

Leftmost  
~~abbede~~  
~~aebcbd~~ (A → b)  
 aAbedde (A → Abc)  
 aAde (B → d)  
 aABe (S → aABe)  
 s.

write all  
 terminal  
 first.

Right most.  
 S → aABe  
 → aAde  
 → aABcd e  
 → abbcd e.

write first  
 production rule  
 of grammar.

Handle punning:

$E \rightarrow E + E \mid E \rightarrow id.$

IP string : id + id + id.

$E \Rightarrow E + E$   
 $E \Rightarrow_{rm} E + E + E$   
 $E \Rightarrow_{rm} E + E + id \quad (E \rightarrow id)$   
 $E \Rightarrow_{rm} E + E + id \quad (E \rightarrow id)$   
 $E \Rightarrow_{rm} E + id + id \quad (E \rightarrow id)$   
 $E \Rightarrow_{rm} id + id + id.$

$E \Rightarrow E + E \quad (E \rightarrow E + E)$   
 $E \Rightarrow_{lm} E + E + E \quad (E \rightarrow id)$   
 $E \Rightarrow_{lm} id + E + E \quad (E \rightarrow id)$   
 $E \Rightarrow_{lm} id + id + E \quad (E \rightarrow id)$   
 $E \Rightarrow_{lm} id + id + id.$

Operator precedence:- parsing.

→ An efficient & easy way of constructing a shift-reduce parser is called operator-precedence parsing.

→ It can be constructed from a grammar called operator precedence.



Eg: consider the grammar.

$\leftarrow \rightarrow$  shift  
 $\rightarrow \rightarrow$  pop.

$$E \rightarrow EAE \mid (E) \mid \text{id}$$

$$A \rightarrow + \mid - \mid * \mid / \mid \text{id} \quad \boxed{\text{I/p string id+id*id}}$$

$$E \rightarrow E + E \mid E * E \mid E - E \mid E / E \mid E \uparrow E \mid (E) \mid \text{id}$$

Rules to find operator precedence:

- 1)  $\uparrow$  is of highest precedence & right associative ( $\leftarrow$ )
- 2)  $*$  and  $/$  are next highest & left associative ( $\rightarrow$ )
- 3)  $+$  and  $-$  are lowest & left associative ( $\rightarrow$ ).
- 4) equal precedence ( $\rightarrow$ ).
- 5) id ( $\leftarrow$ ) (b)  $\$$  ( $\rightarrow$ ), ( ) ( $\leftarrow$ ) ( ) ( $\rightarrow$ ).

$+, -, *, / \rightarrow$  Left associative.

$*$  and  $/$  higher precedence than  $+, -$

	+	-	*	/	$\uparrow$	id	(	)	\$
+	$\rightarrow$	$\rightarrow$	$\leftarrow$	$\leftarrow$	$\leftarrow$	$\leftarrow$	$\leftarrow$	$\rightarrow$	$\rightarrow$
-	$\rightarrow$	$\rightarrow$	$\leftarrow$	$\leftarrow$	$\leftarrow$	$\leftarrow$	$\leftarrow$	$\rightarrow$	$\rightarrow$
*	$\rightarrow$	$\rightarrow$	$\rightarrow$	$\rightarrow$	$\leftarrow$	$\leftarrow$	$\leftarrow$	$\rightarrow$	$\rightarrow$
/	$\rightarrow$	$\rightarrow$	$\rightarrow$	$\rightarrow$	$\leftarrow$	$\leftarrow$	$\leftarrow$	$\rightarrow$	$\rightarrow$
$\uparrow$	$\rightarrow$	$\rightarrow$	$\rightarrow$	$\rightarrow$	$\leftarrow$	$\leftarrow$	$\leftarrow$	$\rightarrow$	$\rightarrow$
id	$\rightarrow$	$\rightarrow$	$\rightarrow$	$\rightarrow$	$\rightarrow$	$\leftarrow$	$\leftarrow$	$\rightarrow$	$\rightarrow$
(	$\leftarrow$	$\leftarrow$	$\leftarrow$	$\leftarrow$	$\leftarrow$	$\leftarrow$	$\leftarrow$	$\rightarrow$	$\rightarrow$
)	$\rightarrow$	$\rightarrow$	$\rightarrow$	$\rightarrow$	$\rightarrow$	$\rightarrow$	$\rightarrow$	$\rightarrow$	$\rightarrow$
\$	$\leftarrow$	$\leftarrow$	$\leftarrow$	$\leftarrow$	$\leftarrow$	$\leftarrow$	$\leftarrow$	$\rightarrow$	$\rightarrow$



Stack.		Input string	Comment.
	<	id + id * id \$	shift id.
\$id	>	+ id * id \$	pop the top of the stack id.
\$	<	+ id * id \$	shift +
\$ +	<	id * id \$	shift id.
\$ + id	>	* id \$	pop id.
\$ +	<	* id \$	pop id. shift *
\$ + *	<	id \$	shift id. id
\$ + * id	>	\$	pop id
\$ + *	>	\$	pop *
\$ +	>	\$	pop +
\$		\$	Accepted.

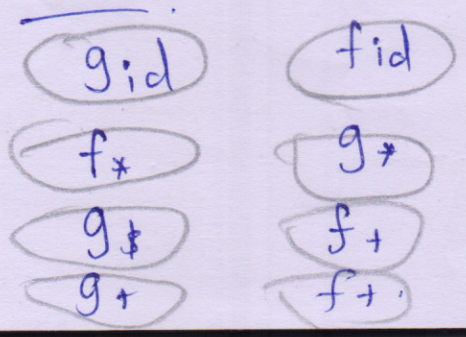
Precedence Relation matrix

	id	+	*	\$
id	-	>	>	>
+	<	>	<	>
*	<	>	>	>
\$	<	<	<	-

Create symbol!

f<sub>id</sub>, f<sub>+</sub>, f<sub>\*</sub>, f<sub>\$</sub>  
 g<sub>id</sub>, g<sub>+</sub>, g<sub>\*</sub>, g<sub>\$</sub>

