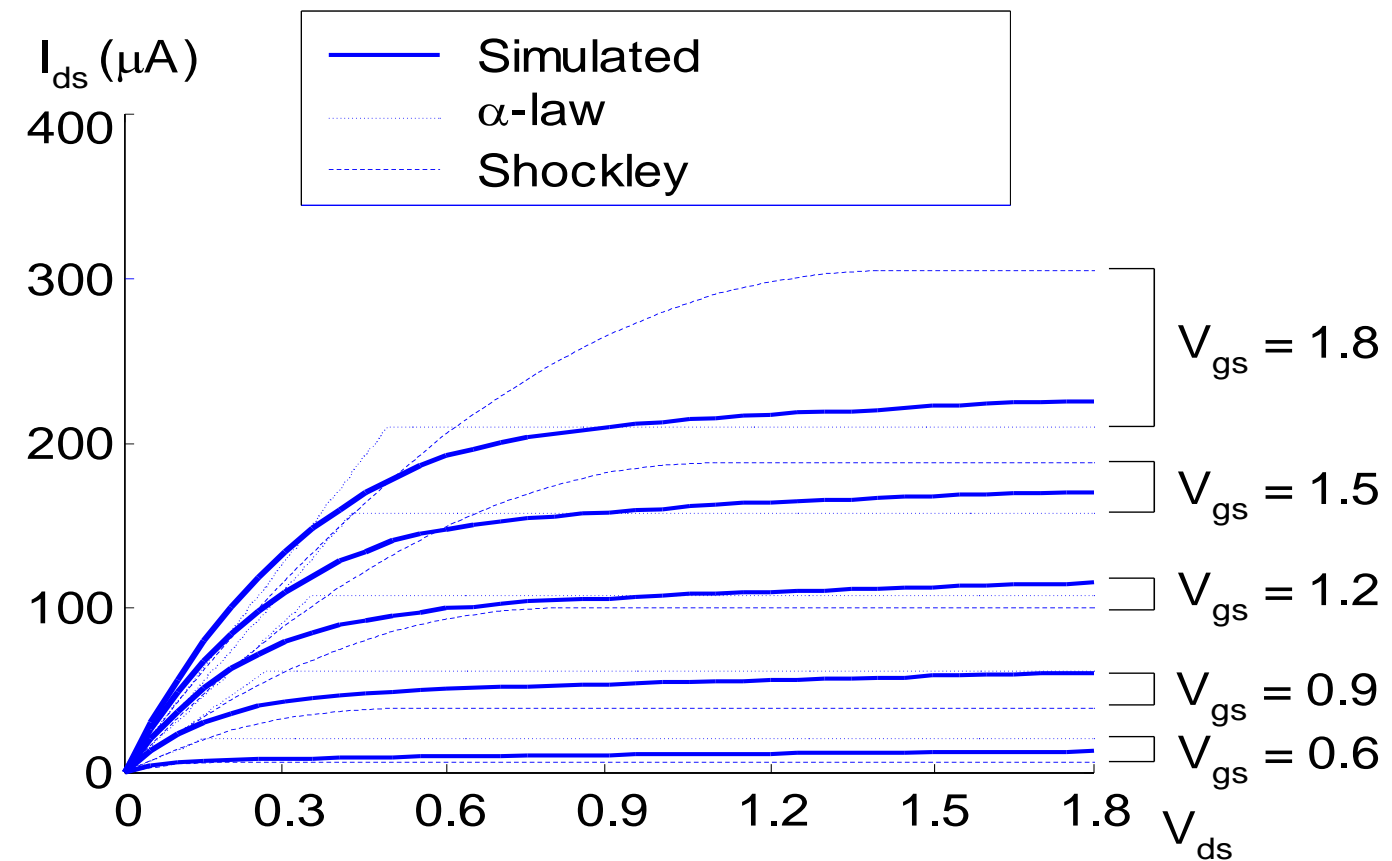
# $\alpha$ - POWER MODEL



$$I_{ds} = \begin{cases} 0 & V_{gs} < V_t & \text{cutoff} \\ I_{dsat} \frac{V_{ds}}{V_{dsat}} & V_{ds} < V_{dsat} & \text{linear} \\ I_{dsat} & V_{ds} > V_{dsat} & \text{saturation} \end{cases}$$

