

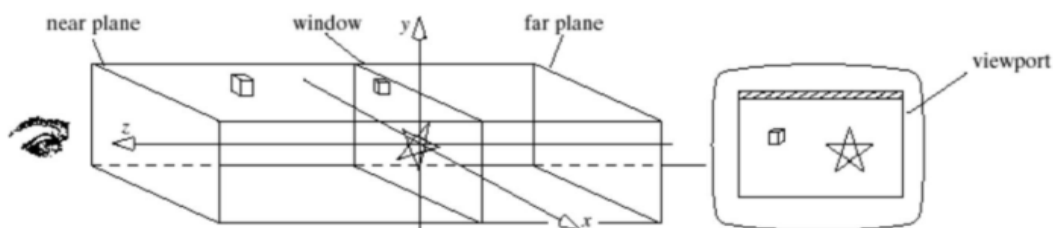
## DRAWING 3D SCENE INTERACTIVELY

### Drawing 3D Scenes in OpenGL

- We want to transform objects in order to orient and position them as desired in a 3D scene.
- OpenGL provides the necessary functions to build and use the required matrices.
- The matrix stacks maintained by OpenGL make it easy to set up a transformation for one object, and then return to a previous transformation, in preparation for transforming another object.

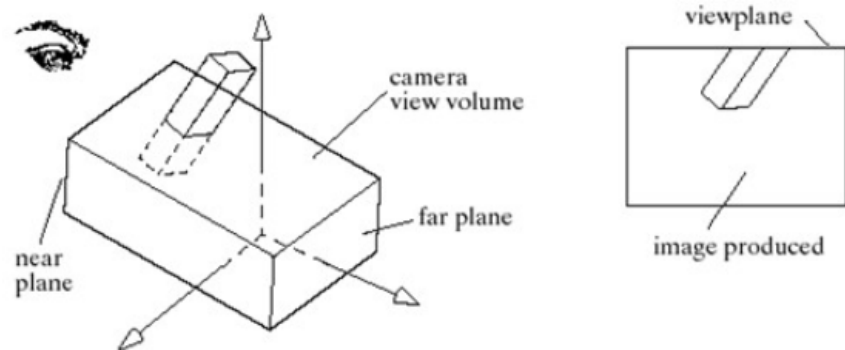
### Graphics Pipeline

- The 2D drawing so far is a special case of 3D viewing, based on a simple parallel projection.
- The eye is looking along the z-axis at the world window, a rectangle in the xy-plane.

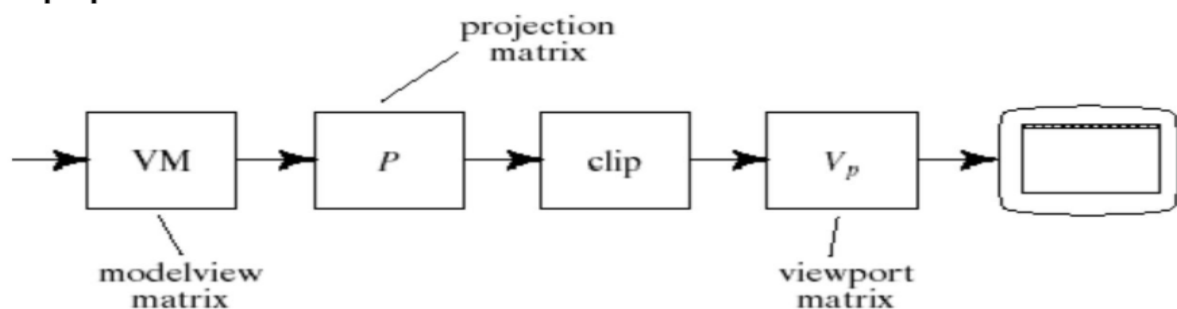


- *Eye* is simply a point in 3D space.
- The “orientation” of the eye ensures that the view volume is in front of the eye.
- Objects closer than *near* or farther than *far* are too blurred to see.

- In 3D, the only change we make is to allow the camera (eye) to have a more general position and orientation in the scene in order to produce better views of the scene.



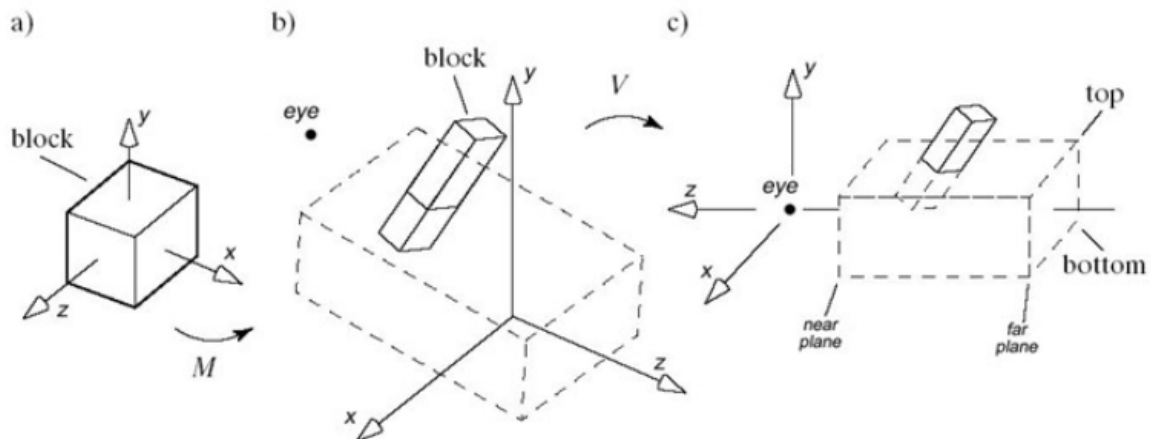
- OpenGL provides functions for defining the view volume and its position in the scene, using matrices in the graphics pipeline.



- Each vertex of an object is passed through this pipeline using `glVertex3d(x, y, z)`.
- The vertex is multiplied by the various matrices, clipped if necessary, and if it survives, it is mapped onto the viewport.
- Each vertex encounters three matrices:
  - The **modelview matrix**;
  - The **projection matrix**;
  - The **viewport matrix**;

# The Modelview Matrix (M)

- A modeling transformation  $M$  scales, rotates, and translates the cube into the block.



# The Projection Matrix

- The **projection matrix** scales and translates each vertex so that those inside the view volume will be inside a *standard cube* that extends from -1 to 1 in each dimension (Normalized Device Coordinates).
- Setting the Projection Matrix:
  - `glMatrixMode(GL_PROJECTION);`
  - `glLoadIdentity (); // initialize projection matrix`
  - `glOrtho (left, right, bottom, top, near, far); // sets the view volume parallelepiped. (All arguments are glDouble ≥ 0.0.)`
- $\text{left} \leq \text{vv.x} \leq \text{right}$ ,  $\text{bottom} \leq \text{vv.y} \leq \text{top}$ , and  $-\text{near} \leq \text{vv.z} \leq -\text{far}$  (camera at the origin looking along -z).

# The Viewport Matrix

- The **viewport matrix** maps the standard cube into a 3D viewport whose  $x$  and  $y$  values extend across the viewport (in screen coordinates), and whose  $z$ -component extends from 0 to 1 (a measure of the depth of each point).
- This measure of depth makes hidden surface removal (do not draw surfaces hidden by objects closer to the eye) particularly efficient.