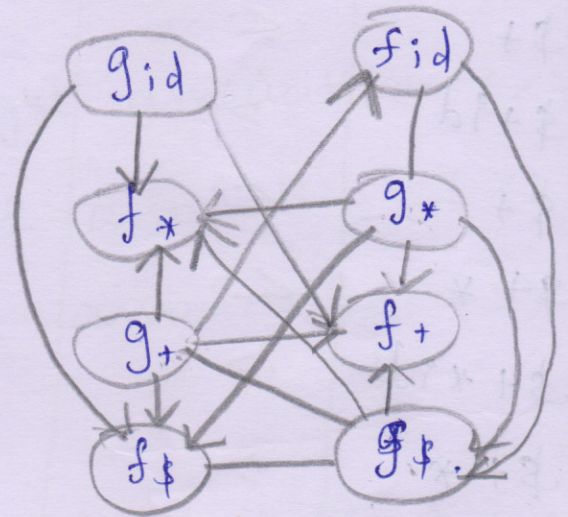
create node!





place the following edges:-

- + < id, edges from gid to f+
- + < \*, edges from g\* to f+
- + > \$, edges from g\$ to f+ ✓
- \* < id, edges from gid to f\*
- \* > +, edges from g+ to f\*
- \* > \$, edges from g\$ to f\*
- \$ < id, edges from gid to f\$
- \$ < +, edges from g+ to f\$
- \$ < \*, edges from g\* to f\$
- id > \$, edges from g\$ to fid ✓
- id > +, edges from g+ to fid ✓
- id > \*, edges from g\* to fid ✓
- + > +, edges from g+ to f+
- \* > \*, edges from g\* to f\*



Ex2:

	+	*	id	\$
f	2	4	1	3
g	1	3	2	1



LR  parsing: (Left to Right).

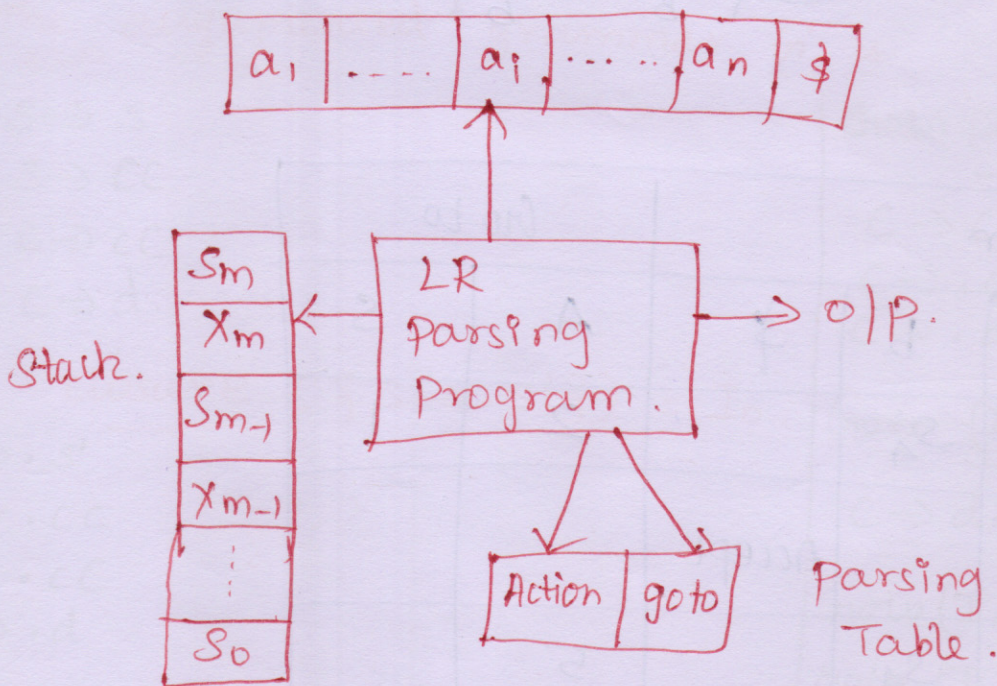
(14)

→ Bottom up syntax analysis technique that can be used to parse a large class of CFG is called LR(K) parsing.

Types of LR  parsing methods:

- ① SLR → simple LR: Easiest to implement. Lower powerful.
- ② CLR → Canonical LR: Most powerful. Most Expensive.
- ③ LALR → Look ahead LR: Intermediate in power and cost b/w the above two method.

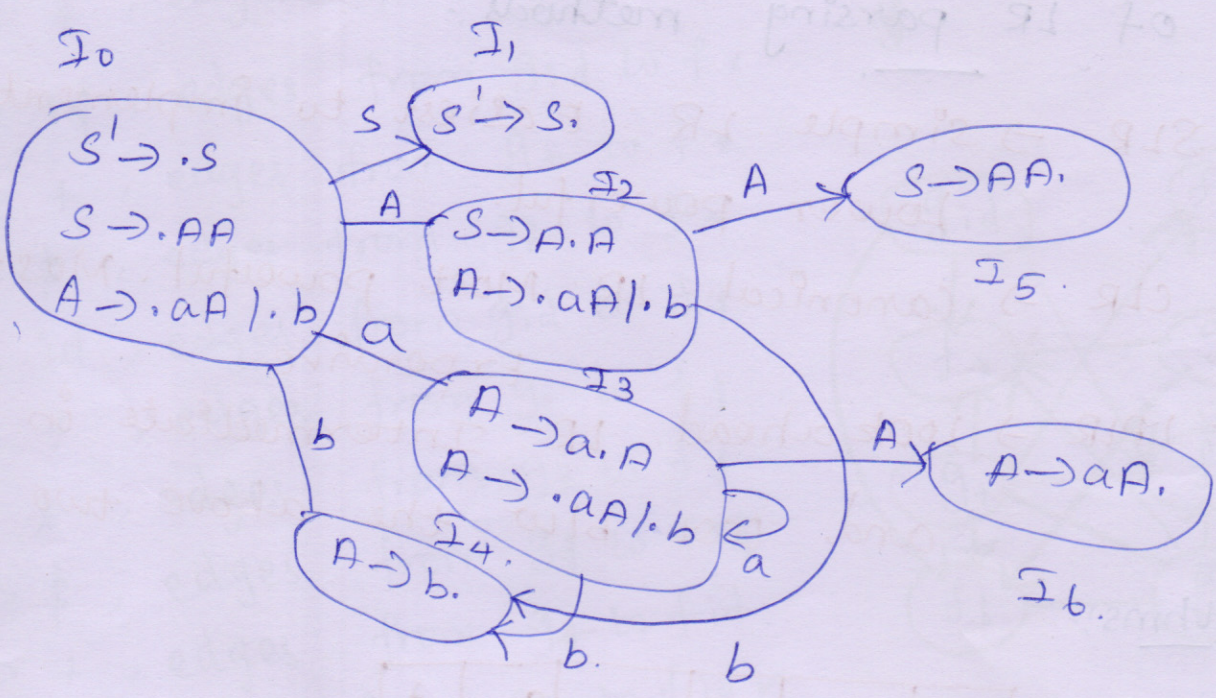
Algorithms:





$S \rightarrow AA$

$A \rightarrow aA \mid b$



	Action.			Go to	
	a	b	\$	A	S
0	S <sub>3</sub>	S <sub>4</sub>		2	1
1			Accept		
2	S <sub>3</sub>	S <sub>4</sub>		5	
3	S <sub>3</sub>	S <sub>4</sub>		6	
4	r <sub>3</sub>	r <sub>3</sub>	r <sub>3</sub>		
5	r <sub>1</sub>	r <sub>1</sub>	r <sub>1</sub>		
6	r <sub>2</sub>	r <sub>2</sub>	r <sub>2</sub>		



## Steps for SLR Parser Problem

1. write an augmented grammar.
2. write the closure of starting NT
3. Apply goto() functions of for all symbols.
4. Computation of FIRST and FOLLOW.
5. Construct Parsing Table.
6. check the input string with stack implementation.

Grammar :- eg

- ①  $S \rightarrow CC$
- ②  $C \rightarrow cC$
- ③  $C \rightarrow d$

& check the I/P string "cdcd" and "ccd".

Step 1: The augmented grammar  $G_1$  is.

- $S \rightarrow S'$   
 (1)  $S \rightarrow CC$   
 (2)  $C \rightarrow cC$   
 (3)  $C \rightarrow d$

- $Goto(I_0, c) = I_3$   
 $C \rightarrow c.C$   
 $C \rightarrow .cC$   
 $C \rightarrow .d$

Step 2: closure ( $\{ S \rightarrow .S' \}$ ) =  $I_0$ .

- $S \rightarrow .S'$   
 $S \rightarrow .cC$   
 $C \rightarrow .cC$   
 $C \rightarrow .d$

- $Goto(I_0, d) = I_4$   
 $C \rightarrow d$

Step 3: Apply goto function.

- $Goto(I_0, S) = I_1$   
 $S \rightarrow S'$

- $Goto(I_1, S) = NIL$   
 $Goto(I_1, C) = NIL$   
 $Goto(I_1, d) = NIL$

- $Goto(I_0, C) = I_2$   
 $S \rightarrow C.C$   
 $C \rightarrow .cC$   
 $C \rightarrow .d$

- $Goto(I_2, S) = NIL$   
 $Goto(I_2, C) = I_5$   
 $S \rightarrow CC$   
 $Goto(I_2, c) = I_3$   
 $C \rightarrow c.C$   
 $C \rightarrow .cC$      $C \rightarrow .d$



$$\text{Goto}(\underline{I_2}, d) = I_4$$

$$c \rightarrow d.$$

$$\text{Goto}(I_3, S) = \text{NIL}$$

$$\text{Goto}(I_3, \underline{c}) = I_6$$

$$c \rightarrow cc.$$

$$\text{Goto}(\underline{I_3}, c) = I_3.$$

$$c \rightarrow c.c$$

$$c \rightarrow .cc$$

$$c \rightarrow .d$$

$$\text{Goto}(I_3, d) = I_4.$$

$$c \rightarrow d.$$

$$\text{Goto}(I_4, S) = \text{NIL}$$

$$\text{Goto}(I_5) = \text{NIL}$$

$$\text{Goto}(I_6) = \text{NIL}$$

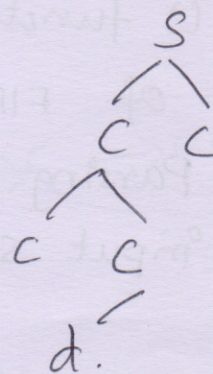
Step 4: Computation First

Grammar

$$S \rightarrow CC$$

$$C \rightarrow cC$$

$$C \rightarrow d.$$



$$\text{first}(S) = \{c, d\}$$

$$\text{first}(C) = \{c, d\}$$

Step 4: Computation Follow:

$$\text{follow}(S) = \{\$ \}$$

$$\text{follow}(C) = \{c, d, \$ \}$$

Step 5: Construct parsing Table:-

S → Shift (1)

R → Reduce (2)

	c	d	\$	S	C
0	S3	S4		1	2
1	S3	S4	Accept.		<del>3</del>
2	S3	S4			5
3	S3	S4			6
4	R3	R3	R3		
5			R1		
6	R2	R2	R2		



# Step 6: Stack Implementation:

Stack	Input string	Action.
0	<u>c</u> dcd \$	shift 3.
<del>0c3</del>	dcd \$	shift 4.
<del>0c3A</del>	ed \$	Reduce 3. $c \rightarrow d$ .
<del>0c3B</del>	<u>c</u> d \$	Reduce 2. $c \rightarrow cc$ .
0c2	cd \$.	shift 3.
0c2c3	d \$	shift 4.
0c2c3A	\$	Reduce 3. $c \rightarrow d$ .
0c2c3B	\$	Reduce 2. $c \rightarrow cc$ .
0c2c3C	\$	Reduce 1. $s \rightarrow cc$ .
0c2c3D	\$	Accept.

## Stack Implementation "ccd."

Stack	Input string	Action.
0	ccd \$	shift 3.
0c3	cd \$	shift 3.
0c3c3	d \$	shift 4.
0c3c3A	\$	Reduce 3. $c \rightarrow d$ .
0c3c3C	\$	<del>Reduce 2. <math>c \rightarrow cc</math></del>
0c3c3B	\$	<del>Reduce 2. <math>c \rightarrow cc</math></del>
0c3	\$	<del>Reduce 1. <math>s \rightarrow cc</math></del>
0c2	\$	Error.