$$I_{dsat} = P_c \frac{\beta}{2} (V_{gs} - V_t)^\alpha$$

$$V_{dsat} = P_v (V_{gs} - V_t)^{\alpha/2}$$

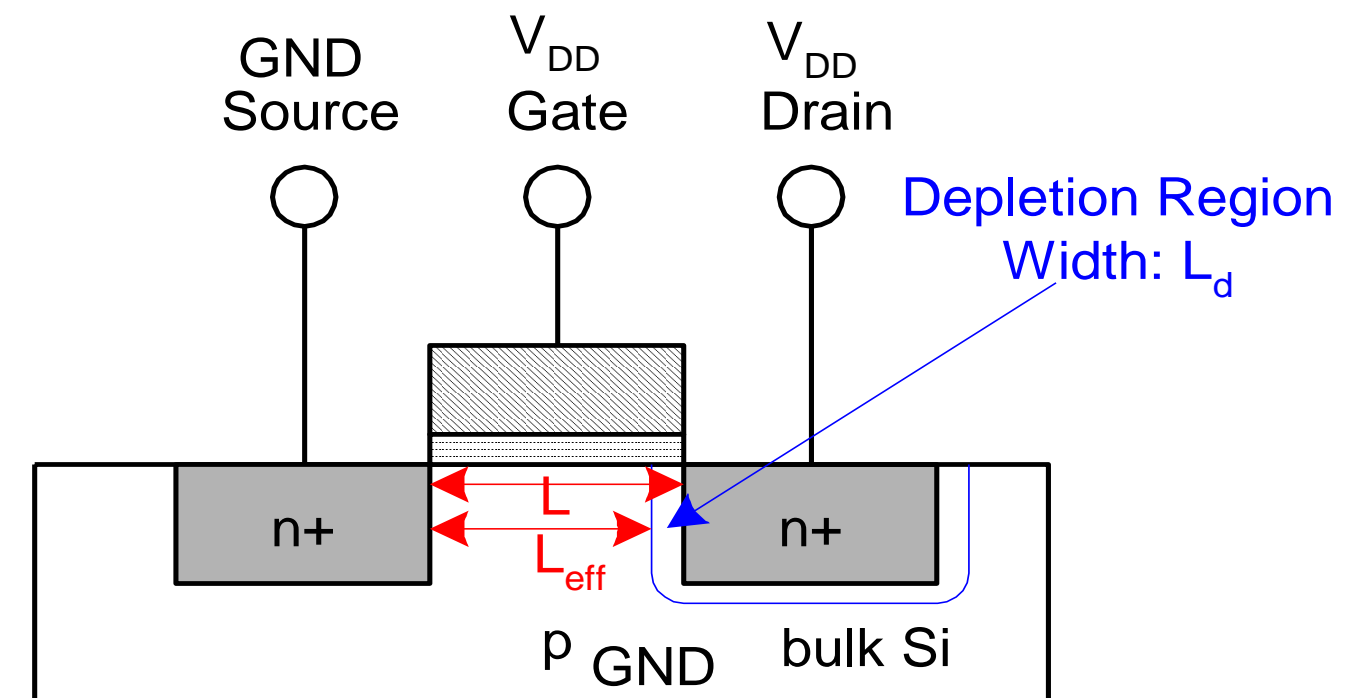




# CHANNEL LENGTH MODULATION



- Reverse-biased p-n junctions form a depletion region
  - Region between n and p with no carriers
  - Width of depletion  $L_d$  region grows with reverse bias
  - $L_{\text{eff}} = L - L_d$
- Shorter  $L_{\text{eff}}$  gives more current
  - $I_{\text{ds}}$  increases with  $V_{\text{ds}}$
  - Even in saturation

