



#### AN AUTONOMOUS INSTITUTION

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## **Topic: 3.2 – RADIUS OF CURVATURE**

4) find the radius of curvature at any point. (x,y) on y=c log sec %. Biven y= c log Sec %. gr (wg x) Y, = C. 1 . Sec X tan X. Sec X . d (Secx)= Secxtanz y1 = tan x e d (tanx)= sec2x y (x,y) = tan x. 92 = d'y = 1. Sec2x  $g = (1 + g_1^2)^2$  $= \left[ 1 + \tan^2 X \right]$ Sec<sup>2</sup> X/ 1/ Sec2 x g = C Sec<sup>3</sup>x Sec<sup>2</sup>x = C Sec x





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5. find the radius of curvature at (a, o) 9 CUENVR XY = a - x3 Adution: Gliven  $xy^2 = a^3 - x^3$ .  $y^2 = a^3 - x^2$ diff. w.r.t x'. g ay dy = - as - ax  $9_1 = \frac{-\chi^3}{2\chi^2 q} - \frac{\gamma}{\gamma}$  $y_1(a, o) = \infty$ hence we find  $d\pi$ ;  $\pi y^2 = a^3 - x^3$ UV=Vdu+udv  $x \, \partial y + y^2 \frac{dx}{dy} = 0 - 3x^2 \frac{dx}{dy} = \frac{v^2 - u - u \frac{dx}{dy}}{v^2}$ 2xy+(y2+3x2) dn =0  $\frac{dx}{dy} = \frac{-2xy}{3x^2+y^2}$   $\left(\frac{dx}{dy}\right)_{(a,o)} = 0 \longrightarrow 0$ Odiff wirt 1 y  $\frac{d^2 x}{dy^2} = (3x^2 + y^2) \left[ -\frac{\partial y}{\partial y} \frac{dx}{dy} - \frac{\partial x}{\partial y} \right] - (-\frac{\partial x}{\partial y}) \left[ \frac{\partial x}{\partial y} + \frac{\partial y}{\partial y} \right]$   $(3x^2 + y^2)^2$ 





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$$\begin{pmatrix} \frac{d^{2}x}{dy^{2}} \\ \frac{d^{2}x}{dy^{2}} \end{pmatrix}_{(a,0)} = \frac{(3a^{2}+o)[(o-2a)-o]}{(3a^{2}+o)^{2}} = \frac{-ba^{3}}{qa^{4}} = \frac{-2}{3a} \\ f = \begin{bmatrix} 1+(\frac{dx}{dy})^{2} \end{bmatrix}^{\frac{3}{2}} = \frac{(1+o)^{\frac{3}{2}}}{-\frac{2}{3}a} \\ f = \frac{1+(\frac{dx}{dy})^{2}}{\frac{d^{2}x}{dy^{2}}} = \frac{(1+o)^{\frac{3}{2}}}{-\frac{2}{3}a} \\ f = -\frac{2}{3}a \\ \frac{dy}{dx} = -\frac{2}{3}a \\ \frac{dy}{dx} = -\frac{2}{3}a \\ \frac{dy}{dx} = -\frac{2}{3}a \\ \frac{dy}{dx} = -\frac{2}{3}a \\ \frac{d^{2}y}{dx^{2}} = \frac{2}{3}a \\ f = (\frac{1+y_{1}}{y_{1}})^{\frac{3}{2}} \\ = \frac{(1+(-1)^{2})^{\frac{3}{2}}}{\frac{2}{3}} \\ = \frac{2}{3}a \\ f = c\sqrt{a} \\ f = c\sqrt{a} . \end{cases}$$





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pointly vature 6127 (Solution)  $u_1 v_2 + u_2 = (1+y_1^2)^2$ 6 42 Grì 9 = Sinh'z Sinhal Cosh y= a cosh wshal= Sinha y, = a sin h (x).1/2 = sinh/2 = with 2 2)  $S = (1 + sinh^2)$ = (cosh 2 cost = a. Losh x = a cost f= a cosh





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parametric to cartenian form:  
find the radius of curvature at any point  

$$x = a \cos^2 \theta$$
,  $y = a \sin^2 \theta$  m the curve  $x(^3 + g)^{\frac{3}{2}} a^{\frac{3}{2}} a^{\frac{3}{2}}$ .  
solution:  
Given  $x = a \cos^2 \theta$ ,  $y = a \sin^3 \theta$ .  
 $\frac{dw}{d\theta} = 3a \cos^2 \theta (-\sin \theta) = -3a \sin \theta \cos^2 \theta$ .  
 $\frac{dy}{d\theta} = 3a \sin^2 \theta \cos \theta = 3a \sin^2 \theta \cos \theta$ .  
 $\frac{dy}{d\theta} = 3a \sin^2 \theta \cos \theta = 3a \sin^2 \theta \cos \theta$ .  
 $\frac{dy}{d\theta} = \frac{dy}{d\theta} \cdot \frac{d\theta}{dx} = \frac{3a \sin^2 \theta \cos \theta}{-3a \cos^2 \theta \sin \theta}$ .  
 $\frac{d^2 y}{dx^2} = \frac{d}{d\theta} \left(\frac{dy}{dx}\right) \cdot \frac{d\theta}{dx} = \frac{d}{d\theta} (-tan\theta) \frac{d\theta}{d\pi}$ .  
 $= -\frac{\sec^2 \theta}{-3a \cos^2 \theta \sin \theta} = \frac{1}{3a \cos^2 \theta} \sin \theta$ .  
 $g = (1+y_1^2)^{\frac{3}{2}} = (1+tan^2 \theta)^{\frac{3}{2}}$ .  
 $= 3a \sin \theta \cos \theta$ .  
 $= 3a \sin \theta \cos \theta$ .  
 $g = \frac{3}{2} a \sin 2\theta$ .  
 $\int \sin^2 \theta = 3 \cos^2 \theta \sin \theta$ .  
 $\int \sin^2 \theta = 3 \cos^2 \theta \sin \theta$ .