Eg 2:  
 $E \rightarrow E + T \mid T$   
 $T \rightarrow T * F \mid F$   
 $F \rightarrow (E) \mid id$

Eg 3:  
 $s \rightarrow (L) \mid a$   
 $L \rightarrow L, s \mid s$



# Canonical Left to Right parser: (CLR).

LALR(1) CLR(1)

LALR

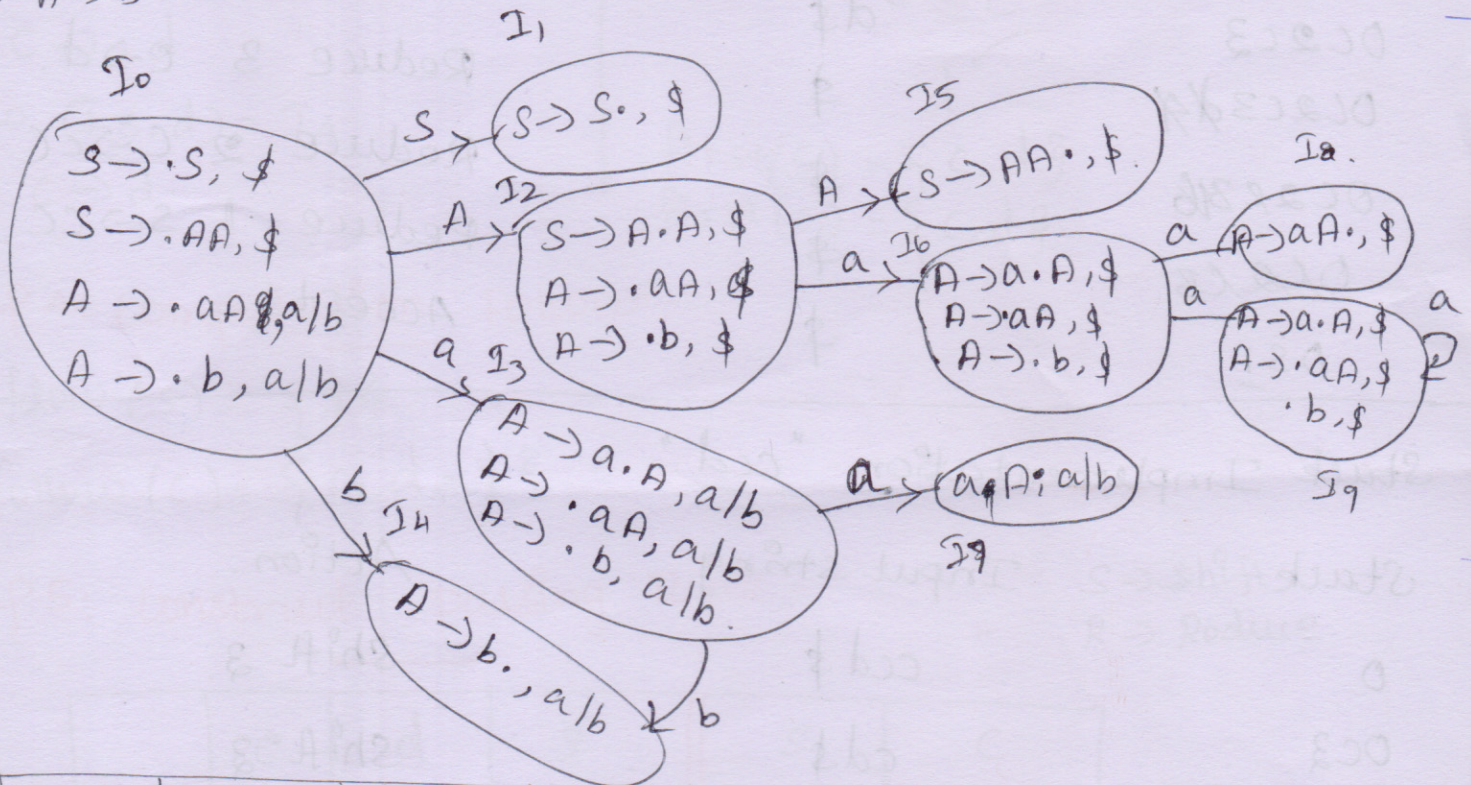
LR(1) Item = LR(0) items.

Grammar:

- ①  $S \rightarrow AA$ .
- ②  $A \rightarrow aA/b$ ,
- ③  $A \rightarrow b$

First(s) = {a, b}  
 (A) = {a, b}

Follow(s) = { \$ }  
 (A) = { \$, a, b }



	a	b	\$	S	A
0	S3	S4		1	2
1			Accept	1	5
2	S6				5
3	S8	S4			
4					
5	R5	R5	R5		
6	S9				
7	R2	R2	R2		
8	R2	R2	R2		
9	S9	S6			



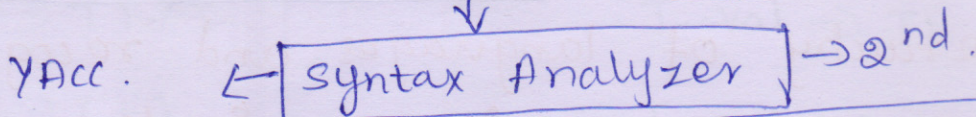
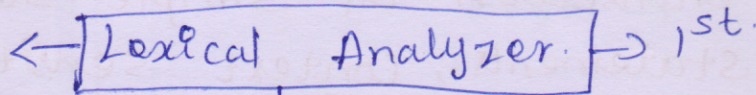
# YACC → Yet Another Compiler Compiler.

lex → Lexical Analyzer generator.

YACC → parser generator.

Its a tool which generate LALR parser.

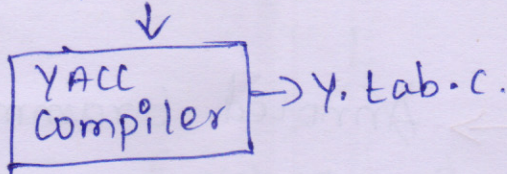
lex → RE specification.