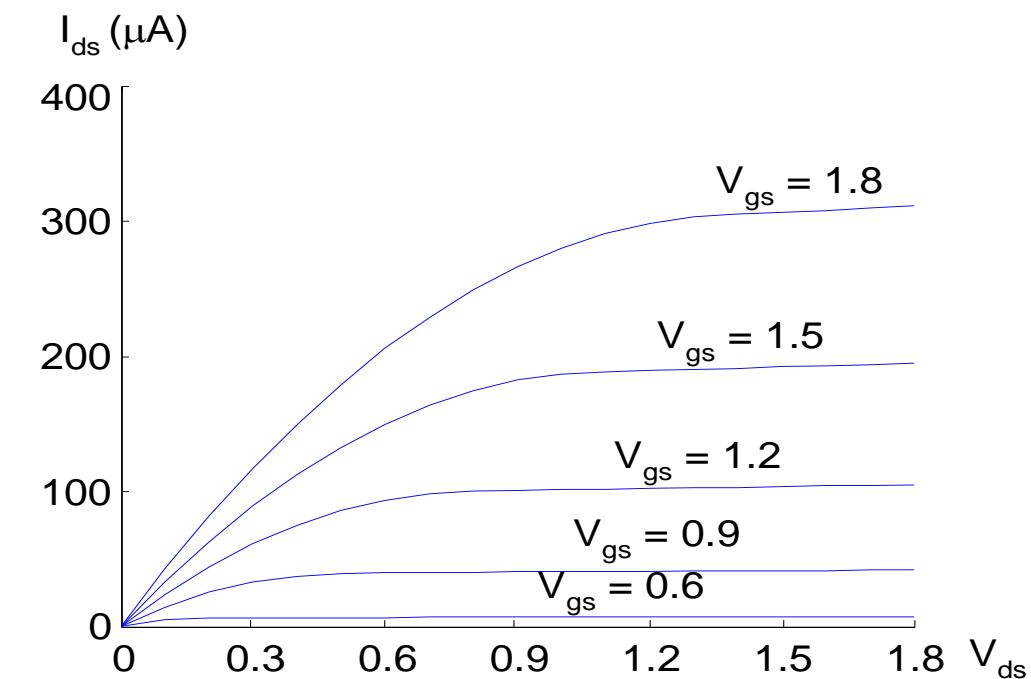




## CHAN.LENGTH MOD I-V



$$I_{ds} = \frac{\beta}{2} (V_{gs} - V_t)^2 (1 + \lambda V_{ds})$$



$\lambda$  = channel length modulation coefficient

- not feature size
- Empirically fit to I-V characteristics





## BODY EFFECT & BODY EFFECT MODEL



- $V_t$ : gate voltage necessary to invert channel
- Increases if source voltage increases because source is connected to the channel
- Increase in  $V_t$  with  $V_s$  is called the body effect

$$V_t = V_{t0} + \gamma \left( \sqrt{\phi_s + V_{sb}} - \sqrt{\phi_s} \right)$$

- $\phi_s = \text{surface potential at threshold}$   
$$\phi_s = 2v_T \ln \frac{N_A}{n_i}$$
  - Depends on doping level  $N_A$
  - intrinsic carrier concentration  $n_i$
- $\gamma = \text{body effect coefficient}$

