



SNS COLLEGE OF ENGINEERING

Kurumbapalayam (PO), Coimbatore - 641 107

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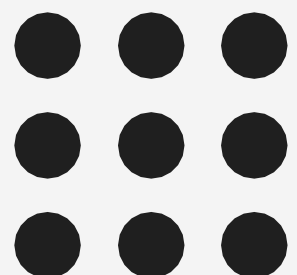
DEPARTMENT OF INFORMATION TECHNOLOGY

COURSE NAME: 19IT301 COMPUTER ORGANIZATION AND ARCHITECTURE

II YEAR/ III SEM

Unit 2 : ARITHMETIC OPERATIONS

Topic 6: Integer Division





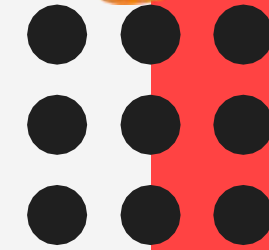
Manual Division

$$\begin{array}{r} 21 \\ \hline 13 \overline{) 274} \\ \underline{26} \\ 14 \\ \underline{13} \\ 1 \end{array}$$
$$\begin{array}{r} 10101 \leftarrow \text{Quotient} \\ \hline \text{Divisor } \rightarrow 1101 \overline{) 100010010} \leftarrow \text{Dividend} \\ \underline{1101} \\ 10000 \\ \underline{1101} \\ 1110 \\ \underline{1101} \\ 1 \leftarrow \text{Remainder} \end{array}$$

Longhand division examples.