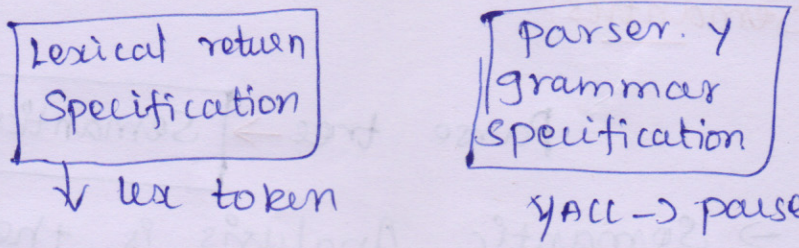
Grammar Specification.

## YACC working:

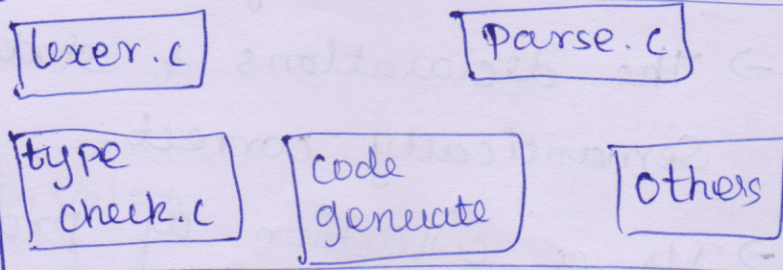
Step 1: YACC specification  
Parser. y



././  
supplementary code.  
Big picture of lex/YACC:

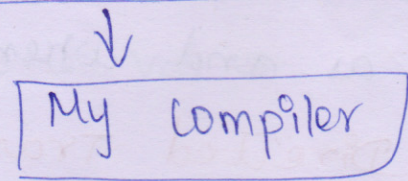


Step 2: Y.tab.c → [C Compiler] → a.out {S.A}

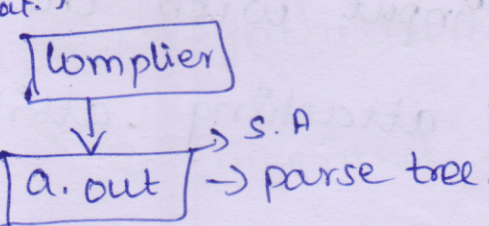


Step 3: i/p tokens LA → [a.out] → O/P {parse}

Grammar. Y → [YACC] → Y.tab.c {source Pgm by YACC}



{file containing desired grammar in YACC format} {YACC pgm}



Definition:  
Declaration of tokens & types of values used on a parse.

token gen by lex.

Rules:  
List of grammar rules with semantic return.

Syntax:  
definitions  
././  
Rules



## Unit - III

### ○ Semantics And Context Sensitive Features.

Semantics: (Syntax directed translations, S-attributed L-attributed grammars), Intermediate code-abstract syntax tree, translation of simple statements and control flow statements, Context sensitive features, Chomsky hierarchy of languages and recognizers, Type checking type conversions, equivalence of type expressions, overloading of functions and operations.

### Semantics:-

Parse tree → Semantics → Annotated Grammar.

→ Semantic Analysis is the third phase of compiler.

→ The declarations & statements of program are Semantically correct.

→ Its a collection of procedures which is called by Parser as and when required by grammar.

### Syntax Directed Translation:-

→ An associate it the input with the programming languages constructs by attaching attributes to grammar symbols.



Synthesized attributes

Eg:-

Production

Semantic Rules.

$L \rightarrow E S$

Print (E.val)

$E \rightarrow E1 + T$

$E.val \rightarrow E1.val + T.val.$

$E \rightarrow T$

$E.val \rightarrow T.val.$

$T \rightarrow T1 * F$

$T.val \rightarrow T1.val * F.val.$

$F \rightarrow (E)$

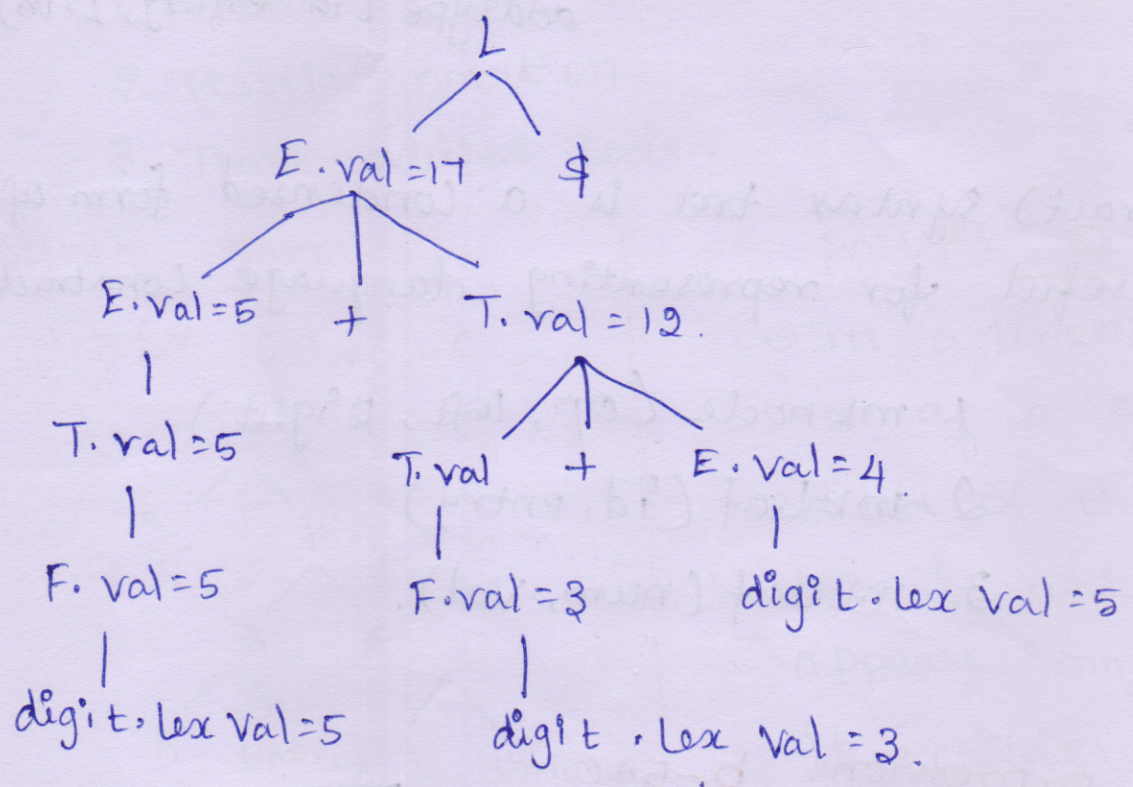
$F.val \rightarrow E.val.$

$F \rightarrow digit.$

$F.val \rightarrow digit, \text{lex val}.$

Eg2:

Input string:  $5 + 3 * 4 = 17$ . (Annotated parse Tree).