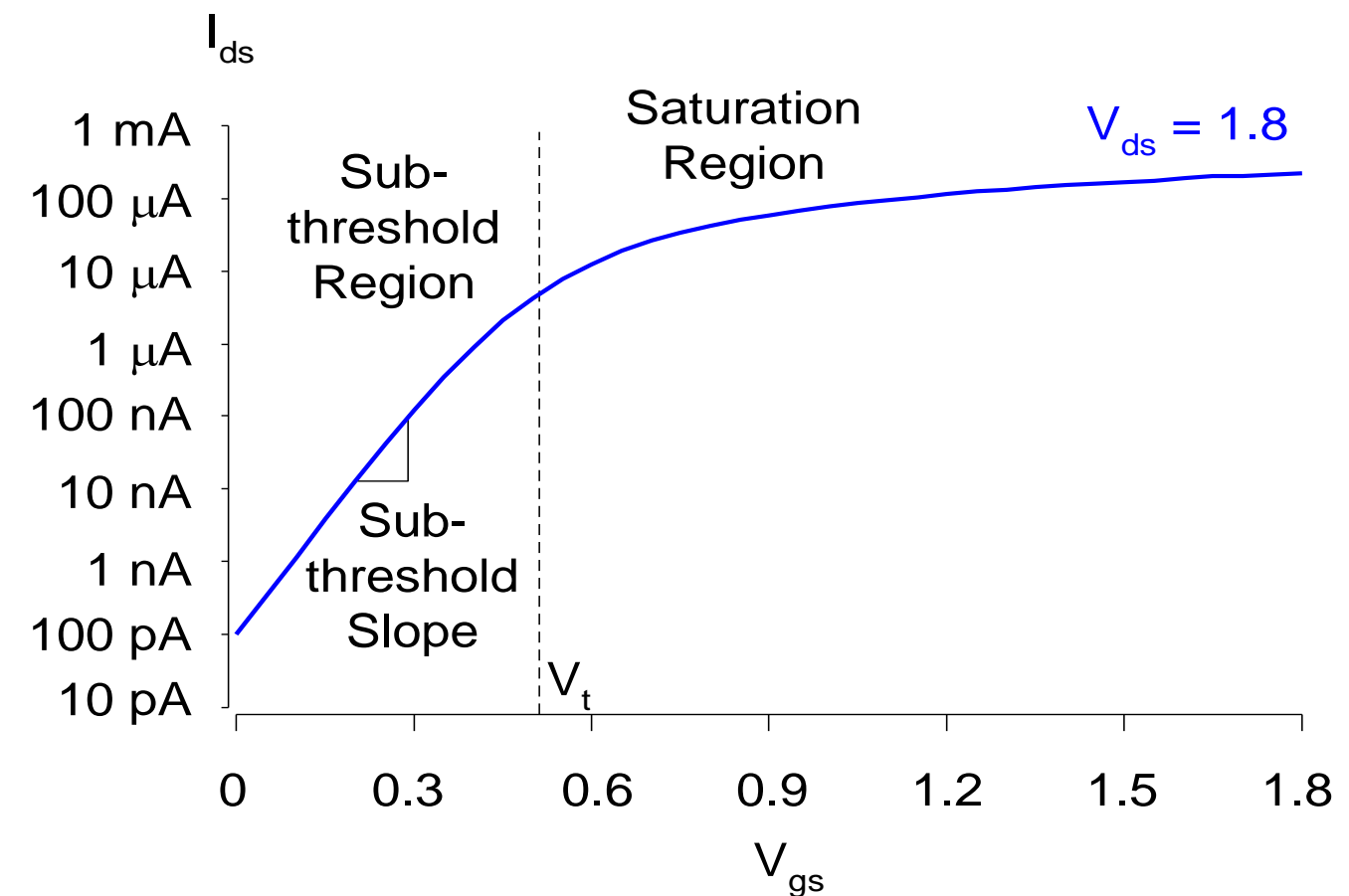
$$\gamma = \frac{t_{ox}}{\epsilon_{ox}} \sqrt{2q\epsilon_{si}N_A} = \frac{\sqrt{2q\epsilon_{si}N_A}}{C_{ox}}$$



# OFF TRANSISTOR BEHAVIOR



- What about current in cutoff?
- Simulated results
- What differs?
  - Current doesn't go to 0 in cutoff





## LEAKAGE SOURCES



- Subthreshold conduction
  - Transistors can't abruptly turn ON or OFF
- Junction leakage
  - Reverse-biased PN junction diode current
- Gate leakage
  - Tunneling through ultrathin gate dielectric
- Subthreshold leakage is the biggest source in modern transistors



## ACTIVITY



**Quick!** Count the number of times that the letter F appears in the following sentence:

“Finished files are the result of years of scientific study combined with the experience of years.”



## SUBTHRESHOLD LEAKAGE

- Subthreshold leakage exponential with  $V_{gs}$

$$I_{ds} = I_{ds0} e^{\frac{V_{gs} - V_t}{nV_T}} \left( 1 - e^{\frac{-V_{ds}}{V_T}} \right) \quad I_{ds0} = \beta v_T^2 e^{1.8}$$

- n is process dependent, typically 1.4-1.5



# DRAIN-INDUCED BARRIER LOWERING DIBL



- Drain-Induced Barrier Lowering
  - Drain voltage also affect  $V_t$

$$V_t' = V_t - \eta V_{ds}$$

- High drain voltage causes sub threshold leakage to increase.