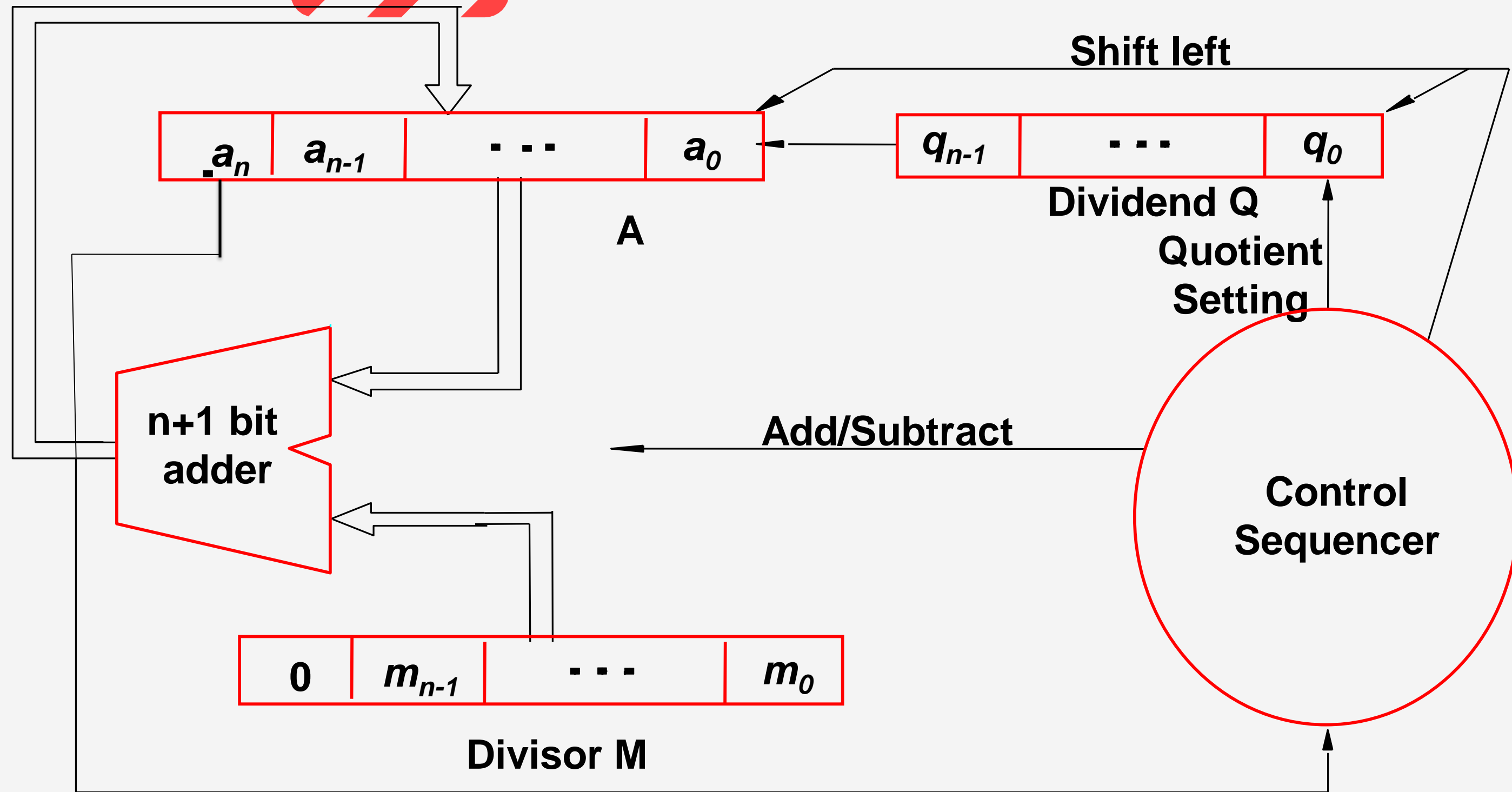


Longhand Division Steps



- Position the divisor appropriately with respect to the dividend and performs a subtraction.
- If the remainder is zero or positive, a quotient bit of 1 is determined, the remainder is extended by another bit of the dividend, the divisor is repositioned, and another subtraction is performed.
- If the remainder is negative, a quotient bit of 0 is determined, the dividend is restored by adding back the divisor, and the divisor is repositioned for another subtraction.

Circuit Arrangement



Logic circuit for restoring division

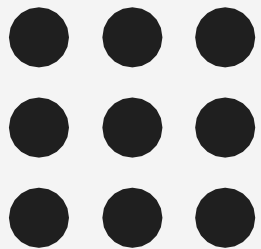


Restoring Division

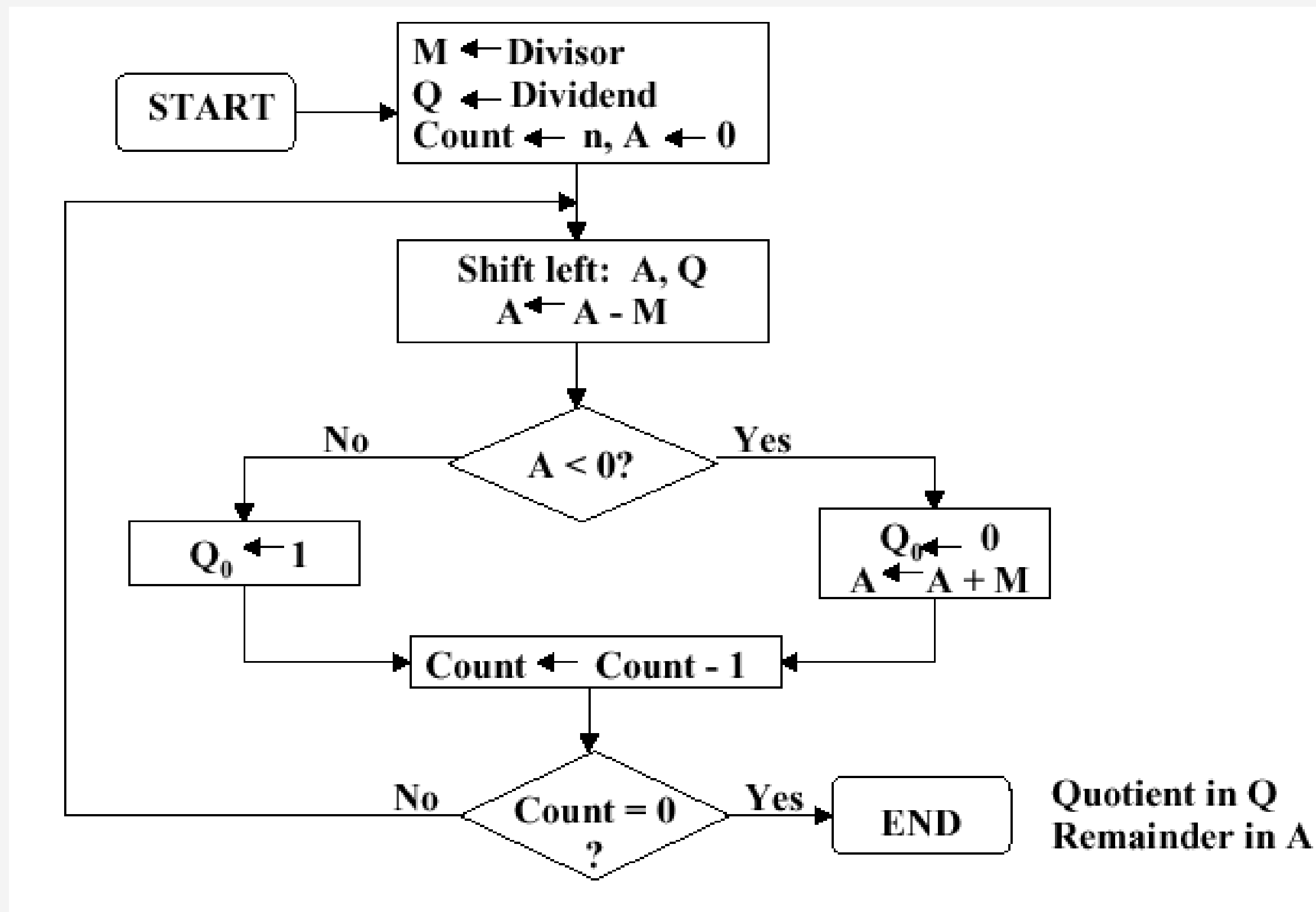
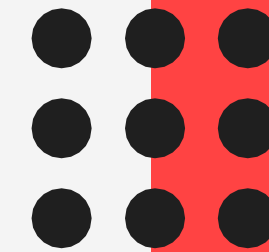