STD:

- 1. Synthesized Attributes
- 2. Inherited attributes.



## 2. Inherited attributes:

→ An inherited attribute is one whose value at a node in a parse tree is defined in terms of attributes at the parent and siblings of that node.

### Production

$D \rightarrow TL$

$T \rightarrow \text{id}$

$T \rightarrow \text{real}$

$L \rightarrow L_1, \text{id}$

$L \rightarrow \text{id}$

### Semantic Actions.

$L.in := T.type$

$T.type := \text{integer}$

$T.type := \text{real}$

$L_1.in := L.in$

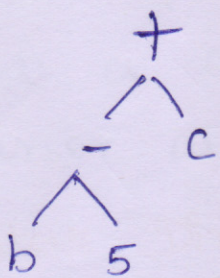
$\text{addtype}(\text{id.entry}, L.in)$

$\text{addtype}(\text{id.entry}, L.in)$

## Syntax Trees:

→ An (abstract) syntax tree is a condensed form of parse tree. useful for representing language constructs.

Eg:  $b-5+c$



1.  $\text{mknode}(\text{op}, \text{left}, \text{right})$

2.  $\text{mkleaf}(\text{id}, \text{entry})$

3.  $\text{mkleaf}(\text{num}, \text{val})$

Syntax tree expression:  $b-5+c$

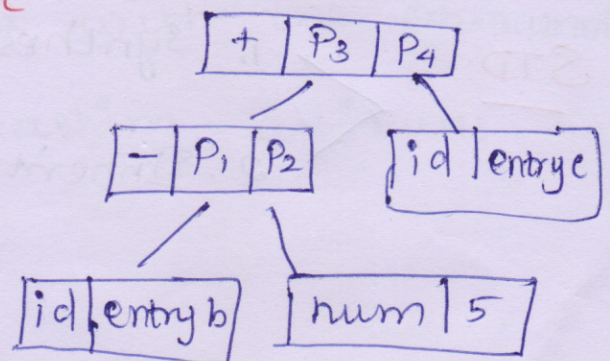
1.  $P_1 := \text{mkleaf}(\text{id}, \text{entry } b)$

2.  $P_2 := \text{mknum}(\text{num}, 5)$

3.  $P_3 := \text{mknode}(\text{'-'}, P_1, P_2)$

4.  $P_4 := \text{mkleaf}(\text{id}, \text{entry } c)$

5.  $P_5 := \text{mknode}(\text{'+'}, P_3, P_4)$





## Production

$$E \rightarrow E_1 + T$$

$$E \rightarrow E_1 - T$$

$$E \rightarrow T$$

$$T \rightarrow (E)$$

$$T \rightarrow id$$

$$T \rightarrow num$$

## Semantic Rules.

$$E.nptr := mknode('+', E_1.nptr, T.nptr)$$

$$E.nptr := mknode('-', E_1.nptr, T.nptr)$$

$$E.nptr := T.nptr$$

$$T.nptr := E.nptr$$

$$T.nptr := mkleaf(id, id.entry)$$

$$T.nptr := mkleaf(num, num.val)$$

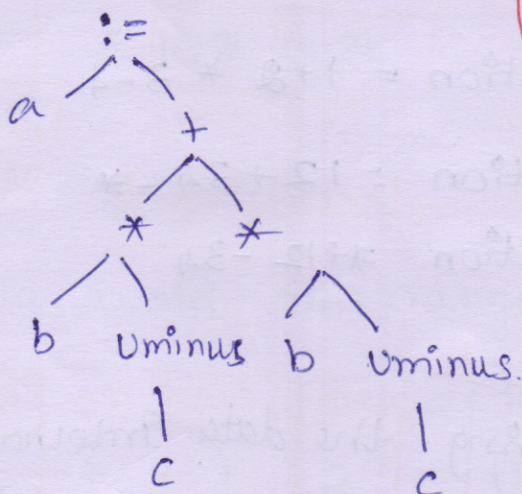
## Intermediate Languages:- (or) code

→ There are 3 kinds of intermediate representations

1. syntax trees
2. postfix notation
3. Three address code.

### Syntax Tree:

$$a := b * - c + b * - c$$



### 3. Three address code.

$$x := y / op z$$

$$x + y * z \text{ is,}$$

$$t_1 := y * z$$

$$t_2 := t_1 + x$$

### postfix notation

→ It is a linearised representation of a syntax tree, its a list of the nodes of the tree in which a node appears immediately after its children.

→ The postfix notation for above syntax tree is

$$abc \text{ uminus } *bc \text{ uminus } * + \text{ assign}$$



## Three address code:

- It contains maximum 3 addresses.
- Complex expressions can be converted into simple address format.

eg:

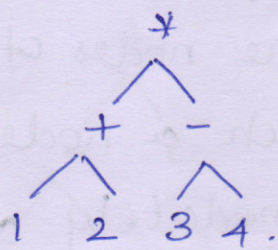
$a = (b+c) / d;$  →  $T_1 = b+c;$  →  $MOV\ b, R0$   
 $T_2 = T_1 / d;$  →  $MOV\ c, R1$   
 $a = T_2;$  →  $ADD\ R0, R1$   
 $MOV\ R1, T1$

- Its easy to generate and can be easily converted to machine code.
- It makes use of maximum three addresses, with temporary variables.
- The compiler decides the order of operation given by three address code.