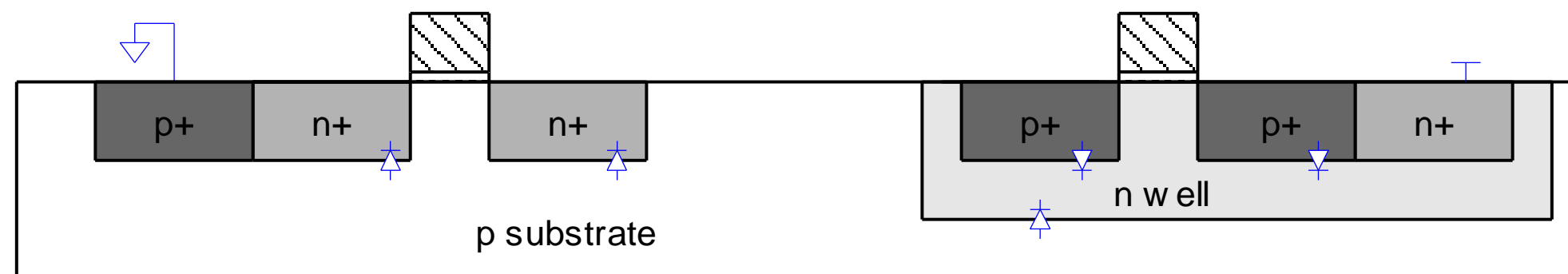


# JUNCTION LEAKAGE

- Reverse-biased p-n junctions have some leakage

$$I_D = I_S \left( e^{\frac{V_D}{V_T}} - 1 \right)$$

- $I_S$  depends on doping levels
  - And area and perimeter of diffusion regions
  - Typically  $< 1 \text{ fA/mm}^2$

