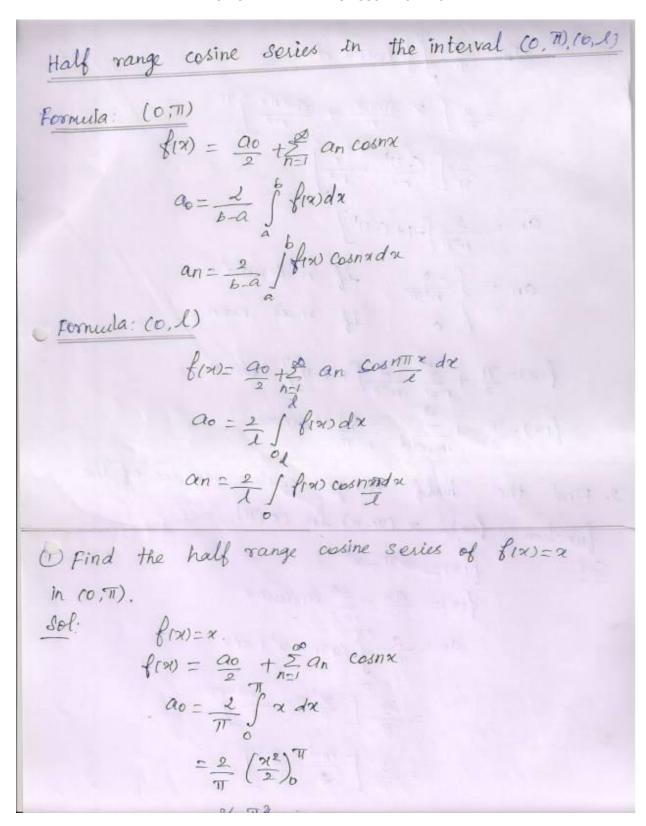




#### **TOPIC: 7 – HALF RANGE COSINE SERIES**







$$a_{n} = \frac{2}{\pi} \int_{-\infty}^{\infty} x \cos nx \, dx$$

$$= \frac{2}{\pi} \left[ \frac{x \sin nx}{n} + \frac{\cos nx}{n^{2}} \right]^{\frac{1}{17}}$$

$$= \frac{2}{\pi} \left[ \frac{(-1)^{n}}{n^{2}} - \frac{1}{n^{2}} \right]$$

$$a_{n} = \frac{2}{n^{2}\pi} \left[ -1 + (-1)^{n} \right]$$

$$a_{n} = \int_{-\infty}^{\infty} \frac{4}{n^{2}\pi} \int_{-\infty}^{\infty} 1 - (-n)^{n} \int_{-\infty}^{\infty} \cos nx \, dx$$

$$f(x) = \frac{\pi}{2} + \sum_{n=1}^{\infty} \frac{2}{n^{2}\pi} \left[ 1 - (-n)^{n} \right] \cos nx$$

$$f(x) = \frac{\pi}{2} + \sum_{n=1}^{\infty} \frac{4}{n^{2}\pi} \int_{-\infty}^{\infty} \cos nx \, dx$$

$$f(x) = \frac{\pi}{2} + \sum_{n=1}^{\infty} \frac{4}{n^{2}\pi} \cos nx$$

$$f(x) = x (\pi - x) \text{ in } (0, \pi).$$
Sol:
$$f(x) = x (\pi - x) \text{ in } (0, \pi).$$

$$f(x) = x (\pi - x) \text{ in } (0, \pi).$$

$$f(x) = \frac{a_{0}}{2} + \sum_{n=1}^{\infty} a_{n} \cos nx$$

$$a_{0} = \frac{2}{\pi} \int_{-\infty}^{\infty} (2\pi - x^{2}) \, dx$$

$$= \frac{2}{\pi} \left[ \frac{x^{2}\pi}{2} - \frac{x^{2}}{3} \right]_{0}^{\pi}$$