## Three address code - generation:

- Parse tree into Linear representation.

eg:  $((1+2) * (3-4))$



→ Infix notation =  $1+2 * 3-4.$

→ Postfix notation =  $12+34-*$

→ Prefix notation =  $*+12-34$

## Representation of 3 address code:-

↳ It means storing the data internally.

- 1). Quadruple.
- 2). Triples
- 3). Indirect Triples.



## Quadruple representation:

→ Its a structure with consist of 4-fields namely Operator (op), operand (arg 1), arg 2 and Result.

repr	op	arg 1	arg 2	res.
(1)	+	1	2	3
(2)	-	3	4	-1
(3)	*	3	-1	-3

Eg:  $(1+2) * (3-4)$

$$T1 = 1+2$$

$$T2 = 3-4$$

$$T3 = T1 * T2$$

## Tuple Representation:-

→ To avoid extra temporary variable.

→ Remove Result column from the quadruple representation.

Eg:  $(1+2) * (3-4)$

repr	op	arg 1	arg 2
(1)	+	1	2
(2)	-	3	4
(3)	*	(1)	(2)

$$T1 = 1+2$$

$$T2 = 3-4$$

$$T3 = T1 * T2$$

→ Representation stored here.

Indirect

## Tuple Representation:-

→ To avoid rearrangement problem during optimization.

repr	op	arg 1	arg 2
(1)	+	1	2
(2)	-	3	4
(3)	*	(51)	(52)

psn	ptr.
(1)	(51)
(2)	(52)
(3)	(53)

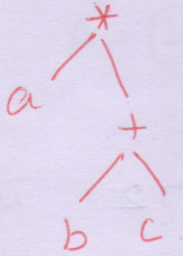


## Abstract Syntax Tree:

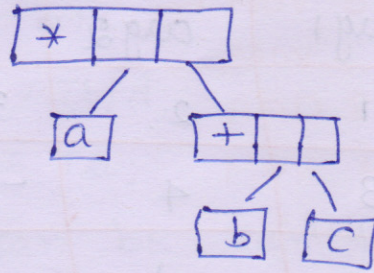
→ Its more compact than a parse tree and can be easily used by compiler.

eg:  $a * b + c$ .

parse tree.



## Abstract Syntax tree.



## Translation of Simple Statement into Control flow Statement:

In the Statement basically two types.

① Numerical Representation.

② Flow of control.

① Numerical Representation

Flow of control

→ To encode true / false value numerically.

→ position reached.

→ Evaluate Boolean expression like arithmetic expression.

→ convenient for if-then and loop Statement.

eg:

In the statement if (E) S

if-then

if-then-else

while-do

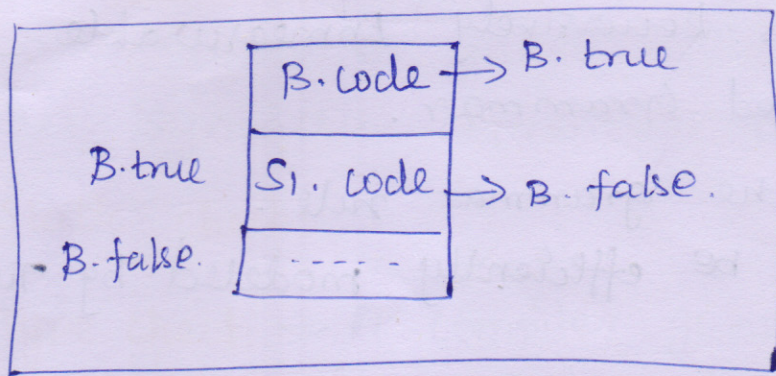
$S \rightarrow \text{if } (B) S_1$  ↗ Boolean expression

$| \text{if } (B) S_1 \text{ else } S_2$  → programming

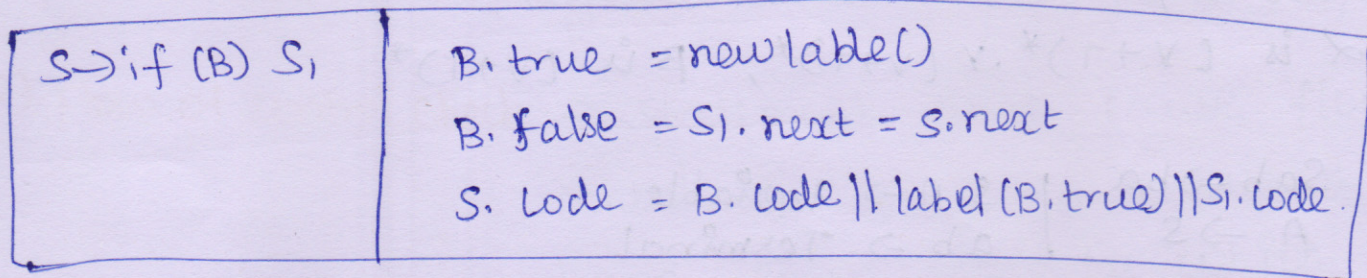
$| \text{while } (B) \text{ do } S_1$  → Statement



## Simple Statement:



code for the control flow statements.



$\rightarrow$  SPP.

Eg: 1.  $\text{if } (a < b) S_1$ .

$\rightarrow$  Assume that the attributes true & false exist for the entire expression as labels Ltrue & Lfalse res.

