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Topic: 3. 1 - CURVATURE AND RADIUS OF CURVATURE

the rate of change of bending of the curve in the given interval is called Courvature of the curve.

Note: (i) The curvature of a straight line is Zero.

(ii) the curvature of a point is infinity.

(iv) the curvature of a circle at any point on it is the same and is equal to the reciprocal of its radius.

Curvature is denoted by $K\left(-\frac{dV}{ds}\right)$





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Radius of curvature:

The reciprocal of the curvature of a curve at any point is called the radius of curvature at the point and is denoted by p

hence $g = \frac{1}{dS}$

Note: the curvature of a circle of radius or at any point is 1.

cartesian formula for the radius of curvature is $g = (1 + y_1^2)^{3/2}$

42





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1. Find the Radius of curvature of $y=e^{x}$ at (0,1) solution: Given $y=e^{x}$. $y_1 = \frac{dy}{dx} = e^{X} \Rightarrow y_{1(0,1)} = e^{-1}$ $y_2 = \frac{d^2y}{dw^2} = e^x \Rightarrow y_{2(0,1)} = e^0 = 1$ $\frac{1}{y_2} = \frac{(1+y_1^2)^{\frac{3}{2}}}{y_2} = \frac{(1+1)^{\frac{3}{2}}}{1} = \sqrt{\frac{3}{2}}$?. find the radius of curvature of the curve $\sqrt{x} + \sqrt{y} = \sqrt{a}$ at the point (24, 24).

polition: Given $\sqrt{x} + \sqrt{y} = \sqrt{a} \longrightarrow 0$ diff. w.r.t 'x => 1 + 1 dy =0. $\int \sqrt{x} \cdot \frac{1}{2\sqrt{y}} \frac{dy}{dx} - \sqrt{y} \cdot \frac{1}{2\sqrt{x}}$





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$$\frac{d^{2}y}{dx^{2}}(a_{x}^{2}, a_{x}^{2}) = -\left[\int_{-\frac{1}{2}}^{2}\frac{1}{4} \cdot \frac{1}{2\sqrt{2}}(a_{x}^{2}, a_{x}^{2})\right] = -\left[\int_{-\frac{1}{2}}^{2}\frac{1}{4} \cdot \frac{1}{4} \cdot$$