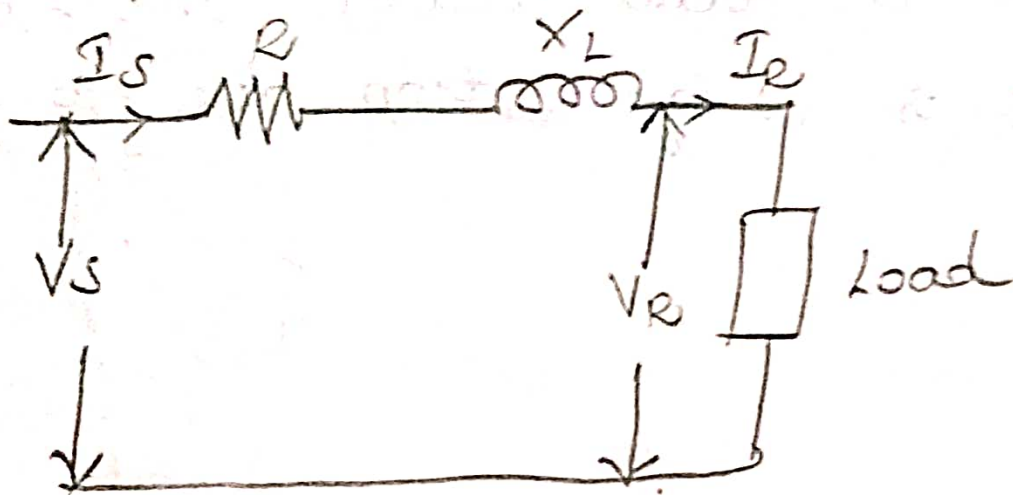


Short Tr. line



Capacitance is neglected.

Resistances & Inductance are considered

$$V_s = V_r + I_r R + j I_r X_L \quad \text{--- (1)}$$

$$V_s = V_r + I_r Z \quad \text{--- (1)}$$

$$I_s = I_r \quad \text{--- (2)}$$

Eq (1) & (2) is matrix form

$$\begin{bmatrix} V_s \\ I_s \end{bmatrix} = \begin{bmatrix} 1 & Z \\ 0 & 1 \end{bmatrix} \begin{bmatrix} V_r \\ I_r \end{bmatrix}$$

