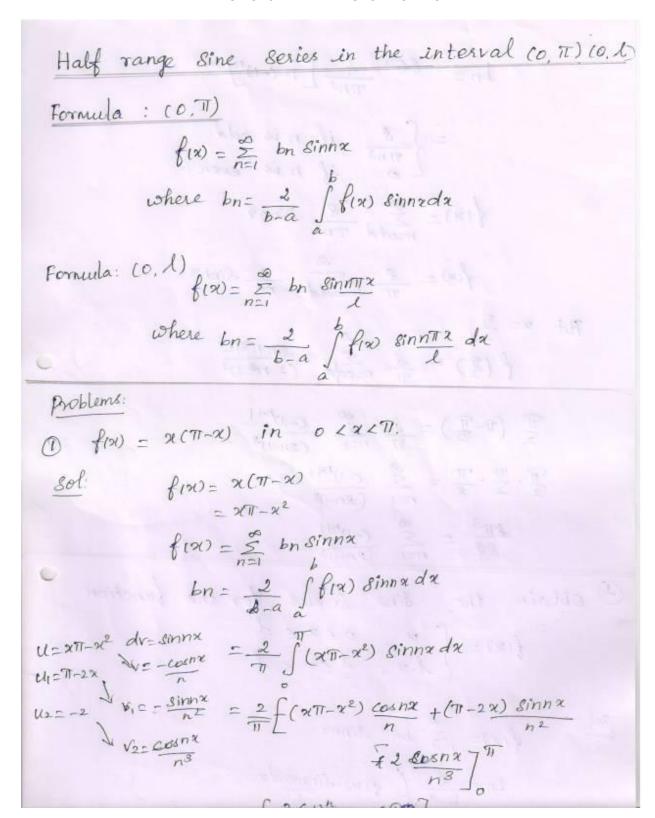




#### **TOPIC: 6 - HALF RANGE SINE SERIES**







$$b_{n} = \frac{8}{T \ln^{3}} \left[ 1 - (-1)^{n} \right]$$

$$= \begin{cases} \frac{8}{T \ln^{3}} & \text{if } n \text{ is odd} \\ \frac{8}{T \ln^{3}} & \text{if } n \text{ is even} \end{cases}$$

$$\begin{cases} (\pi) = \frac{8}{T} & \frac{8}{\pi 2 \text{odd}} & \frac{1}{\pi^{3}} & 8 \text{inn} 2 \\ \frac{8}{T \ln^{3}} & \frac{8}{\pi^{3}} & \frac{8}{\pi^{3}} & \frac{8}{\pi^{3}} & \frac{8}{\pi^{3}} \end{cases}$$

$$R_{\text{II}} \propto = \frac{\pi}{2}$$

$$f\left(\frac{\pi}{2}\right) = \frac{8}{T} & \frac{5}{\pi^{2}} & \frac{6 \ln \pi}{(2n-1)^{3}}$$

$$\frac{\pi}{2} \cdot \frac{\pi}{2} \cdot \frac{\pi}{8} = \frac{8}{5} \cdot \frac{(-1)^{n+1}}{(2n-1)^{3}}$$

$$\frac{R_{\text{II}}}{2} = \frac{8}{5} \cdot \frac{(-1)^{n+1}}{(2n-1)^{3}}$$

$$\frac{$$





$$u_{1}=1$$

$$v_{2}=-\frac{\cos n\pi x}{2}$$

$$u_{1}=1$$

$$v_{2}=-\frac{\sin n\pi x}{2}$$

$$u_{2}=0$$

$$v_{1}=-\frac{\sin n\pi x}{2}$$

$$u_{2}=0$$

$$v_{1}=-\frac{\sin n\pi x}{2}$$

$$\frac{(n\pi)^{2}}{(n\pi)^{2}}$$

$$v_{2}=0$$

$$v_{3}=-\frac{\sin n\pi x}{2}$$

$$v_{4}=-\frac{\sin n\pi x}{2}$$

$$v_{5}=-\frac{\sin n\pi x}{2}$$

$$v_{7}=-\frac{\sin n\pi x}{2}$$

$$v_{1}=-\frac{\sin n\pi x}{2}$$

$$v_{2}=0$$

$$v_{3}=-\frac{\sin n\pi x}{2}$$

$$v_{4}=-\frac{\sin n\pi x}{2}$$

$$v_{5}=-\frac{\sin n\pi x}{2}$$

$$v_{6}=-\frac{\sin n\pi x}{2}$$

$$v_{7}=-\frac{\sin n\pi x}{2}$$

$$v_{8}=-\frac{\sin n\pi x}{2}$$

$$v_{8}=-\frac{\sin n\pi x}{2}$$

$$v_{8}=-\frac{\sin n\pi x}{2}$$

$$v_$$









$$a_{n} = \frac{2}{\pi} \int_{-\pi}^{\pi} x \cos nx \, dx$$

$$= \frac{2}{\pi} \left[ \frac{x \sin nx}{n} + \frac{\cos nx}{n^{2}} \right]^{\pi}$$

$$= \frac{2}{\pi} \left[ \frac{(-1)^{n}}{n^{2}} - \frac{1}{n^{2}} \right]$$

$$a_{n} = \frac{2}{n^{2}\pi} \left[ -1 + (-1)^{n} \right]$$

$$a_{n} = \int_{-\pi^{2}\pi}^{\pi} \left[ -1 + (-1)^{n} \right]$$

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$$a_{n} = \int_{-\pi^{2}\pi}^{\pi} \left[ -1 + (-1)^{n} \right] \cos nx$$

$$f(x) = \frac{\pi}{2} + \sum_{n=1}^{\infty} \frac{2}{n^{2}\pi} \left[ -1 + (-1)^{n} \right] \cos nx$$

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$$f(x) = \frac{\pi}{2} + \sum_{n=1}^{\infty} a_{n} \cos nx$$

$$f(x) = x (\pi - x) \text{ in } (0, \pi).$$

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$$f(x) = \frac{2}{\pi} \int_{-\pi^{2}\pi}^{\pi} (x\pi - x^{2}) \, dx$$

$$= \frac{2}{\pi} \left[ \frac{x^{2}\pi}{2} - \frac{x^{2}}{3} \right]_{0}^{\pi}$$

$$= \frac{2}{\pi} \left[ \frac{\pi^{2}}{2} - \frac{\pi^{2}}{3} \right]_{0}^{\pi}$$

$$= \frac{2}{\pi} \left[ \frac{\pi^{2}}{2} - \frac{\pi^{2}}{3} \right]_{0}^{\pi}$$