Algorithm

- Shift A and Q left one binary position
- Perform $A - M$, and place the answer back in A
- If the sign of A is 1, set q_0 to 0 and add M back to A (restore A); otherwise, set q_0 to 1
- Repeat these steps n times



Restoring division Flowchart





Example: Restoring Division

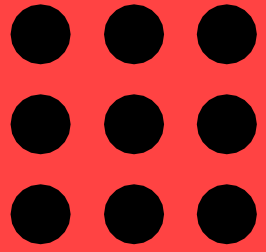


$$\begin{array}{r}
 10 \\
 11 \overline{) 1000} \\
 \underline{11} \\
 10
 \end{array}$$

	A	Q(Dividend)	Count
Initially	0 0 0 0 0	1 0 0 0	4
M	0 0 0 1 1		
Shift	0 0 0 0 1	0 0 0 <input type="text"/>	
Subtract	1 1 1 0 1		
Set q_0	1 1 1 1 0		First cycle
Restore	0 0 0 0 1	0 0 0 0	3
Shift	0 0 0 1 0	0 0 0 <input type="text"/>	
Subtract	1 1 1 0 1		
Set q_0	1 1 1 1 1		Second cycle
Restore	0 0 0 1 0	0 0 0 0	2
Shift	0 0 1 0 0	0 0 0 <input type="text"/>	
Subtract	1 1 1 0 1		
Set q_0	0 0 0 0 1		Third cycle
Shift	0 0 0 1 0	0 0 0 1	1
Subtract	1 1 1 0 1	0 0 1 <input type="text"/>	
Set q_0	1 1 1 1 1		Fourth cycle
Restore	0 0 0 1 0	0 0 1 0	0

Remainder
Quotient

SNSCE / IT/ V Sem/V Vaishnav
AP-IT



Nonrestoring Division



- Avoid the need for restoring A after an unsuccessful subtraction.
- Any idea?

