

Formal Language & Regular Expressions.

(2)

→ It's a set of words, i.e) finite strings of letters symbols or tokens.

Regular Expressions.

→ A sequence of symbols & characters expressing a string or pattern to be searched for within a longer piece of text.

Languages (L)

Eg1: $\Sigma = \{a, b\}$.

$$\Sigma = \{a, b, c, \dots, z\}.$$

$$\Sigma^* = \{\epsilon, a, b, c, \dots, z, aa, ab, ac, \dots, zz, \dots, aaa, \dots\}.$$

Eg2:-

$$\Sigma = \{a, b\} = \Sigma^* = \{\epsilon, a, b, ab, ba, aa, bb, aaa, \dots\}$$

L = Set of all the strings starts with a.

$$L = \{a, aa, ab, aaa, abb, aab, \dots\}.$$

Eg3:

L = Set of all the strings ends with bb.

$$L = \{bb, abb, aabb, aaabb, \dots\}.$$

Language Definition:- (L).

Let Σ be an alphabet and Σ^* be the set of all strings over Σ . Consider a subset of Σ^* , this subset is called language over Σ and denoted by L.

$$\boxed{L \subseteq \Sigma^*}$$

↓
subset.

$$\Sigma = \{a, b\}.$$

$L = \{ \text{starts with } a \text{ and ends with } b \}$.

$$= \{ ab, aab, aabb, aaabb, abbb, \dots \}.$$

$$RE = a(a+b)^*b.$$

$$\Sigma = \{ 0, 1 \}$$

$L = \{ \text{ends with } 11 \}$.

$$= \{ 11, 011, 0011, 01011, 1111, 01111, \dots \}.$$

$$RE = (0+1)^* 11.$$

$$RE = \cancel{(0+1)^* 11} \cdot (a+b)^* bb = \{ \epsilon, a, b, aa, ab, ba, bb, \dots \} bb.$$

$$= \{ bb, abb, bbb, aabb, abbb, \dots \}.$$

$L = \{ \text{ends with } bb \}$.

Basic expression:

$$a^* = \{ \epsilon, a, aa, aaa, aaaa, \dots \}.$$

$$1^* = \{ \epsilon, 1, 11, 111, 1111, \dots \}.$$

$$(0+1)^* = \{ \epsilon, 0, 1, 01, 00, 10, 000, 1111, \dots \}.$$

$$(00)^* = \{ \epsilon, 00, 000, 0000, \dots \}.$$

$$(01)^* = \{ \epsilon, 01, 0101, 010101, \dots \}.$$

$$01^* = \{ \epsilon, 0, 01, 011, 0111, 01111, \dots \}.$$

$$L = \{ \text{starts with zero followed by } 0 \text{ to } n, \text{ no. of } 1's \}.$$

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