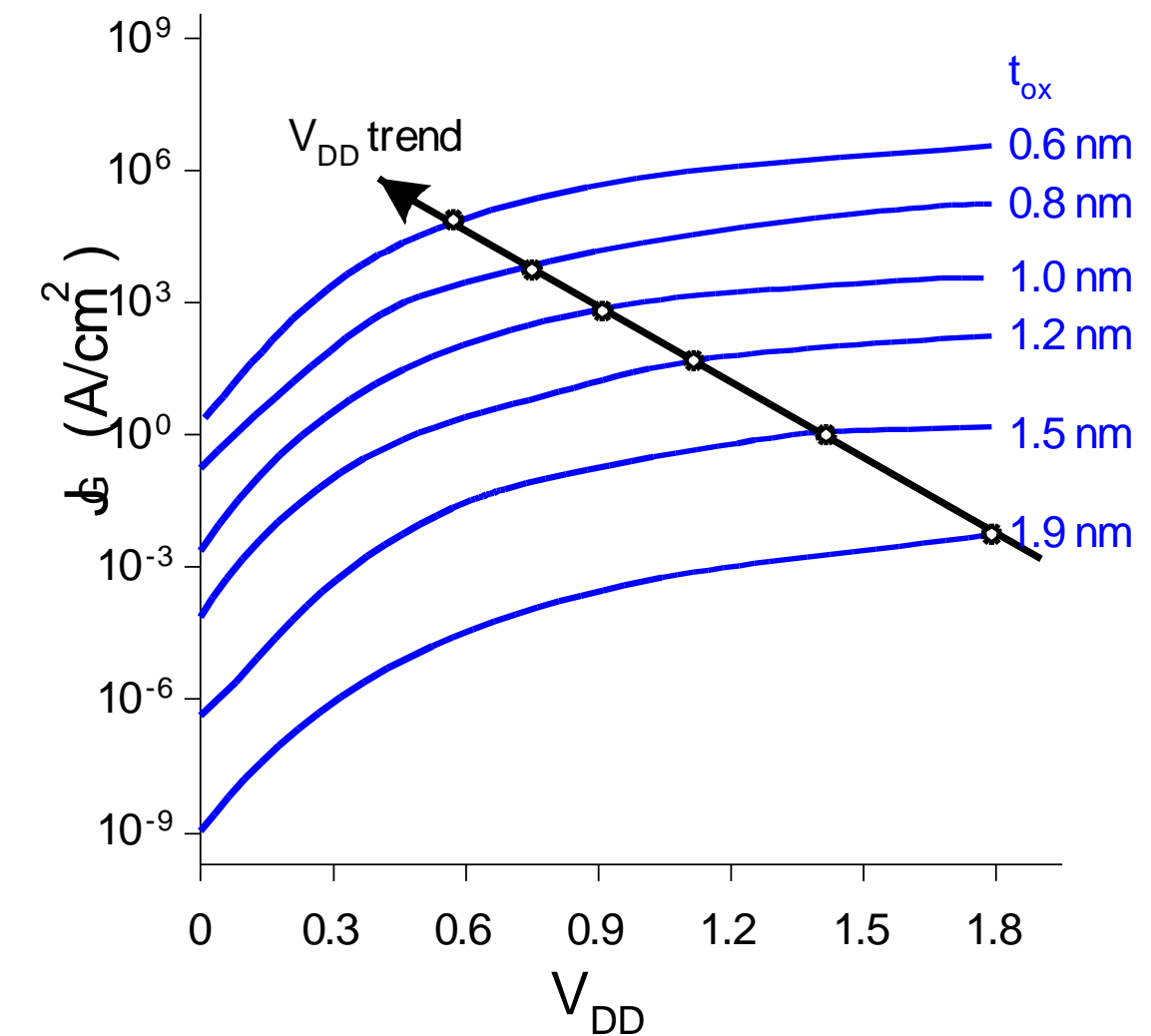




# GATE LEAKAGE



- Carriers may tunnel through very thin gate oxides
- Predicted tunneling current
- Negligible for older processes
- May soon be critically important



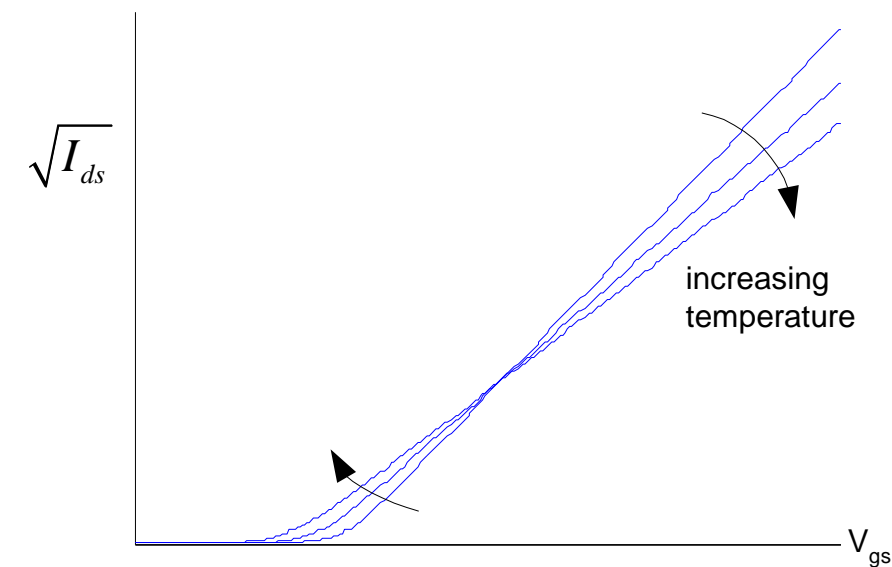




# TEMPERATURE SENSITIVITY



- Increasing temperature
  - Reduces mobility
  - Reduces  $V_t$
- $I_{ON}$  **decreases** with temperature
- $I_{OFF}$  **increases** with temperature