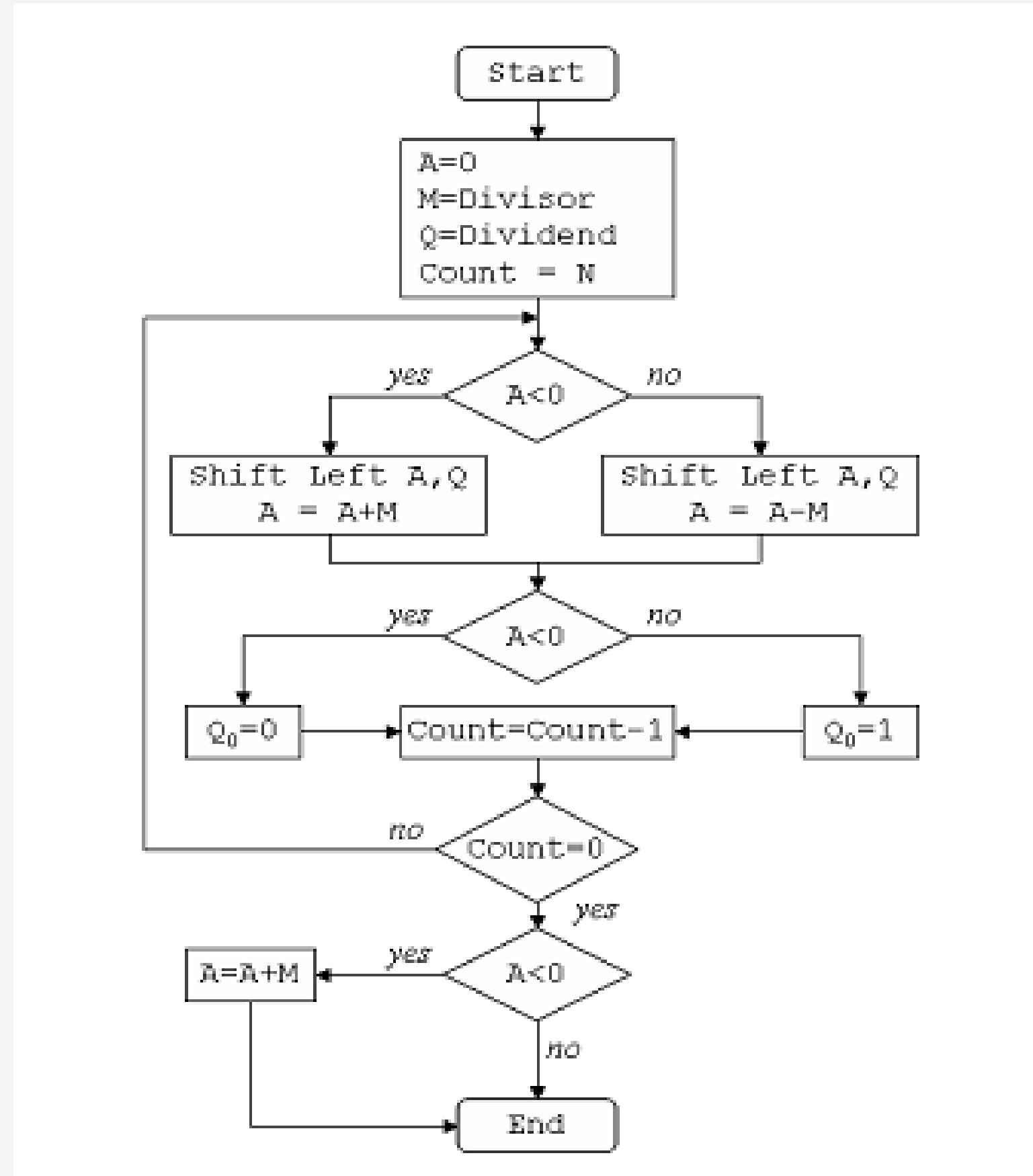
Step 1: (Repeat n times)

- If the sign of A is 0, shift A and Q left one bit position and subtract M from A; otherwise, shift A and Q left and add M to A.
- Now, if the sign of A is 0, set q_0 to 1; otherwise, set q_0 to 0.

Step2: If the sign of A is 1, add M to A



Nonrestoring division Flowchart





A nonrestoring-division example



$$\begin{array}{r}
 11111 \\
 00011 \\
 \hline
 \text{Add } 00010 \\
 \hline
 \text{Remainder}
 \end{array}$$

Restore remainder

M = 00011
 2's complement of M = 11101

	A	Q(Dividend)	Count
Initially	0 0 0 0 0	1 0 0 0	4
M	0 0 0 1 1		
Shift	0 0 0 0 1	0 0 0 <input type="checkbox"/>	First cycle
Subtract	1 1 1 0 1		
Set q_0	1 1 1 1 0	0 0 0 <input type="checkbox"/>	
Shift	1 1 1 0 0	0 0 <input type="checkbox"/> <input type="checkbox"/>	Second cycle
Add	0 0 0 1 1		
Set q_0	1 1 1 1 1	0 0 <input type="checkbox"/> <input type="checkbox"/>	
Shift	1 1 1 1 0	0 <input type="checkbox"/> <input type="checkbox"/> <input type="checkbox"/>	Third cycle
Add	0 0 0 1 1		
Set q_0	0 0 0 0 1	0 <input type="checkbox"/> <input type="checkbox"/> <input type="checkbox"/> <input type="checkbox"/>	
Shift	0 0 0 1 0	<input type="checkbox"/> <input type="checkbox"/> <input type="checkbox"/> <input type="checkbox"/>	Fourth cycle
Subtract	1 1 1 0 1		
Set q_0	1 1 1 1 1	<input type="checkbox"/> <input type="checkbox"/> <input type="checkbox"/> <input type="checkbox"/>	

Quotient



Division of signed operands

- No simple algorithms for performing division of signed operands

Solution

- Transform the operands to positive values, use either restoring or non-restoring algorithm
- Transform the result to correct signed values



Exercise



Compute $27/11$ using restoring and non-restoring algorithm



Thank You