$$= \frac{2}{\pi} \left[ \frac{\pi^{3}}{2} - \frac{\pi^{3}}{3} \right]_{0}^{\pi}$$





$$a_{n} = \frac{2}{\pi} \int_{-\infty}^{\infty} x \cos nx \, dx$$

$$= \frac{2}{\pi} \left[ \frac{x \sin nx}{n} + \frac{\cos nx}{n^{2}} \right]_{0}^{\pi}$$

$$= \frac{2}{\pi} \left[ \frac{(-1)^{n}}{n^{2}} - \frac{1}{n^{2}} \right]$$

$$a_{n} = \frac{2}{n^{2}\pi} \left[ -1 + (-1)^{n} \right]$$

$$a_{n} = \int_{-\infty}^{\infty} \frac{4}{n^{2}\pi} \sin \theta \sin \theta$$

$$e^{-\frac{\pi}{n^{2}\pi}} \int_{0}^{\infty} e^{-\frac{\pi}{n^{2}\pi}} e^{-\frac{\pi}{n^{2}\pi}} \int_{0}^{\infty} e^{-\frac{\pi}{n^{2}\pi}} \int_{0}^{\infty} e^{-\frac{\pi}{n^{2}\pi}} e^{-\frac{\pi}{n^{2}\pi}} \int_{0}^{\infty} e^{-\frac{\pi}{n^{2}\pi}} e^{-\frac{\pi}{n^{2}\pi}} \int_{0}^{\infty} e^{-\frac{\pi}{n^{2}\pi}} e^{-\frac{\pi}{n^{2}\pi}} \int_{0}^{\infty} e^{-\frac{\pi}{n^{2}\pi}} e^{-\frac{\pi}{n^$$





$$a_{n} = \frac{2}{\pi} \int_{0}^{\pi} (x \pi_{-} x^{2}) \cos nx \, dx$$

$$u = x\pi_{-} x^{2} \qquad \int dv = \int \cos nx \, dx$$

$$u_{1} = \pi_{-} 2x \qquad v = \frac{\sin nx}{n}$$

$$u_{2} = -2 \qquad v_{1} = -\frac{\cos nx}{n^{2}}$$

$$u_{3} = 0 \qquad v_{2} = -\frac{g \sin nx}{n^{2}}$$

$$d_{1} = \frac{2}{\pi} \left[ -\pi - x^{2} \right] \frac{\sin nx}{n} + (\pi_{-} 2x) \frac{\cos nx}{n^{2}}$$

$$+ 2 \frac{g \sin nx}{n^{3}} \int_{0}^{\pi}$$

$$= \frac{2}{\pi} \left[ -\pi - \frac{(-1)^{n}}{n^{2}} \right]$$

$$= \frac{2\pi}{\pi} \left[ -(-1)^{n} \right]$$

$$= -\frac{2}{n^{2}} \left[ 1 + (-1)^{n} \right]$$

$$a_{1} = \int_{0}^{\pi} \int_{0}^{\pi} \sin x \, dx$$

$$\int_{0}^{\pi} \sin x \, dx$$





$$a_0 = \frac{2}{1} \int_{0}^{\infty} f(x) dx$$

$$= 2 \int_{0}^{\infty} (x-1)^{2} dx$$

$$= 2 \int_{0}^{\infty} (x-1)^{2} \int_{0}^{\infty} f(x) \cos n\pi x dx$$

$$= 2 \int_{0}^{\infty} (x-1)^{2} \cos n\pi x dx$$

$$u = (x-1)^{2} \int_{0}^{\infty} dx \int_{0}^{\infty} dx$$

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$$u = 2 \int_{0}^{\infty} (x-1)^{2} \int_{0}^{\infty} dx \int_{0}^{\infty} dx$$

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$$v = \int_{0}^{\infty} dx \int_{0}^{\infty} dx \int_{0}^{\infty} dx$$

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$$v = \int_{0}^{\infty} dx \int_{0}^$$