## SO WHAT?



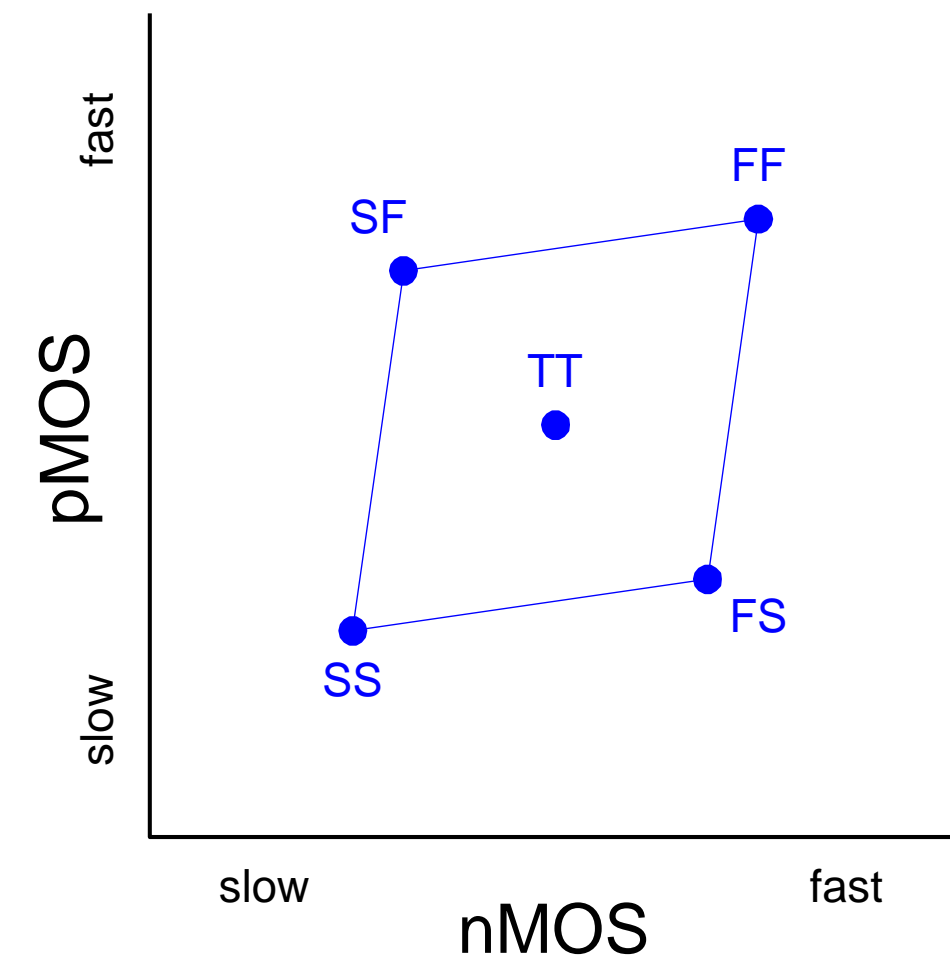
- So what if transistors are not ideal?
  - They still behave like switches.
- But these effects matter for...
  - Supply voltage choice
  - Logical effort
  - Quiescent power consumption
  - Pass transistors
  - Temperature of operation



# PARAMETER VARIATION



- Transistors have uncertainty in parameters
  - Process:  $L_{\text{eff}}$ ,  $V_t$ ,  $t_{\text{ox}}$  of nMOS and pMOS
  - Vary around typical (T) values
- Fast (F)
  - $L_{\text{eff}}$ : **short**
  - $V_t$ : **low**
  - $t_{\text{ox}}$ : **thin**
- Slow (S): opposite
- Not all parameters are independent for nMOS and pMOS





## ENVIRONMENTAL VARIATION



- $V_{DD}$  and  $T$  also vary in time and space
- Fast:
  - $V_{DD}$ : high
  - $T$ : low

Corner	Voltage	Temperature
F	1.98	0 C
T	1.8	70 C
S	1.62	125 C



# PROCESS CORNERS



- Process corners describe worst case variations
  - If a design works in all corners, it will probably work for any variation.
- Describe corner with four letters (T, F, S)
  - nMOS speed
  - pMOS speed
  - Voltage
  - Temperature



## IMPORTANT CORNERS



Some critical simulation corners include

<b>Purpose</b>	<b>nMOS</b>	<b>pMOS</b>	<b>V<sub>DD</sub></b>	<b>Temp</b>
Cycle time	S	S	S	S
Power	F	F	F	F
Subthreshold leakage	F	F	F	S
Pseudo-nMOS	S	F	?	?



# ASSESSMENT



1. Write the CHANNEL LENGTH MODULATION equation
2. Write the body effect derivation with its factors
3. In parameter Variation
  - Fast (F)

$-L_{\text{eff}}$ : -----  $V_t$ : -----  $t_{\text{ox}}$ : -----

4.

Purpose	nMOS	pMOS	$V_{DD}$	Temp
Cycle time	?	?	?	?
Power	?	?	?	?
Subthreshold leakage	?	?	?	?
Pseudo-nMOS	?	?	?	?



## SUMMARY & THANK YOU