V_s - Sending end phase Voltage

I_s - " " " current

V_r - Receiving " " Voltage

I_r - " " " current

$Z = R + j X_L$ series im pedance

R - loop resistance, $X_L =$ inductive loop reactance

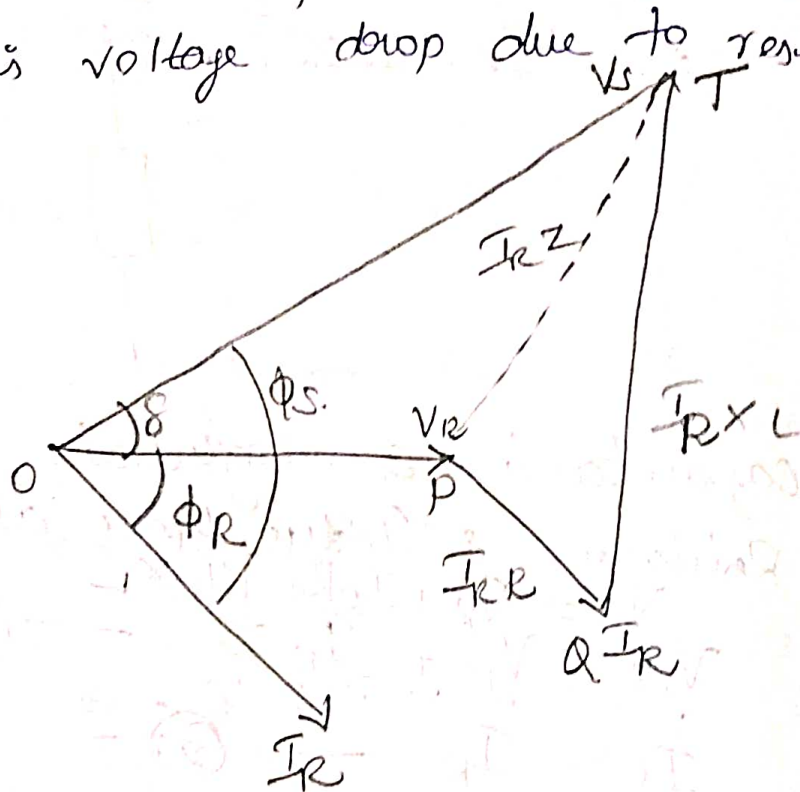
Lagging power factor load

Assume V_R as a reference vector, draw a line OP .

Draw I_R with lags V_R by angle ϕ_R

At P draw parallel line to I_R .

PQ is voltage drop due to resistance $I_R R$

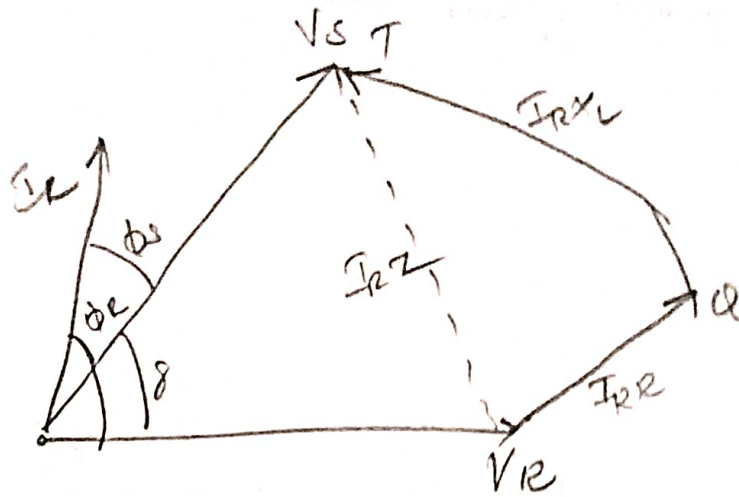


With Q as centre draw a 90° line which gives voltage drop due to inductive reactance $I_R X_L$ is ϕ_T .

PT gives voltage drop due to impedance $I_R Z$.

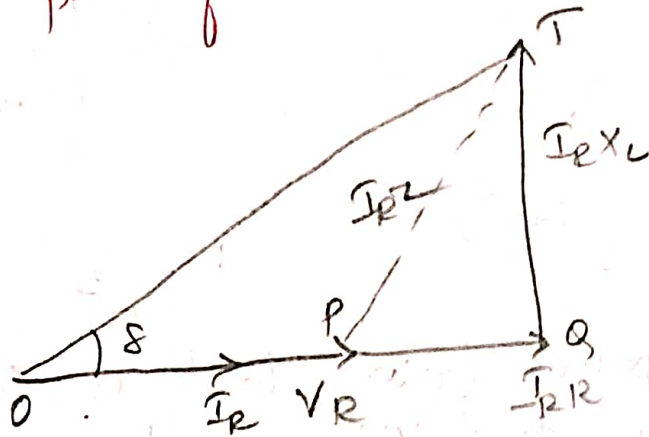
This OT which gives sending end phase voltage V_S and δ give the load angle.

Leading power factor load.



I_R leads V_R by an angle ϕ_R

Unity power factor load.



I_R is in phase with V_R

$$\cos \phi = 1$$

$$\phi = 0 = \phi_R$$

$$\cos \phi_R = \text{unity}$$

$$\cos \phi_s = \text{lagging}$$

$$Z = a + jb$$

$$jZ = j(a + jb)$$

$$jZ = ja - b$$

$$= -b + ja$$

$$0 + 90^\circ - \alpha$$

$$= 90^\circ$$