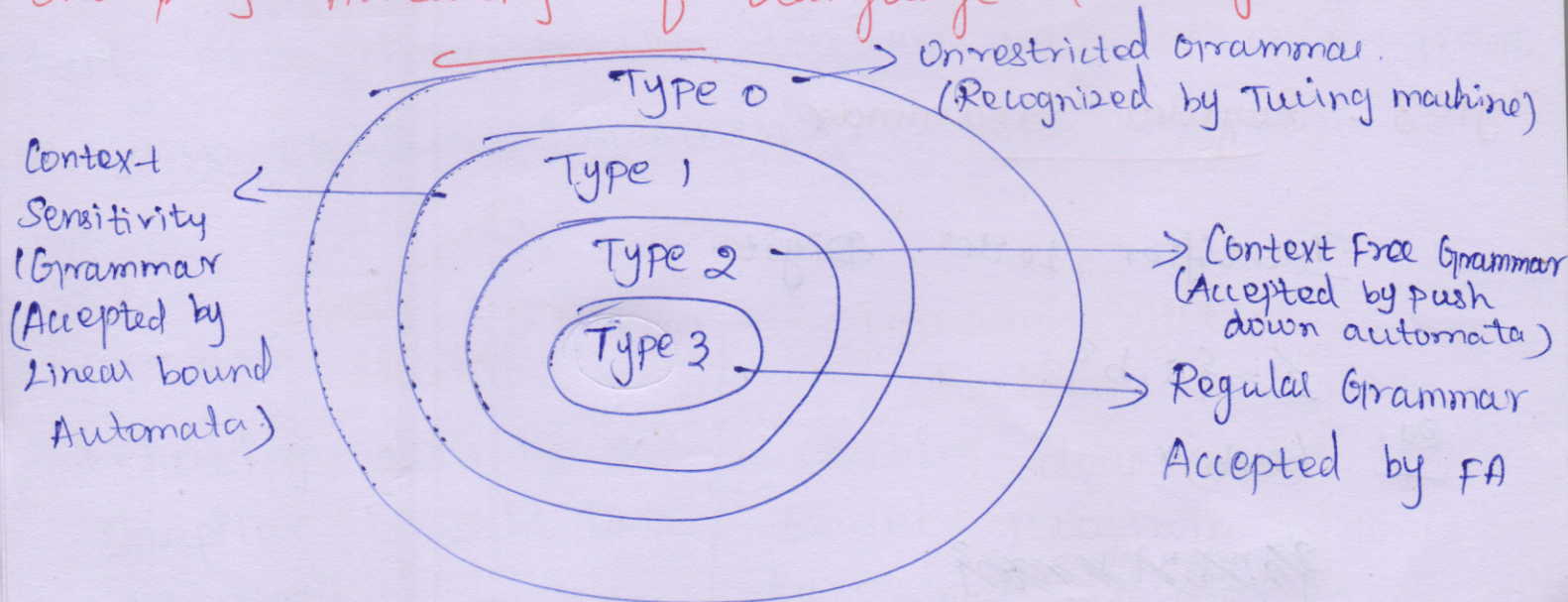
if  $a < b$  goto Ltrue  
 goto Lfalse

Ltrue:  $S_1.\text{code}$

Lfalse.

## Context Sensitivity Features

Chomsky hierarchy of language & recognizers.





## Type 0 - Unrestricted Grammar

→ Its also known as Recursively Enumerable language / Unrestricted Grammar.

→ No restriction as the grammar rule.

→ These language can be efficiently modeled by Turing machine.

$$\alpha \rightarrow \beta$$

$\alpha$  is  $(V+T)^* \cdot V (V+T)^*$ ,  $\beta$  is  $(V+T)^*$

Eg:

$S \rightarrow ba$  |  $S, A \rightarrow$  Variable.  
 $A \rightarrow S$  |  $ab \rightarrow$  Terminal.

## Type 1 - Context Sensitive Grammar

1) Eg:

$V \rightarrow T$
$S \rightarrow AT$
$T \rightarrow xy$
$A \rightarrow z$

## Type 2 - Context Free Grammar

$A \rightarrow aBb$

$A \rightarrow b$

$B \rightarrow a$ .

## Type 3 - Regular Grammar

Identifier, Letter, Digit.

$\Sigma = \{a, b\}$ .

Eg:  $(a+b)^*$

~~xxxxxxxxxxxxx~~



## Type checking:

→ A compiler must check the source program after syntactic convention is called static checking.

### Eg: static check:

(1) Type check → A compiler generate error if an operand is applied to an incompatible operand.

(2) Flow of control check → statement that cause flow of control to leave a construct must have some place to which to transfer the flow of control.

eg: break statement.

(3) Uniqueness check → An object must be defined exactly only once.

eg: labels in case statement.

(4) Name - Related check → Some times, the same name must appear two or more times.

Type system is a collection of rules of assigning type expressions to the various parts of a program.

A type checker implements a type system.

### Static Type checking

→ checking done by a compiler is said to be static.

### Dynamic Type checking.

→ checking done when the target program runs is termed as dynamic.



## Type Expressions:

→ A type expression is either a basic type or is formed by applying an operator called a type constructor to other type expressions.

1. Arrays.
2. Products
3. Records.
4. Pointers.

## Type checking expressions:

→ The synthesized attributes type for E gives the type expression assigned by the type system to the expression generated by E.

$E \rightarrow \text{literal } \{ E.type := \text{char} \}$ .

$E \rightarrow \text{num } \{ E.type := \text{integer} \}$

$E \rightarrow \text{id } \{ E.type := \text{lookup}(id, \text{entry}) \}$ .

When an identifier appears in an expression, declared type is fetched and assigned to the attribute type.

$E_1 \rightarrow E_1 \text{ mod } E_2 \{ E.type := \text{if } E_1.type = \text{integer and}$

$E_2.type = \text{integer then integer}$

$\text{else type-error} \}$ .

The expression formed by applying the mode operator to two subexpressions of type integer has type integer, otherwise, its type is type-error.

$E \rightarrow E_1[E_2] \{ E.type := \text{if } E_2.type = \text{int and}$

$E_1.type = \text{array}(s, t) \text{ then } t$

$\text{else type error} \}$ .



In any array reference  $E_1[E_2]$ , the index expression  $E_2$  must have type integer, in which case the result is element type  $t$  obtained from the type array  $(s, t)$  of  $E_1$ .

$E \rightarrow E, \uparrow \quad \{ E.type := \text{if } E_1.type = \text{pointer}(t) \text{ then } t \text{ else type-error} \}$

Type postfix operator  $\uparrow$  yields the object pointed to by its operand. The type of  $E\uparrow$  is the type  $t$  of the object pointed to by the pointer  $E$ .

### Overloading of functions and operations:-

→ Function overloading is defined as the process of having two or more function with the same name, but different in parameters. is known as function overloading.

→ The function is redefined by using their different types of arguments or a different number of arguments.

